

Optimization of nutrient concentration for citric acid production by solid-state culture of *Aspergillus niger* on polyurethane foams

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Citric acid production from mussel processing effluents by *Aspergillus niger* in solid-state culture was studied using polyurethane foam particles soaked with the culture medium. Conditions were used that allowed comparison of the results with those obtained before in submerged culture and the attribution of the differences to the characteristics of solid-state culture.

A screening of several strains gave different results than in submerged culture and a reduction in the incubation time. The joint effect of nitrogen and phosphorus initial concentrations was examined by means of orthogonal factorial designs in five selected strains. The results showed that different requirements of N and P for each individual strain were needed. Optimization was done using different experimental strategies for two selected strains. Following either the direction of the linear approximation gradient of the first-order empirical model obtained or with a new rotatable factorial design, an optimum value could be obtained.

In comparison with previous results in submerged culture, the strains with high requirements of N and P seemed to be disfavored in solid-state culture. The ones with low requirements were favored and showed a bigger tolerance to a surplus of both nutrients.

Keywords: Solid-state culture; citric acid production; mussel processing wastes; nutrient optimization; empirical models; *Aspergillus niger*

Introduction

Citric acid production is one of the possible procedures for exploitation of mussel processing wastes (MPW). This effluent, generated in the steam treatment of mussel, constitute (due to their high volume and organic load, average COD: 25 g O₂ l⁻¹; glycogen as main component: 10 g l⁻¹) an important eutrofication factor in the Galician Rias Baixas estuaries (Northwest coast of Spain). The process developed by our group initially in submerged culture (SC)¹⁻⁴ demonstrated the suitability of this media for citric acid production, the redundancy of pretreatment, and the importance of nitrogen and phosphorus concentrations.^{5,6} At present, our work has been redirected toward the development of solidstate culture (SSC) processes. This type of culture has shown positive results for citric acid production in previous reports⁷ and has advantages over SC. One of these is that SSC requires less economic investment, an important aspect when the intention is to encourage the application of methods for the treatment of wastes. Furthermore, the development in SSC of other bioproductions based on MPW also showed a production comparable or superior to that in SC.^{8,9}

Traditionally, SSC are characterized by the development of microorganisms in a low-water activity environment on a nonsoluble material that acts both as physical support and source of nutrients;¹⁰ however, it is not necessary to combine the role of support and substrate, but rather reproduce the conditions of low-water activity and high oxygen transference by using a nutritionally inert material soaked with a nutrient solution.^{7-9,11,12} Apart from the fact that this is the only possible option for utilization of a liquid waste like MPW, this SSC system shows interesting advantages from both theoretical and practical points of view. It permits the composition of the culture medium and support-depending (such as particle diameter or porosity) or interface-depending (as proportion of liquid phase in the system) physical factors to be varied independently. At the same time and most important for this work, this system allows a direct comparison with SC, and so to attribute the different results, using the same strains and culture medium composition, to the features of each type of culture.

Strain selection is an important factor for achieving high yield of citric acid. For each strain, the requirements of nitrogen and phosphorus concentration in the initial medium shows a great variability.⁵ The performance of the different strains depends also on the type of culture used. In fact, strains suitable for production in SC may not be suitable for solid-state production;¹³ moreover, the properties of SSC can condition the effect of

nutrients such as metal ions and minerals and consequently determine different optimal levels.¹⁴

Nitrogen and phosphorus limitation are crucial factors in citric acid production by *Aspergillus niger*.¹⁵⁻¹⁷ The negative effect of their excess makes hyperbolic models such as Michaelis and Menten or Monod type inadequate and unsuitable for optimizing nutrient concentration for citric acid production improvement. On the other hand, the interaction between both nutrients makes the study of their combined effect necessary as observed in our previous work⁵ and by other authors.¹⁸ To overcome both problems, empirical models based on factorial orthogonal or rotatable designs have proven to be useful.⁵ In previous work¹⁹ in fed-batch SC, nitrogen showed a regulating role important in production and having two effects. One effect was negative since, in excess, N promoted a bigger growth and consequently diverted the source of carbon toward energy and biomass production. The other effect was positive because a moderate input contributed to the maintenance of citric acid productive biomass.

The objective of this work has been to check the capability of different strains of *A. niger* in SSC and to establish the requirements of nitrogen and phosphorus in the culture medium. This was done applying the same methodology used for an analogous study employing SC.⁵ It was possible, therefore, to compare the tendencies resulting from the respective empirical models obtained for the same strains directly. Differences in behavior were shown to be conditioned by the type of culture.

Materials and methods

Microorganism and inoculum preparation

The 11 *A. niger* strains used (CBS, Baarn, Holland, identification numbers in Figure 1) were maintained on malt-yeast extract agar slants at 4°C by subculturing every month. For inoculum preparation, the spores were grown on a slant at 30°C for 7 days, and were scraped in distilled water solution. The spore density was measured by optical density measurement at 750 nm following calibration between this data and direct hemocytometer counting. The suspensions were centrifuged and the spores resuspended in the appropriate volume of culture medium.

Fermentation medium and culture conditions

The processing of MPW (clarification, concentration, and hydrolysis) were as described elsewhere.⁴ The basic medium (10M-H) used contained in g l⁻¹: glucose, 108; total nitrogen, 0.710; and total phosphorus, 0.060. The main fraction (~95%) of the nitrogen content was of proteic nature and approximately 75% could be used by *A. niger*.¹⁹ Initial pH of the medium was adjusted to 4.0 with 5 N HCl.

Solid-state culture was always prepared under conditions established in previously published results.⁷ The support was a commercial polyurethane foam with density 60 g dm⁻³ (COPO Iberica) cut into cylindrical particles with a diameter and height of 6 mm. The load per experimental unit (50 ml Erlenmeyer flask) was 0.372 g, approximately 40 foam cylinders, equivalent to an apparent volume of support of 6.2 cm³. The addition of liquid culture medium was done so that the foam attained 50% of the total liquid retention capacity which implies a volume of 2.83 ml per experimental unit.

Sterilization was performed by steaming for 1 h. Each experimental unit was inoculated with 20×10^6 suspended spores in a suitable volume of each culture medium under sterile conditions. The incubations were performed at 30°C in a heater with constant humidity and static conditions. To avoid possible agglomerations of the material due to fungal growth, the cultures were manually shaken once a day.

Factorial design

Empirical models for the production of citric acid with respect to nitrogen and phosphorus concentration were calculated for the different strains of *A. niger*. These models were obtained by means of a complete first-order orthogonal plan with quadruple replication in the center of the domain according to the procedures described by Akhnazarova and Kafarov²⁰ and Box et al.²¹ The strategies of optimization used with the most interesting strains were an extension of the experimental domain guided by the linear approximation gradient method (LAG) and the use of a second-order rotatable plan.

Extraction of the samples

At preestablished times, the whole content of each experimental unit was analyzed. The foam support was compressed in a syringe and washed repeatedly with distilled water. The extracts thus obtained were centrifuged at 5,000 rpm, and the analytical determinations performed on the corresponding supernatants. The sediment was added to the rest of the washed material for biomass estimation.

Analytical methods

Reducing sugars were estimated by means of the 3,5-dinitrosalicylic acid reaction²² with glucose as standard. Citric acid was measured by the spectrophotometric method of Marrier and Boulet.²³ Biomass was estimated by drying the washed material of each experimental unit over P₂O₅ under reduced pressure in a dessicator/oven at 55°C and then weighing. All analyses were performed in duplicate.

Results

Screening of the aptitude of different strains of *A. niger* for citric acid production

To select the better producing strains in SSC, a screening of the 11 available strains was conducted with the culturing conditions described above and using the concentration of nutrients in the liquid phase: glucose, 108 g l⁻¹; total nitrogen, 955 mg l⁻¹, and total phosphorus, 90 mg l⁻¹. The results were compared with those obtained in SC with the same medium under the conditions described elsewhere.⁵

The results obtained in SSC (Figure 1) showed an almost exhaustive consumption of the carbon source in most of the strains after an incubation period of 96 h. This is much earlier than in SC, which takes about 192 h. Later cultures confirmed that the maximum production of acid in SSC takes place between 48–72 h. Bearing this in mind, it can be supposed that in some cases, the determination of the produced acid was conducted already in a postoptimal phase. Despite this, the productivity of the individual strains in SSC showed marked differences with that obtained in SC.

Strains CBS 554–65, 120–49, 126–48, 246–65, and 733–88 were selected with the first two showing particularly good yields. (554–65 showed very similar productions in both modalities of culture). As with SC,⁵ the optimum concentration of nutrients (mainly nitrogen and phosphorus) may depend on the strain; therefore, the production of the five selected strains was studied with a wider range of concentrations of both nutrients.

Joint effect of initial levels of N and P in the selected strains

As described previously, surplus N or P exert a depressive effect on citric acid production in SC. Even at low levels, the optimum requirements of both nutrients depended greatly in the strain considered;⁵ thus, for studying an analogous behavior in SSC and with the aim of comparing the results, this aspect was studied with the selected strains by means of a first-order orthogonal factorial plan in the same experimental domain assayed in SC (Table 1).

With the culture conditions described, sampling time was reduced to 72 h (increasing production of the acid before carbohydrate exhaustion). The criterion for model acceptance was based on the Student's t test ($\alpha < 0.05$) for the coefficients and on the Fisher's F test (also $\alpha < 0.05$) applied to the ratios: experimental error/total error and lack of fit/experimental error for the global validity.

At such levels of significance, only the behavior of strain 120–49 could be described by means of a linear model (Table 2). For the others, the model was acceptable with respect to the relation total error/experimental error, but it was not in regard to the relation lack of fit/experimental error, showing the existence of more or less pronounced curvatures; nevertheless, the results obtained (Figure 2) allowed selection criteria and the improvement direction to be established as discussed below.

Strain 554–65 clearly performed as the most efficient for citric acid production in this culturing mode as it did in SC. The linear model is not appropriate, suggesting a second-order effect in one or both of the variables. The response increases with increasing levels of both variables with a maximum value at $N = +1$, $P = +1$, and extrapolation shows that the optimum lies at higher values of N and P out of the experimental domain assayed.

With the strain CBS 120–49, although the standardized residuals show a shallow curvature (Figure 3), it can be approximated by a linear model:

$$\text{CIT (g l}^{-1}\text{)} = 9.45 + 1.55 \text{ N} + 2.20 \text{ P} + 1.67 \text{ NP} \quad (1)$$

which also predicts improvement of the response toward high levels of both nutrients.

Similarly with strain 126–48, best results were obtained in the medium with high values of N and P. Here, lowering one or both N and P levels promotes a bigger decrease in the production than CBS 120–49.

Strain 246–65 improves toward high values of N and low values of P. The difficulty in reducing P levels of MPW make the increase in the concentration of N the most feasible way to adjust relative concentrations. As a result, this strain is less interesting.

With the strain 733–88, maximum production obtained in the center of the domain suggests that the location of the optimum would only require the experimental enlargement of the domain with four the points needed for a rotatable design; nevertheless, it does not seem foreseeable that the optimum surpasses substantially the results already obtained, and never the ones obtained with strains 554–65 and 120–49.

Extrapolation of the model obtained for strain CBS 120–49

Although the results of this strain are less interesting from the point of view of the total production reached, the empirical model obtained suggests the possibility of improving production simply by increasing initial levels of N and P. Considering experimental economy, the enlargement of the experimental domain was done applying the linear gradient approximation (LAG) method to Eq. (1) beginning from the center (in coded values, $N = 0$; $P = 0$), determining each new point by:

$$N_n = N_{(n-1)} + (\partial\text{CIT}/\partial N) \Delta N \text{ and}$$

$$P_n = P_{(n-1)} + (\partial\text{CIT}/\partial P) \Delta P$$

assigning equal increments in ΔN and ΔP of 1/40 of the domain (0.05 in coded values).

Although this method gives good predictions within the domain, an area in which N and P have not yet had a deleterious effect, it is foreseeable that by increasing gradually both nutrients, a maximum of citric acid will be reached and after it, production will drop.

The five points of the LAG assayed appear (defined by coded and natural values) in Table 3. Cultures were conducted in a 10M–H medium with the required supplements and under the same conditions and incubation times as in the previous culture.

In contrast to the theoretical extrapolation, the experimental results showed the limitation of improving the production in this way (Figure 4). After a slight increase (smaller than predicted) up to the point $N = 1,211$; $P = 142 \text{ mg l}^{-1}$, the production of the acid drops with an almost parabolic trajectory. N and P concentrations above $N = 1,552$ and $P = 195 \text{ mg l}^{-1}$ inhibit citric acid production completely. The increment in biomass production follows an asymptotic type curve and carbohydrate consumption declines from a maximum situated further on than the one for the production of citric acid.

The LAG method was thus useful for establishing the optimal range of interacting variables using a small number of experiments. Based on this, a rotatable second-order plan could be conducted to establish the precise optimal values, but in this case, no important further improvement can be expected which would justify the selection of this strain.

A rotatable design for strain CBS 554–65

In view of the inadequacy of a first-order model for describing the production response, this suggests second-order effects in at least one of the variables. The original domain was enlarged toward higher values of N and P with the necessary points needed for a second-order rotatable plan (Table 4) centered on the limit of higher production ($N + 1$, $P + 1$). The unitary increments for the natural values were the same as in the previous plan.

The results after 60 h of incubation allowed description of the effects of N and P on three parameters (citric acid, biomass production, and consumed glucose) by means of empirical second-order equations whose validity was tested with the same criteria as before (Table 5 and Figure 5). The response surfaces are shown in Figure 6.

1. Citric acid: Eq. (2) obtained for this response reflects the significant interaction between N and P as well as a large negative quadratic effect in both variables:

$$\text{CIT (g l}^{-1}\text{)} = 39.62 + 3.99\text{N} + 0.92\text{P} + 1.90\text{NP} - 4.26\text{N}^2 - 2.96\text{P}^2 \quad (2)$$

The calculated optimum corresponds to the point $\text{N} = 0.69$; $\text{P} = 0.48$ (equivalent to $\text{N} = 1,416$ and $\text{P} = 140 \text{ mg l}^{-1}$) with a predicted production of 40.73 g l^{-1} verified experimentally by obtaining a production of 40.01 g l^{-1} .

2. Biomass: Eq. (3) shows a clear effect due to N with P appearing only in the interaction term.

$$\text{B (g l}^{-1}\text{)} = 20.27 + 2.09\text{N} + 0.87\text{NP} - 1.10\text{N}^2 \quad (3)$$

In fact, raising the constraints of the Student's test to the level $\alpha = 0.01$, Eq. (4) is reduced to:

$$\text{B (g l}^{-1}\text{)} = 20.27 + 2.09\text{N} - 1.01\text{N}^2 \quad (4)$$

so that P disappears and yet passes both Fisher's tests at a level $\alpha < 0.05$.

With regard to Eq. (3) and (Figure 6), high levels of biomass require a high initial concentration of both nutrients, although the variable P shows a linear effect of different sign depending on the level of N—an interaction that demonstrates the need for balance between the nutrients.

3. Consumed glucose: Although this response is largely affected by N, it only takes place with low values of P:

$$\text{Gc(g l}^{-1}\text{)} = 80.45 + 10.43\text{N} - 3.37\text{P} - 1.84\text{NP} - 4.32\text{N}^2 \quad (5)$$

The effect of N can be related directly with biomass production, but it is more difficult to explain the negative effect of P.

Comparing the surfaces obtained for the different responses, it should be noted that the production of the acid does not depend directly on the total biomass production and that with glucose consumption up to medium levels of nutrients, it is not always correlated with production of biomass and/or citric acid.

Discussion

It has been shown that SSC develops at a higher rate, reaching maximum production in about 2–3 days; SC takes 8–10 days. The productivity of the different strains and their nutritional requirements also vary with the culturing mode. This work shows the utility

of factorial designs for establishing these requirements by allowing not only the selection of the most interesting strains but also the criteria for improved performance. It is evident that this type of procedure is well suited to locating the optimum production, particularly in the case of variables with important interactions as demonstrated in this work.

Comparing the results in SSC with the corresponding results in SC for same strains⁵ (Table 6) and referring to the tendencies of production as a function of the levels of N and P, it can be appreciated how the culturing modality conditions the behavior of the microorganism. For both culturing methods, the strains 554–65, 120–49, and 126–48 showed a similar behavior, but with improvement toward low levels of N and P in SC and toward high levels in SSC, and with superior productions and yields in the latter. In contrast, for strains 264–65 and 733–88, higher levels of N and P improved production in SC and decreased it in SSC.

This could be interpreted in accordance with Ramesh and Lonsane²⁴ and Shankaranand and Lonsane¹⁴ who recognized that the specificity of SSC is largely due to a lower diffusion rate of nutrients and metabolites that occurs in low-water activity conditions; thus, the strains with high requirements of N and P seem to be disfavored as a consequence of the restrictions of accessibility to the nutrients in the medium. These restrictions would also explain the bigger tolerance to a surplus of N and P detected in the strains in which the response decreases.

For strain 554–65, citric acid production in SSC can be compared with the equation obtained previously for the same domain and with the same unitary increments of N and P in SC, although of first order (6):

$$\text{CIT (g l}^{-1}\text{)} = 22.4 - 9.3\text{N} - 4.3\text{P} \quad (6)$$

It can be noted that, besides a change in the requirements, both nutrients have a lower effect in SSC with smaller values of the N and P coefficients compared with the independent term, so this system is less sensitive within the same range of variables.

This work demonstrates differences in behavior between the two culturing modes, although more work should be done to elucidate whether these differences are due to diffusional restrictions or other factors such as morphological and physiological

changes induced by the growth of the fungus on a support. From a more practical point of view, the results of this work indicate the advantages of SSC for bioproduction when based on residual substrates such as MPW, particularly in reducing the effect of varying composition.

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Figure 1 Citric acid production (CIT: shadowed bars) and consumed glucose (Gc: light bars) for 11 strains of *A. niger*. Upper: Solid-state culture on polyurethane foam under the conditions described in text at 96 h. Lower: Submerged culture with the same initial medium at 192 h

Figure 2 Experimental results with strains CBS 554–65, CBS 126–48, CBS 246–65, and CBS 733–88 after a solid-state incubation period of 72 h in the media defined in Table 1. N and P in coded values

Figure 3 Response surface generated from the empirical equation obtained for strain CBS 120–49 in solid-state culture, standardized residuals (in columns), and correlation between observed and expected values (E)

Figure 4 Extrapolation of the model obtained for strain CBS 120–49 in solid-state culture following the lineal approximation gradient. Citric acid (CIT): expected values (thick line) and experimental results (\blacklozenge), biomass (B, \diamond) and consumed glucose (Gc, \circ) as a function of the initial concentration of N (in coded values)

Figure 5 Standardized residuals and correlation between observed and expected values according to the models proposed for strain CBS 554–65 in solid-state culture for the responses: citric acid (CIT, g l^{-1}), biomass (B, g l^{-1}), and consumed glucose (Gc, g l^{-1})

Figure 6 Response surfaces obtained from the empirical models corresponding to citric acid (CIT), biomass B, and consumed glucose (Gc) with strain CBS 554–65 in solid-state culture as a function of the initial concentration of N and P (in coded values)

Table 1 Experimental domain and codification criteria of the independent variables

	Coded values	Natural values	
		N (mg l^{-1})	P (mg l^{-1})
	-1	710	60
	0	955	90
	1	1,200	120
Increments	1	245	30

Codification:

$$V_c = (V_n + V_o/dV_n)$$

Decodification:

$$V_n = V_o + (dV_n p V_c)$$

V_c : Coded value

V_n : Natural value

V_o : Natural value in the center of the domain

dV_n : Increment of V_n corresponding to one unit of V_c

Table 2 Results of the experimental plan and analysis of the significance of the proposed model for strain CBS 120–49 in solid-stat culture

N	P	Y	\hat{Y}	Coefficients	t	Model
1	1	14.56	14.87	9.45	39.73	9.45
1	-1	6.82	7.13	1.55	4.62	1.55 N
-1	1	8.12	8.43	2.20	6.55	2.20 P
-1	-1	7.05	7.36	1.67	4.96	1.67
						NP
0	0	9.73	9.45		Average response = 9.45	
0	0	9.91	9.45		Average central response = 9.76	
0	0	8.89	9.45		Var(Ee) = 0.453	
0	0	10.52	9.45		$t(\alpha < 0.05; v = 4) = 3.182$	
		SS	df	QM		
Model		40.167	3	13.389	QME/QMEe = 1.182	F^4_3 (a = 0.05) = 9.01
Error		2.139	4	0.535	QMLF/QMEe	F^1_3 (a

				= 1.726	=
					0.05)
					= 9.55
Exper. error	1.358	3	0.453	$r^2 = 0.949$	
Lack of fit	0.781	1	0.781	adjusted $r^2 =$	
Total	42.306	7	6.044	0.912	

\hat{Y} and \hat{Y} : Observed and expected values of citric acid (g l^{-1}), respectively; SS: sum of squares; df: degrees of freedom; QM: quadratic means. E: total error; Ee: experimental error; LF: lack of fit. Variables according to Table 1

Table 3 Coded and natural values of N and P for four ascending points within the trajectory defined by the linear approximation gradient method used in the extrapolation of the model obtained for the strain CBS 120–49 in solid-state culture

Coded Values		Natural Values (mg l^{-1})	
N	P	N	P
0	0	955	90
0.91	1.11	1,096	123
1.47	1.71	1,211	142
2.19	2.47	1,360	165
3.12	3.42	1,552	195

Table 4 Experimental domain and values of the variables used in the rotatable factorial plan with strain CBS 554–65

Coded values	Natural values	
	N (mg l^{-1})	P (mg l^{-1})
-1.41	903	73
-1	1,004	87
0	1,248	122
1	1,492	157
1.41	1,594	172

Increments	1	244	35
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Table 5 Results of the experimental plan and analysis of the significance of the proposed second-order models for the three responses with strain CBS 554–65 in solid-state culture

N	P	Citric acid (g l ⁻¹)		Biomass (g l ⁻¹)		Consumed glucose (g l ⁻¹)				
		Y	\hat{Y}	Y	\hat{Y}	Y	\hat{Y}			
1	1	37.53	39.21	22.72	22.21	81.09	81.35			
1	-1	33.15	33.57	20.41	20.48	92.90	91.76			
-1	1	126.54	27.44	16.17	16.30	64.75	64.16			
-1	-1	29.76	29.40	17.33	18.03	69.21	67.22			
1.41	0	37.95	36.74	20.79	21.20	86.58	86.56			
-1.41	0	25.57	25.46	15.79	15.29	55.87	57.05			
0	1.41	36.56	35.01	19.64	20.27	76.67	75.68			
0	-1.41	32.18	32.41	20.79	20.27	84.21	85.21			
0	0	39.63	39.62	20.56	20.27	80.99	80.45			
0	0	38.68	39.62	19.25	20.27	78.99	80.45			
0	0	39.47	39.62	20.56	20.27	79.79	80.45			
0	0	39.31	39.62	20.56	20.27	81.70	80.45			
0	0	41.04	39.62	20.41	20.27	81.10	80.45			
		Coeff	t	Model	Coeff	t	Model	Coeff	t	Model
		39.62	101.69	39.62	20.27	79.125	20.27	80.45	147.67	80.45
N		3.99	12.94	3.99	2.09	10.312	2.09	10.43	24.23	10.43
P		0.92	2.99	0.92	-0.06	0.295	NS	-3.37	7.82	-3.37
NP		1.90	4.36	1.90	0.87	3.025	0.87	-1.84	3.02	-1.84
N ²		-4.26	12.91	-4.26	-1.01	4.664	-1.01	-4.32	9.36	-4.32
P ²		-2.96	8.95	-2.96	-0.05	0.231	NS	0.29	0.62	S
		$\hat{Y} =$		$\hat{Y}_o =$	$\hat{Y} =$		$\hat{Y}_o =$	$\hat{Y} =$		$\hat{Y}_o =$
		35.2		39.6	19.6		20.3	78.0		80.5
		Var (Ee) = 0.759			Var (Ee) = 0.328			Var (Ee) = 1.484		
		t ($\alpha < 0.05$; v = 4) =			t ($\alpha < 0.05$; v = 4) =			t ($\alpha < 0.05$; v = 4) =		

	2.776			2.776			2.776		
	SS	df	QM	SS	df	QM	SS	df	QM
Model	315.55	5	63.110	45.16	3	15.054	4	1107.67	276.92
Error	10.91	7	1.559	3.17	9	0.353	8	14.95	1.87
Exper. error	3.04	4	0.759	1.31	4	0.328	4	5.94	1.48
Lack of fit	7.88	3	2.625	1.86	5	0.372	4	9.01	2.25
Total	326.46	12	27.205	48.21	12	4.018	12	1124.09	93.67
	QME/QMEe = 3.458			QME/QMEe = 1.134			QME/QMEe = 1.519		
	$F^3_4 (\alpha = 0.5) = 6.59$			$F^5_4 (\alpha = 0.05) = 6.26$			$F^4_4 (\alpha = 0.05) = 6.39$		
	QMLF/QMEe = 2.053			QMLF/QMEe = 1.075			QMLF/QMEe = 1.259		
	$F^7_4 (\alpha = 0.05) = 6.09$			$F^9_4 (\alpha = 0.05) = 6.00$			$F^8_4 (\alpha = 0.05) = 6.04$		
	$r^2 = 0.967$			$r^2 = 0.937$			$r^2 = 0.985$		
	adjusted $r^2 = 0.943$			adjusted $r^2 = 0.912$			adjusted $r^2 = 0.980$		

Y: Observed values; \hat{Y} : predicted values; NS: not significant coefficient; SS: sum of squares; df: degrees of freedom; QM: quadratic means. E: total error; Ee: experimental error; LF: lack of fit

Table 6 Comparison between the tendencies of N and P requirements in the five most productive strains in solid-state culture and those obtained in submerged culture (Pintado et al.)⁵

Strain	Submerged culture (192 h, 264 h)				Solid-state culture (72 h)			
	Tendency	Values at the maximum			Tendency	Values at the maximum		
		CIT (g l ⁻¹)	Gc (g l ⁻¹)	CIT/Gc (%)		CIT (g l ⁻¹)	Gc (g l ⁻¹)	CIT/Gc (%)
CBS								
554–69 ^a	N-1 P-1	35.09	107.37	32.68	N+1 P+1	46.56	83.18	55.98
120–49 ^b	N-1 P-1	4.46	99.92	4.46	N+1 P+1	14.56	89.21	16.32
126–48 ^b	N-1 P-1	6.70	92.06	7.28	N+1 P+1	13.60	97.11	14.00

246-	N+1 P+1	13.94	108.00	12.91	N+1 P-1	9.26	93.99	9.85
65 ^a								
733-	N+1 P+1	15.09	98.00	15.40	N0 P0	12.69	91.24	13.90
88								
