Evidence for weak ferromagnetic moment within the basal plane of hematite natural crystals at low temperature

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[1] Low-temperature magnetization of hematite within the basal plane has been studied in a collection of natural crystals by means of torque magnetometry. Comparison between the torque curves at room temperature and at 77 K allows identification of a weak ferromagnetic moment constrained within the basal plane at temperatures well below the Morin transition. Annealing the samples produces the expected reduction of the weak ferromagnetic moment, but there is also a relationship between the ferromagnetic moment before and after annealing. Low-temperature measurements after the annealing experiment reveal the presence of a weak ferromagnetic moment that survives the annealing. This observation suggests the magnetic structure of natural hematite crystals below the Morin transition can still be a carrier of magnetization.

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1. Introduction

[2] Hematite is an iron oxide (α -Fe₂O₃) that represents the most oxidized state in the wüstite-magnetite-hematite system. It is present in a multitude of natural environments on Earth and it has also been reported on Mars [e.g., Moore, 2004; Squyres *et al.*, 2009]. Hematite has long been rec-

ognized as a stable and reliable carrier of natural remanent magnetization in rocks, which reflects the Earth's magnetic field [e.g., Butler, 1992]. However, in the particular case of sedimentary rocks, it has been postulated that the remanent magnetization carried by hematite falsely records the inclination of the ancient geomagnetic field in an effect that has been named “inclination

shallowing” or “flattening.” Inclination shallowing has important implications for the determination of paleolatitudes, because this will lead to a false paleolatitude, hence geographic position [e.g., *Bilardello and Kodama*, 2010a; *Garces et al.*, 1996]. Two main methods have been proposed for the correction of inclination. One is based on models of the past geomagnetic field [*Kent and Tauxe*, 2005; *Tauxe et al.*, 2008] and the second is based on measurements of the magnetic anisotropy [e.g., *Bilardello and Kodama*, 2010b; *Jackson et al.*, 1991; *Kodama and Sun*, 1992]. The use of one method or the other depends on technical aspects, such as number of data points, intensity, and quality of the signal or rock magnetic properties. To better understand the role of inclination flattening, better knowledge of the magnetic anisotropy of hematite single crystal is needed.

[3] Hematite is antiferromagnetic (AFM) at room temperature with a small canted moment lying within the crystal symmetry plane or basal plane (weak ferromagnetism, WFM) [e.g., *Dunlop and Özdemir*, 1997; *Néel*, 1953]. At low temperature, hematite undergoes a magnetic phase transition from WFM to a pure antiferromagnetic configuration (AF), which is known as the Morin transition [*Morin*, 1950]. It has been the object of a multitude of studies since the seminal work by Morin, with transition temperatures ranging from 235 to 263 K (see *Morrish* [1994] for a comprehensive summary on values and techniques).

[4] A number of earlier studies have reported a remanent magnetization below the Morin transition [*Flanders and Scheuele*, 1964; *Néel*, 1953; *Tasaki and Iida*, 1963a; *Tasaki et al.*, 1960], thus inferring a nonparallel structure of the spins along the *c* axis. More recently, a magnetoelastic origin of the spins’ misalignment has been proposed to explain the observed magnetization [*Özdemir and Dunlop*, 2005, 2006]. However, the exact orientation of this weak-ferromagnetic moment at low temperature (WFM-LT), with respect to the room temperature orientation and its relationship to the crystallographic *c* axes is still unknown.

[5] The behavior of hematite remanence at temperatures below the Morin transition may be important in planetary environments as a possible carrier of magnetization where its presence has been confirmed [*Squyres et al.*, 2009]. Mars is one example in our solar system, in which daily temperature ranges from 27°C (300 K) to −143°C (130 K) [*Liu et al.*, 2003], thus crossing the Morin transition on a daily basis [*Morin*, 1950]. There

are currently two hypotheses that could explain the magnetic anomalies measured in Martian crust. The first proposes three magnetic minerals common also in the Earth’s crust (magnetite, hematite, and pyrrhotite) that would carry the remanent magnetization [*Kletetschka et al.*, 2000, 2003]. The second hypothesis suggests that lamellar magnetism, the strong magnetic coupling in hemoilmenite exolutions [*Hargraves*, 1959], could be the origin of the Martian crustal anomalies [*Fabian et al.*, 2011; *Robinson et al.*, 2002]. The confirmation of a WFM-LT would add another possible source magnetic anomalies in the Martian crust.

[6] This work reports on a set of torque measurements from nine hematite natural crystals at room temperature and at 77 K. The measurements at room temperature are modeled by the theoretical function of torque curves in hematite plates due to the WFM constrained within the basal plane [*Martin-Hernandez and Hirt*, 2004; *Porath and Chalmers*, 1966]. The measurements at 77 K, below the Morin transition, can be divided in two types: (i) crystals that show pure antiferromagnetic behavior, i.e., similar to the torque curves of paramagnetic minerals [*Martin-Hernandez and Hirt*, 2001] and (ii) crystals that show WFM-LT constrained within the basal plane. Six of the samples were subsequently annealed during 24 h in order to release accumulated stress, reduce dislocation density, and reduce the defect moment [*Dunlop*, 1971]. Torque was remeasured after annealing at room temperature for all six crystals and at low temperature for two crystals.

2. Hematite Magnetic Structure

[7] Hematite crystallizes in the rhombohedral system, although it is commonly indexed using hexagonal axes, with a triaxial structure in the basal plane (0001) and *c* axes normal to it [*Coey*, 2010; *Giocavazzo*, 2011]. *Dzyaloshinsky* [1958] explained the presence of a WFM at room temperature using a thermodynamic model based on Landau’s theory of phase transition of the second kind [*Landau*, 1936]. The theory, which was further improved by *Moriya* [1960] by including the antisymmetric interactions of spin-orbit coupling, predicts three solutions that minimize the thermodynamic potential named States I, II, and III (the latter has only been found empirically in one study [*Flanders*, 1972]).

[8] For State I, solution of the thermodynamic potential at temperatures below 250 K, the spins are aligned antiferromagnetically parallel to the *c*

Table 1. List of Samples, Their Place of Origin, and Experiments Performed on the Crystal^a

Sample	Locality	Experiments
EH02a	Elba, Italy	TM high, TM low, HYS, IRM, FORC, HF-AMS RT/LT, AN HF-AMS RT/LT
EH03c	Elba, Italy	HYS, IRM, FORC, HF-AMS RT/LT, AN HF-AMS RT/LT
GB2b	Gorpibach, Switzerland	TM high, TM low, HYS, IRM, FORC, HF-AMS RT, AN HF-AMS RT
GB3	Gorpibach, Switzerland	TM low, HYS, IRM, FORC, HF-AMS RT/LT
GB4	Gorpibach, Switzerland	TM low, HF-AMS RT/LT, AN HF-AMS RT
KUKU	Kuckucksberg, Harghita, Romania	HYS, IRM, FORC, HF-AMS RT/LT, AN HF-AMS RT/LT
HEM2a	Elba, Italy	TM high, HYS, IRM, FORC, HF-AMS RT/LT
HEM3038	Madeira, Portugal	HYS, IRM, FORC, HF-AMS RT/LT
HEM3044b	Madeira, Portugal	TM high, HYS, IRM, FORC, HF-AMS RT/LT

^aTM: thermomagnetic curve; HYS: hysteresis loop; IRM: IRM and/or backfield IRM; RT: room temperature; LT: low temperature; HF: high-field torque; AN: annealed.

axis. It represents the highest symmetry configuration case. The theory, however, does not predict a remanent moment in ideal single crystals.

[9] For Stage II, the spins lie antiferromagnetically within the basal plane at temperatures above 250 K with a canted moment in the symmetry plane. For Stage III the spins also lie antiferromagnetically within the basal plane, but the canted moment falls within the *a-c* plane. State II would imply a remanent moment constrained within the basal plane, whereas State III would imply a remanent moment with a projection along the *c* axis.

[10] In addition to the canted moment at room temperature, hematite exhibits an additional weak, more variable magnetic moment referred as “defect moment” [Dunlop, 1971]. Most of the studies that have focused their attention on the hematite defect moment are based on remanence measurements [Dunlop, 1971; Ozdemir and Dunlop, 2006; Rochette *et al.*, 2005], but also on *H-M* magnetization curves [Besser *et al.*, 1967] or neutron diffraction [Curry *et al.*, 1965].

3. Samples and Methods

[11] Nine natural hematite crystals have been analyzed in this study, and the origin of the samples can be found in Table 1. The magnetic properties of the crystals were analyzed using a combination of the following rock magnetic methods (Table 1): (i) thermomagnetic curves between 77 and 973 K, (ii) acquisition of isothermal remanent magnetization (IRM) and subsequent back-field IRM, (iii) hysteresis loops up to 1 T, and (iv) first-order reversal curve (FORC) analysis within the basal plane of the crystal. Thermomagnetic curves at high temperature were carried out with a Vibrating Field Translation Balance (VFTB) [Krasa *et al.*, 2007] for samples HEM2 and HM3044b. IRM

acquisition curves, back-field IRM, hysteresis loops, and FORC diagrams were measured on a MicroMag 3900 Vibrating Sample Magnetometer (VSM) manufactured by Princeton Measurements Corporation. Low-field magnetic susceptibility was measured at low temperatures on an AGICO KLY-2 susceptibility bridge for samples GB3, HEM2, KUKU, and EH03A in order to determine the antiferromagnetic nature of the crystals at temperatures below the Morin transition.

3.1. High-Field Torque Magnetometer

[12] Samples were measured on a high-field torque magnetometer in at least five applied fields with angular steps of 20° or 30° at the Laboratory of Natural Magnetism (LNM), ETH-Zurich, Switzerland [Bergmüller *et al.*, 1994]. The measurement requires the sample to be measured in three mutually perpendicular positions in which one plane is the basal plane of the crystal. The samples were first measured at room temperature and subsequently measured at 77 K following the measurements protocols described by Martin-Hernandez and Hirt [2001] and Schmidt *et al.* [2007b], respectively.

[13] There is little literature about high-field torque magnetometry in the field of rock magnetism, but a good technical summary can be found in works such as Bhathal [1971] and Collinson [1983]. The magnetic torque determined in hematite and hematite-bearing rocks has been nicely summarized by Bhathal [1971] and Stacey and Banerjee [1974].

[14] When a magnetic field (**B**) is applied, the torque (**t**) can be computed as

$$\mathbf{t} = \mathbf{m} \times \mathbf{B} \quad (1)$$

where **m** is the magnetization of the sample with an applied field and **B** is the applied field. Paramagnetic and diamagnetic minerals have a

magnetization that is linearly dependent with an applied field, with a proportionality constant defined by the susceptibility tensor:

$$m_i = k_{ij}H_j \quad \forall i, j = 1, 2, 3 \quad (2)$$

m_i is the magnetization along the i direction, k_{ij} is the (i, j) term of the symmetric susceptibility tensor, and H_j is the applied field along the j direction. Applying equation (2), the magnetic torque will be proportional to the square of the applied field [Martin-Hernandez and Hirt, 2001; Owens and Bamford, 1976]. A sample rotated in the x_1 - x_2 plane, where the magnetic field is applied, would experience a torque in the perpendicular direction given by

$$t_3(\theta, B) = \frac{1}{2\mu_o} B^2 [(k_{22} - k_{11})\sin 2\theta + 2k_{12}\cos 2\theta] \quad (3)$$

where t_3 is the magnetic torque along the x_3 direction, B is the applied field, k_{ij} are the terms of the paramagnetic susceptibility tensor, and θ is the angle between the applied field and the x_1 direction. The torque signal is characterized by a periodic curve (Figure 1a) with increasing amplitude as a function of increasing the applied field. The amplitude can be fitted using a second-order polynomial with only the quadratic term (Figure 1b).

[15] Ferri/ferromagnetic minerals above their saturation have a magnetization, which is constant with applied field. Magnetic anisotropy is a function of differences in the demagnetization factor as well as the torque signal, which is constant with increasing applied fields [Martin-Hernandez and Hirt, 2001; Owens and Bamford, 1976]. Similar to the previous example, a sample rotated in the x_1 - x_2 plane, in which the magnetic field is applied, would experience a torque in the perpendicular direction given by

$$t_3 = \frac{1}{2\mu_o} M_s^2 [(N_{22} - N_{11})\sin 2\theta + 2N_{12}\cos 2\theta] \quad (4)$$

where t_3 is the magnetic torque, M_s is the saturation magnetization of the ferri/ferromagnetic phase, and N_{ij} is the (i, j) term of the demagnetization tensor. The torque curve is characterized by a periodic curve (Figure 1c), which does not increase its amplitude as the strength of the applied field is increased (Figure 1d).

[16] The magnetization in hematite crystals at room temperature is expressed as the sum of two terms

[Lin, 1959a; Tasaki and Iida, 1963b; Townsend, 1920]:

$$m = m_o + \chi H \quad (5)$$

where χ is the magnetic susceptibility and H is the applied field. The first term m_o is the weak ferromagnetic moment constrained within the basal plane that arises from a canting effect (m_o), and the second term is the induced magnetization due to the applied field. The torque of a sample at a certain applied field can be described by a first-order term that depends on the applied field and the weak ferromagnetic moment, and a second-order term that depends on the square of the applied field and the magnetic susceptibility [Kaczer and Shalnikova, 1964; Martin-Hernandez and Hirt, 2004; Porath and Chamalaun, 1966].

[17] The torque attributed to the weak ferromagnetic moment in a plane different than the basal plane is described by

$$t(\theta) = \text{sign}[\cos(\theta - \theta_o)] \frac{m_o B \sin(\theta - \theta_o) \sin^2 \varphi}{\sqrt{1 + \tan^2(\theta - \theta_o) \cos^2 \varphi}} \quad (6)$$

where θ is the orientation of the hematite with respect to the sample coordinates, θ_o is the initial orientation of the weak ferromagnetism with respect to the sample coordinates, m_o is the constant term of the WFM, φ is the angle between the hematite basal plane and the plane of rotation, and B is the applied field (Figure 2). Torque curves for hematite crystal and hematite bearing rocks are characterized by a drop in the torque signal when the term $\text{sign}[\cos(\theta - \theta_o)]$ changes value with torque drastically changing being +1 when the argument $\cos(\theta - \theta_o)$ is positive and vice versa.

[18] The torque from an antiferromagnetic material depends on the square of the applied field and its generic torque can be described by

$$t(\theta) = \frac{1}{2\mu_o} B^2 [(\chi_{\perp} - \chi_{\parallel}) \sin 2\theta] \quad (7)$$

where $\chi_{\perp}$ is the magnetic susceptibility perpendicular to the easy axes and $\chi_{\parallel}$ is the magnetic susceptibility parallel to the easy axes within the plane of measurement.

[19] The torque curve is characterized by a periodic function with a 2θ component. Figure 1e shows a typical torque curve for a hematite single crystal (or hematite-bearing rock) featuring a

Figure 1. (a, c, and e) Torque as a function of increasing applied field and angle and (b, d, and f) corresponding amplitude of the torque signal as a function of applied field for three typical magnetic behavior examples. Biotite single crystal with typical paramagnetic behavior (Figures 1a and 1b), hornblende crystal with a strong concentration of ferromagnetic inclusions above their saturation (Figures 1c and 1d) and hematite single crystal with typical canted antiferromagnetic behavior (Figures 1e and 1f).

sudden drop in the magnetization after the maximum torque value that coincides with a 180° change in the direction of the WFM within the basal plane [Porath and Chamalaun, 1966]. The amplitude of the torque signal increases linearly with increasing applied fields as predicted by the proposed model (Figure 1f).

[20] The torque amplitude at room temperature for every measurement angle has been fitted as a function of field strength into a polynomial of second order without ordinate. The fitting is automatic unless the correlation coefficient is lower than 0.97; N.B. the fitting was always automatic in this

study. The linear coefficient has been fitted as a function of angular position using equation (6). The orientation of the magnetization and its magnitude have been computed using a least squares nonlinear fitting of the curve with a MATLAB® subroutine developed by Martin-Hernandez and Hirt [2004].

[21] The torque curve at different applied fields has also been measured below the Morin transition at 77 K [Schmidt et al., 2007a, 2007b]. Similarly, the torque amplitude at all measuring angles has been fitted as a polynomial as a function of applied field. Some samples possessed a significant linear

Figure 2. Schematic diagram of the angular relationship between the hematite crystal, the orientation of the weak ferromagnetic moment within it (m), the plane of measurement (x - y), and the sample coordinate system. When $\mathbf{B}$ is the applied field, θ is the angle between the field $\mathbf{B}$ and the x direction of the sample coordinate system, θ_0 is the angle between the measuring plane x - y and the intersection of the crystal and this plane, and φ is the angle between the rotation plane and the crystal basal plane.

term of the polynomial, which has been fitted into the theoretical torque curve attributed to hematite in a WFM state (equation (6)). Other samples showed only a torque amplitude dependence on the square of the applied field, related to the magnetic susceptibility of hematite in an AF state [Martin-Hernandez and Hirt, 2001]. Torque curves in samples showing this behavior could be fitted using a series of trigonometric functions derived using Fourier analysis (equation (7)).

[22] Six of the samples were annealed in a Schoensted oven for 24 h at 650°C. After cooling the samples in a zero-field environment, the high-field anisotropy was measured at room temperature for all samples and at 77 K for three samples. The mathematical treatment of the signal is the same as described above.

4. Results

4.1. Rock Magnetism

[23] Thermomagnetic curves allow the determination of the Néel temperature of hematite. A small chip from samples GB2b, HEM2, and HM3044b was measured up to 700°C in order to define the temperature at which magnetization is lost. The three samples showed a Néel temperature of 680°C (Figure 3a) compatible with pure hematite [Dunlop and Özdemir, 1997]. Low-temperature thermomag-

netic curves were run on four samples and showed a Morin transition between 240 and 250 K. For example, samples GB3 and HEM2 (Figures 4a and 4b) show a drop in magnetization at 260 K (−13°C), characteristic of hematite Morin transition [Morin, 1950]. Samples KUKU and EH02A display a lower temperature Morin transition at about 240 K (−33°C) (Figures 4c and 4d).

[24] IRM acquisition curves and subsequent DC backfield IRM demagnetization show the same feature in all samples (Figure 3b). Magnetization increases with applied field and saturation in the basal plane is reached at approximately 600 mT. The coercivity of remanence is very similar in all samples with values that range from 12.1 to 70.1 mT (Table 2), which is compatible with hematite [Peters and Dekkers, 2003] and in particular with hematite single crystals [Martin-Hernandez and Guerrero-Suárez, 2012; Özdemir and Dunlop, 2006]. FORC diagrams measured within the hematite basal plane are characterized by a low coercivity also compatible with the bulk coercivity, obtained from the hysteresis loops (Figure 3d). The diagrams show two features that have been already reported in hematite single crystals. First, the maximum value of the diagram shifted toward negative values of H_u [Martin-Hernandez and Guerrero-Suárez, 2012]. Second, the shape of the maximum intensity is asymmetric following a pattern described by Brownlee et al. [2011] as “kidney shaped.”

4.2. Room Temperature Torque Curves

[25] The nine samples show similar features when torque curves are measured in a plane perpendicular to the basal plane (Figure 5). Here amplitude of the torque signal increases as a function of angle until it reaches a position where a sudden drop in torque occurs (Figure 5a). This coincides with the measurement within the basal plane where magnetization changes direction [Flanders and Remeika, 1965; Kaczer and Shalnikova, 1964; Porath and Chamalaun, 1966; Tasaki et al., 1962]. At any measurement angle, the torque amplitude increases with the applied field (Figure 5b). Torque as a function of field can be fitted by a polynomial of second order with no ordinate. The linear term originates in the WFM of hematite (equation (6)) and the second-order term is attributed the magnetic susceptibility of the antiferromagnet (equation (7)). The linear coefficient of the polynomial fitting, when plotted as a function of angular position, represents the torque per field exerted by the WFM moment constrained in the basal plane (Figure 5c). A least squares, nonlinear

Figure 3. Summary of rock magnetic properties within the basal plane for sample HM3044b. (a) Thermomagnetic curve from room temperature to 700°C showing the Curie temperature at 680°C, (b) IRM acquisition curve and subsequent back-field IRM demagnetization, (c) hysteresis loop after subtraction of the susceptibility of the reversible part, and (d) FORC diagram with an smoothing factor (SF) of 4.

Figure 4. Low-field susceptibility measurements within the basal plane from room temperature to 77 K for samples (a) GB3, (b) HEM2, (c) KUKU, and (d) EH02A.

Table 2. Rock Magnetic Properties of the Hematite Single Crystals Derived From Hysteresis Loops^a

Sample	Weight (g)	M_r (Am ² /kg)	M_s (Am ² /kg)	H_{cr} (mT)	H_c (mT)	H_{cr}/H_c	M_r/M_s
EH02A	0.10560	0.27225	0.70938	17.8	14.0	1.27	0.38
EH03C	0.01400	0.15464	0.23943	69.6	55.0	1.27	0.65
GB2B	0.16280	0.17881	0.32432	24.3	20.3	1.20	0.55
GB3	0.05360	0.20075	0.27817	79.5	55.2	1.44	0.72
GB4	0.18290	~	~	~	~	~	~
KUKU	0.08030	0.26772	0.32468	84.0	52.4	1.60	0.82
HEM2A	0.15591	0.20244	0.28844	29.0	24.9	1.16	0.70
HM3038	0.32310	0.04493	0.04720	12.3	10.0	1.23	0.95
HM3044b	0.13220	0.13900	0.18267	70.7	67.9	1.04	0.76

^a M_r is the remanent magnetization, M_s is the saturation magnetization, H_c is the coercivity field, and H_{cr} is coercivity of remanence.

fitting of the data for two perpendicular measurement planes, which are different from the basal plane, into the theoretical curve provides information about the magnitude and initial orientation of the ferromagnetic moment (Figure 5c and Table 3). The ferromagnetic moment ranges in magnitude from approximately 900 A/m to a maximum value of 2923 A/m, similar to specific measurements of the weak ferromagnetic moment in hematite [Morrish, 1994]. The computed ferromagnetic moment tends to lie in the direction of the first applied field, i.e., the declination is close to zero, the value of the first orientation. Schmidt and Fuller [1970] also noted this when examining magnetic anisotropy in the basal plane of hematite with low field methods. The inclination of the magnetization, with respect to the hematite basal plane is very flat, with a maximum deflection of 17°, which is within the uncertainty of the orientation of hematite crystals (Table 3).

4.3. Low-Temperature Torque Curves

[26] Eight of the natural crystals have been measured at liquid nitrogen temperature (Figure 6).

Measurements in a plane perpendicular to the basal plane show two different types of behavior. The torque curves as a function of applied field for samples HEM2A and HM3038 have a symmetrical shape (Figure 6a). At any given measurement angle, the torque amplitude depends only on the square of the applied field (Figure 6b). The proportionality coefficient derived from the fitting, when plotted as a function of angular orientation, can be modeled with a symmetric trigonometric function with a frequency of 2θ (Figure 6c). These samples, therefore, show no WFM-LT below the Morin transition.

[27] The other six samples showed a different torque signal when measured as a function of orientation. The curve is similar to the measurements at room temperature, with a strong asymmetry with respect to the vertical axes (Figure 6d). At one fixed angular position, the torque can be fitted as a function of applied field into a second-order polynomial with a significant linear term (Figure 6e). The computed linear coefficient, when represented as a function of orientation can be fitted using the model of torque for a weak ferromagnetic moment proposed for hematite at room temperature (Figure 6f).

Figure 5. Summary of torque measurements at room temperature in a plane perpendicular to the hematite basal plane at different applied fields for sample HM3044b. (a) Torque curve of a hematite crystal within the basal plane as a function of applied field for fields ranging from 0.6 to 1.5 T at 100 mT step, (b) amplitude of the torque signal as a function of applied field at one fixed angle of 30° with respect to the origin and least square polynomial fitting, and (c) linear component of the torque signal as a function of the applied field and fitting into the theoretical function described by Martin-Hernandez and Hirt [2004].

Table 3. Ferromagnetic Moment Constrained Within the Basal Plane of Hematite Natural Crystals Derived From Torque Curves and Initial Orientation (Declination D and Inclination I) of the Weak Ferromagnetic Moment Within the Basal Plane in the Sample Coordinate System^a

Sample	Mass (gr)	300 K						77 K					
		m_1 (A/m)	I_1 (deg)	D_1 (deg)	m_2 (A/m)	I_2 (deg)	D_2 (deg)	m_1 (A/m)	I_1 (deg)	D_1 (deg)	m_2 (A/m)	I_2 (deg)	D_2 (deg)
EH02A	0.1056	2147	16.3	1.5	2382	5.9	5.5	1766	43.0	12.9	×	×	×
EH03C	0.0140	869	0.0	0.0	1007	11.5	15.0	×	×	×	×	×	×
GB2B	0.0952	2923	4.0	4.1	2650	4.9	2.5	~	~	~	~	~	~
GB3	0.2889	2916	13.6	1.9	2851	11.1	1.0	2393	0.0	0.0	2196	0.0	0.0
GB4	0.2960	2368	17.0	2.4	2412	17.9	1.9	1070	19.8	7.0	1018	19.7	5.9
KUKU	0.0432	2237	10.1	2.7	2097	0.0	4.2	1812	0.1	0.0	1859	0.1	0.1
HEM2A	0.1559	1000	7.0	12.1	1021	8.3	12.3	No ferromagnetic moment					
HM3038	0.3231	1787	0.1	0.1	1833	4.1	2.5	No ferromagnetic moment					
HM3044b	0.1322	1258	6.7	5.1	1433	9.0	9.7	1291	8.9	10.0	1288	11.8	10.6

^aMeasurements are done at two temperatures above (300 K) and below (77 K) the Morin transition of hematite. Tilde symbol is shown in samples where the measurement was not possible for technical reasons and cross symbol measurements where the proposed model for the magnetization did not converge.

[28] Table 3 summarizes the magnitude and initial orientation of the WFM of samples, where a WFM moment has been modeled at temperatures below

the Morin transition. Samples EH02A and EH03C had a very noisy signal when measured at low temperature. The magnitude of the ferromagnetic

Figure 6. Comparison between the torque curve at 77 K for (a–c) sample HEM2 with no indication of weak ferromagnetic moment and (d–f) sample KUKU with a strong indication of weak ferromagnetic moment within the basal plane measured in a plane perpendicular to the hematite basal plane. Figures 6a and 6d show the torque curve as a function of the applied field at low temperature, Figures 6b and 6e show the amplitude of the torque signal at one angular position as a function of applied field and fitting into the best polynomial function. Figures 6c and 6f are the main coefficients of the polynomial fitting as a function of angular position and best theoretical fitting, where Figure 6c has been modeled as a trigonometric function by Fourier analysis and Figure 6f has been modeled with the model proposed by *Martin-Hernandez and Hirt* [2004].

Figure 7. Comparison between the torque curves at (a–c) room temperature and (d–f) low temperature for sample KUKU after annealing at 650°C during 24 h.

moment at 77 K ranges from 1018 A/m in sample GB4 to 2393 A/m in sample GB3. The moment is always smaller than the magnetization computed at room temperature for all the analyzed samples. The initial orientation of the weak ferromagnetic moment is similar to the direction of the first applied field in the measurement protocol.

4.4. Annealing Experiments

[29] Six samples have been annealed for 24 h in a magnetically shielded environment in order to reduce the intralattice stress, dislocation, and defects. The magnetic moment of hematite is known to decrease after annealing [Dunlop, 1971]. Measurements at room temperature after annealing show similar features to the samples before heating (Figures 7a–7c). The torque curves are characteristic of hematite crystals and hematite bearing rocks when measured in a plane perpendicular to the basal plane (Figure 7). They are periodic curves characterized by a sudden drop in the torque value when the field is applied in the direction containing the basal plane, similar to those described by Owens [1981] (Figure 7a) and an amplitude of the torque signal that depends on both the square of the applied field and applied field (Figure 7b). The linear coefficient of the torque amplitude when represented as a function of

applied field shows the characteristic feature of the torque due to a weak ferromagnetic moment constrained in the crystals basal plane (Figure 7c). It can be satisfactorily fitted using the corresponding theoretical function (equation (6)).

[30] Table 4 summarizes the three parameters that describe the weak ferromagnetic moment by means of torque magnetometry. The magnitude of the magnetization after annealing measured at room temperature is lower than measurements before annealing (Tables 3 and 4). However, despite the general decrease of magnetic moment associated with the annealing experiments, the initial direction of the weak ferromagnetic moment remains very similar before and after heating. Annealing decreases the magnetic moment determined by torque magnetometry, with the exception of sample KUKU.

[31] Three of the samples have also been measured at low temperature after being annealed (Figures 7d–7f and Table 4). Although the torque curve is weaker than the measurements at 77 K before annealing the samples, they still show the characteristics of the weak ferromagnetism (Figure 7d). The amplitude of the torque signal also depends on both the square of the applied field and the applied field (Figure 7e). The linear term of the polynomial fitting of torque as a function of field

Table 4. Ferromagnetic Moment Constrained Within the Basal Plane of Hematite and First Anisotropy Constant After Annealing the Samples in a Zero Field Environment for 24 h at 650°C^a

Sample	Mass After Anneal (g)	300 K						77 K					
		m_1^a (A/m)	I_1^a (deg)	D_1^a (deg)	m_2^a (A/m)	I_2^a (deg)	D_2^a (deg)	m_1^a (A/m)	I_1^a (deg)	D_1^a (deg)	m_2^a (A/m)	I_2^a (deg)	D_2^a (deg)
EH02A	0.1056	210	16.0	1.4	198	8.1	10.7	182	21.4	11.1	×	×	×
EH03C	0.0140	837	8.3	21.2	900	18.3	4.7	×	×	×	×	×	×
GB2B	0.0952	2482	1.9	2.0	2674	15.6	0.3	~	~	~	~	~	~
GB3	0.2889	237	13.3	13.4	290	20.6	1.8	~	~	~	~	~	~
KUKU	0.0420	2096	2.4	1.4	2102	1.2	0.8	1893	0.5	0.7	1900	2.1	0.4

^aSymbols and terms as explained in Table 3. Tilde indicates samples where the LT torque curve could not be measured.

can be modeled following the function of a weak ferromagnetic moment constrained within the crystal's basal plane (Figure 7f). The ratio of magnetization at room temperature and 77 K is approximately 1.1.

5. Discussion

[32] Despite the large variation of the hysteresis parameters in the basal plane, H_c , H_{cr} , M_s , and M_r , their hysteresis ratios are relatively well confined with high magnetization and low coercivity ratios, similar to those reported in *Martin-Hernandez and Guerrero-Suárez* [2012] and *Ozdemir and Dunlop* [2006]. Table 2 summarizes the results from the set of samples analyzed in this study, which indicates that these crystals display a range of all possible crystalline anisotropy structures. M_r/M_s within the basal plane above 0.75 are indicative of a triaxial crystalline anisotropy structure, whereas values close to 0.5 are indicative of a uniaxial crystalline anisotropy structure [*Dunlop and Özdemir*, 1997].

[33] Figure 3 shows representative rock magnetic properties for the hematite crystals. In particular, hysteresis loops for the crystals show a reversible behavior at fields higher than 500 mT, even for sample HM3044b, the sample with highest coercivity (Table 2). FORC diagrams, however, reveal an asymmetric (kidney) shape and shift in FORC distribution to the field of negative interaction characteristic of unsaturated diagrams [*Beron et al.*, 2011]. The magnetization in the basal plane requires a higher field than suggested from the hysteresis loops, in order to achieve full saturation [*Beron et al.*, 2011].

[34] Table 3 summarizes the initial orientation and magnitude of the WFM at room temperature. Although the reported values appear to be well constrained, with a mean value of 2500 A/m [*Lin*,

1959b; *Néel*, 1953] the moment from the samples in this work shows a wide range of values. This variation can be explained by several mechanisms that will reduce the parasitic ferromagnetism of hematite, including doping of the lattice with cations other than Fe [*Flanders and Remeika*, 1965; *Tasaki et al.*, 1962] or oxidation [*Tasaki et al.*, 1960]. A more detailed compositional analysis would be required in order to explore the origin of this variability in the ferromagnetic moment, but it is not allowed for our collection of crystals.

[35] The torque measurements shown in Figure 6 confirm the presence of a WFM constrained within the crystals' basal plane both at room temperature and at 77 K in five of the eight samples studied. Low-temperature torque curves were previously reported in studies of the Morin transition, magnetic anisotropy and general magnetic properties [*Bogdanov*, 1973; *Flanders and Remeika*, 1965; *Kaczer and Shalnikova*, 1964; *Tasaki and Iida*, 1963a; *Vlasov and Fedoseyeva*, 1968]. All of these measurements were concentrated on synthetic crystals with no evidence of a WFM at low temperatures. The origin of the ferromagnetic moment at room temperature has been traditionally explained by the presence of an interaction term described in the Dzyaloshinsky-Moriya model [*Dzyaloshinsky*, 1958; *Moriya*, 1960]. However, theory predicts pure antiferromagnetic behavior below the transition temperature. The presence of a moment at low temperature has already been reported in natural crystals [*Gallon*, 1968; *Lin*, 1959b; *Ozdemir and Dunlop*, 2006] but not in synthetic samples [*Lin*, 1961]. The magnetic moment measured at 77 K decreases significantly with respect to the values at room temperature (Table 3), but the amount of this decrease varies from one sample to another.

[36] The initial orientation of the ferromagnetic moment is very close to the direction of the first applied field in all the samples with a maximum

Figure 8. Schematic depiction of the possible spin configuration within the hematite lattice and resulting magnetic moment within alternating lattices (a) above the Morin transition and (b) below the Morin transition. Location of Fe^{3+} within the hematite lattice modified after Nagata [1961].

deviation of 17.9° in sample GB4. This initial orientation of the magnetic moment is maintained after rotating the sample into the second measuring position. It is noteworthy that the initial orientation of the magnetization is also close to the direction of the first applied field at low temperatures (Tables 3 and 4). This phenomenon was also reported for low-field susceptibility [Schmidt and Fuller, 1970; Tasaki *et al.*, 1962].

[37] The origin of the unexpected magnetization at low temperatures has long been discussed, and two explanations have been postulated to explain its presence. The first hypothesis is that it is related to defect density, based on the effect that annealing has on the reduction of this magnetization [Néel, 1953; Tasaki *et al.*, 1960]. Because crystallographic twinning has been reported to tilt Bloch walls out of the basal plane of hematite crystals [Tanner *et al.*, 1988], this may be another type of crystalline defect, which is important in preserving a WFM at low temperature. The second idea is that the magnetization has a crystallographic origin [Hirai *et al.*, 1971; Özdemir and Dunlop, 2006].

[38] The samples in this study show that annealing does reduce the magnetization being particularly important in sample EH02A. This result implies that defects, dislocations, impurities, stress field, and/or twinning influence the WFM measured by torque magnetometry [Dunlop, 1971]. The defect moment in the hematite magnetization therefore has a strong influence in the WFM measured. However, the measured WFM-LT survives annealing, which suggests that there is either another mechanism that also influences the magnetization at low temperatures within the basal plane, or there is no complete removal of the defects by annealing.

[39] Since the WFM is constrained within the basal plane, a more in-depth analysis of the anisotropy within the symmetry plane is needed at the conditions proposed in this work, RT-LT before and after annealing.

[40] Because current theories about the magnetic anisotropy of hematite within the basal plane suggest it is influenced by the magnetoelastic properties [Martin-Hernandez and Guerrero-Suárez, 2012; Özdemir, 2008], further work is needed to understand whether the anisotropy within the basal plane controls the WFM at low temperature (Figure 8).

[41] The analysis of the spin orientation at low temperature could be completed by correlating macroscopic torque measurements with neutron diffraction or Mössbauer spectroscopy and determining the microstructural changes and domain structure above and below the transition temperature. Also SEM, microscopy work, or X-ray topography within the basal plane could add in the interpretation of the role played by crystallographic structures in the presence of a WFM-LT.

6. Conclusions

[42] The presence of a weak ferromagnetic moment in hematite natural crystals has been detected at 77 K, well below the Morin transition. Classical theories of spin-canted antiferromagnetism predict that hematite should behave like a pure antiferromagnet below the Morin transition. However, the natural hematite crystals in this study show evidence for a WFM moment constrained within the hematite basal plane at 77 K. This WFM moment at low temperature persists even after annealing the samples.

[43] The initial orientation of the WFM moment is parallel, within measurement error, to the orientation of the first applied field. Annealing the samples at 650°C reduces the total magnetization from room temperature to 77 K, but a weak WFM persists and maintains the direction of the first applied field. These results suggest that hematite could possibly play a role in planetary magnetism at temperatures below the Morin transition.

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