Native defects in hybrid C/BN nanostructures by density functional theory calculations

J. M. Pruneda*

Centre d'Investigació en Nanociència i Nanotecnologia (CSIC-ICN), Campus de la UAB, E-08193 Bellaterra, Spain

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First-principles calculations of substitutional defects and vacancies are performed for zigzag-edged hybrid C/BN nanosheets and nanotubes which recently have been proposed to exhibit half-metallic properties. The formation energies show that defects form preferentially at the interfaces between graphene and BN domains rather than in the middle of these domains, and that substitutional defects dominate over vacancies. Chemical control can be used to favor localization of defects at C-B interfaces (nitrogen-rich environment) or C-N interfaces (nitrogen-poor environment). Although large defect concentrations have been considered here (10^6 cm^{-1}), half-metallic properties can subsist when defects are localized at the C-B interface and for negatively charged defects localized at the C-N interface; hence the promising magnetic properties theoretically predicted for these zigzag-edged nanointerfaces might not be destroyed by point defects if these are conveniently engineered during synthesis.

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I. INTRODUCTION

Hybrid C and BN nanostructures have been studied since the first attempts to dope carbon nanotubes with boron or nitrogen.¹ Nanotubes (NTs) with C, B, and N were theoretically predicted² and experimentally synthesized in the mid-1990s,^{1,3–5} but the recent advent of graphene has revitalized the field. Hybrid C and BN nanosheets are becoming accessible,^{6,7} offering a new route to enhance graphene's promise, enabling the fine-tuning of the electronic and optical properties (for example, modulation of the electronic band gap, chemical reactivity, etc.).

Following the advances in experimental growth of hybrid C-BN nanostructures,^{7–9} the stability of domain-separated C and BN nanosheets and nanotubes has been studied by first-principles simulations in the last few years.^{10–14} There is general agreement that segregation is energetically advantageous, because B-N and C-C bonds are more stable than C-N and C-B bonds and the former are favored by the formation of C and BN domains. Furthermore, according to molecular dynamics simulations, hybrid C-BN armchair nanotubes can be spontaneously formed via the connection of zigzag-edged BN and graphene nanoribbons (BNNRs and GNRs) at room temperature,¹¹ and their stability can be competitive with that of the corresponding pristine BN and C nanotubes (BNNTs and CNTs).¹⁴ These zigzag-edged heterostructures are particularly appealing for spintronic applications, as the polarity of the BNNR gives an interfacial dipole and hence an effective electric field acting on the graphene ribbon.¹⁵ It has been predicted that half metallicity can be induced in zigzag GNRs by application of a sufficiently large in-plane electric field perpendicular to the edges of the ribbon.¹⁶

Magnetism in zigzag-edged graphene-based nanostructures is related to the presence of electronic states that are mainly localized at the edges.¹⁷ These states seem to be ubiquitous in hexagonal structures with zigzag borders¹⁸ and are not present in armchair edges. Roughness and defects have been shown to strongly affect the electronic properties of zigzag GNRs, inducing a continuous decrease of the magnetic moments with increasing concentration of defects until the system becomes nonmagnetic for concentrations of one defect per

$\sim 10 \text{ Å}$, which might be a typical concentration for real samples.¹⁹ Nevertheless half metallicity induced by external electric fields seems to survive at similar defect concentrations with the same critical field strength.¹⁶ At zigzag interfaces between C and BN domains, however, defects can change the electronic screening of the edge polarity, hence affecting the effective electric potential on graphene's ribbon and destroying its intrinsic half metallicity. It is then important to address the role played by point defects at the boundary between graphene and BN domains. In this work, first-principles simulations are performed to determine the formation energies and electronic properties of intrinsic point defects (vacancies and substitutional defects) at zigzag interfaces between C and BN nanodomains that could exhibit magnetism. It is shown that these defects are energetically favored when localized close to domain interfaces, and their electronic properties are determined by the presence of a defect-induced electronic state localized at the C-N interface which could be occupied or empty depending on the donor or acceptor nature of the defect.

The paper is organized as follows. After describing the technicalities in Sec. II, we present and discuss the findings in Sec. III. Results of the energetics of neutral defects at the interfaces are examined and compared to similar defects placed at a graphenelike or BN-like monodomain. Magnetism at the interfaces and other electronic properties are then analyzed and the effect of defect concentration and charge state discussed. Finally, Sec. IV summarizes the conclusions.

II. METHODOLOGY

Ab initio pseudopotential density functional calculations are performed for both planar [two-dimensional (2D)] superlattices¹⁵ and (n,n) armchair nanotubes ($5 \leq n \leq 14$) with zigzag-edged C-BN domains along the tube axis following the geometries discussed in the literature.^{11,12,14,20} Troullier-Martin-type pseudopotentials²¹ and numerical atomic orbitals with double- ζ -plus polarization are used to describe the electronic valence states within the spin-polarized generalized-gradient approximation²² as implemented in the FIESTA code.²³ The atomic positions

FIG. 1. (Color online) Band structures for hybrid C-BN nanotubes with different armchair chiralities and zigzag edges between C and BN domains along the tube axis. Different relative compositions of $C_x(BN)_{1-x}$ are picked to ensure half metallicity. The absence (presence) of a band gap for up (down) spin polarizations is revealed in the solid (red) or dashed (blue) lines.

are determined with a structural relaxation until the forces are smaller than $0.02 \text{ eV}/\text{\AA}$. An accurate description of the boundary electronic states requires a smooth sampling of the reciprocal space, and typically Monkhorst-Pack grids of at least $1 \times 1 \times 100$ are used to sample the Brillouin zone.

It has been claimed that half metallicity in C-BN nanotubes can be achieved within a certain ratio of carbon content (30%–50%) and is not dependent on the diameter of the tube.²⁰ This allegation can be misleading. Although half-metallic ground states can be obtained for different chiralities (see Fig. 1), this happens only for C concentrations under a critical value, which does depend on the tube diameter. Analogously to the case of planar C-BN heterostructures, the critical parameter is the relative width of the C and BN strips.¹⁵ To address the stability of magnetism to the presence of defects, systems that have half-metallic properties in their pristine (defect-free) structure are considered. In particular, throughout this work we take (i) a nanotube with chirality (5,5) and 50% C concentration (corresponding to five C and five BN zigzag chains), and (ii) a planar (5,7) C-BN superlattice (composed of five C and seven BN zigzag chains). Native point defects are introduced near the edges of the C and BN domains in a supercell geometry, with at least $30 \text{ \AA}$ empty space between periodic images. Different concentrations can be modeled by changing the size of the supercell along the periodic axis. If not otherwise stated, supercells made of eight repetitions of the unit cell along the tube axis are considered (a total of 160 atoms).

The formation energy of a defect in charge state q is defined in terms of the chemical potentials of the species involved in

the defect and the Fermi level μ_e measured relative to the top of the valence band E_v :

$$E_f(X) = E_{\text{tot}}(X) - \sum_i n_i \mu_i + q(\mu_e + E_v), \quad (1)$$

where E_{tot} is the energy of the defective supercell containing n_i atoms of species i (C, B, and N) with chemical potential μ_i , at $T = 0$ (entropic contributions are neglected). These chemical potentials are specified by a reference system that acts as the reservoir of atoms. Typically, reference values used in the literature are taken from graphene, molecular nitrogen, and bulk boron. These, however, will give formation energies only in the limits of high concentrations of C, N, or B. Formally, one can use the formation energies of these reference systems as thermodynamic limits to the chemical potentials, which must satisfy the following conditions:

(1) stability of the C-BN complex:

$$\mu_C + \mu_B + \mu_N = \Delta E_f(\text{CBN}); \quad (2)$$

(2) the values that cause precipitation into its constituents,

$$\mu_C \leq 0, \quad \mu_B \leq 0, \quad \mu_N \leq 0;$$

(3) the values that cause formation of each domain,

$$\begin{aligned} \mu_B + \mu_N &\leq \Delta E_f(\text{BN}), \\ \mu_C &\leq \Delta E_f(\text{C}), \end{aligned}$$

where ΔE_f denotes the generalized formation free energy of the corresponding system relative to a pure C or BN nanotube. Relation (2) can be used to write one of the atomic chemical potentials in terms of the other two. Considering that C doping in BNNTs has proved elusive,²⁴ whereas BNNTs can be synthesized by substitutional reaction from CNTs,²⁵ in the following the chemical potential of C will be set to the value that corresponds to a clean CNT, meaning that the defect formation energies will be given in the C-rich limit. Equation (2) is then used to express μ_B in terms of μ_N , which will be used as a free parameter, with values ranging between precipitation into molecular nitrogen (N rich, or condition 2 above) and the poorest nitrogen atmosphere that, nevertheless, allows for h -BN growth (condition 3).

III. RESULTS AND DISCUSSION

Substitutional carbons on the boron and nitrogen sublattices (C_B and C_N), boron or nitrogen atoms in carbon sites (B_C and N_C), and vacancies of each species (V_C , V_B , and V_N) were considered, as shown in Fig. 2. Ghost orbitals are used to improve the localized atomic orbital description at the (unreconstructed) vacancy sites.²⁶ The labels N and B will be used to denote the edge at which the defect is placed, where N designates the interface with C-N bonds, whereas B is the edge with C-B bonds. Accordingly defects are classified into set N (C_N , B_C , V_N^N , V_B^N , or V_C^N), and set B (C_B , N_C , V_N^B , V_B^B , or V_C^B).

The formation energies for the interfacial (neutral) defects in a (5,5) C-BN nanotube are shown in Fig. 2 and compared to the energetics of the same defects in a pristine pure CNT and pure BNNT of the same chirality. The energies of pure C and BN nanotubes are in agreement with values

FIG. 2. (a) Atomic positions considered for the different defects. Circles, filled squares, and empty squares denote C, B, and N atoms. Periodic boundary conditions require that both C-N and C-B edges are included in the simulation box. The arrow indicates the axis of the nanoribbons or the direction of the tube axis. Formation energies (in eV) for the studied neutral defects as a function of nitrogen chemical potential (μ_N) are shown in the lower panel for (b) the pure CNT, (c) hybrid C-BN nanotubes (solid lines) with eight repetitions of the unit cell and 2D nanosheets (dashed lines) with seven repetitions of the unit cell, and (d) BN nanotubes with (5,5) chirality.

published in the literature,^{27–29} considering that the formation energy depends on the chirality and increases with tube's diameter.^{27,30} The cost of removing atoms (vacancy formation) is generally larger than the energy of atom substitution (disorder), which is indicative of the high stability of the honeycomb structure. First-principles calculations have shown that vacancy formation is energetically more favorable near the edge of zigzag BNNRs than in the center of the ribbon.³¹ A similar effect is observed now, with defects at the edge being at least 1 eV less energetic. Interestingly, recent experiments have shown that carbon substitution (doping) in BN nanostructures is favored at the edges.⁹

Note that C_N and B_C (defects of set N) are energetically favorable in a nitrogen-poor environment (B rich), and the same is true for N_C and C_B (set B) in a N-rich situation, so that the localization of defects at each edge of the heterojunction could be chemically controlled. Furthermore, when neutral C_N and B_C defects are formed, one hole is added to the system, so that these defects can act as electron traps. On the other hand, N_C and C_B add one extra electron to the system and could possibly become positively charged under appropriate conditions (low electron chemical potential μ_e). In pure BN

FIG. 3. Density of states (DOS) around the Fermi level (at 0 eV) for defects localized at the C-N (top) and C-B (bottom) interfaces. Dark shaded regions correspond to the projected DOS (PDOS) on C orbitals localized at the N interface. Gray regions for V_C^N and V_B^N are the PDOSs on C or N orbitals close to the C or B vacancy, respectively.

nanosheets and nanotubes, V_B is also an acceptor that can trap charges to form V_B^- , whereas V_N has two one-electron states in the gap, one occupied and the other empty, enabling the formation of either V_N^+ or V_N^- , depending on the value of μ_e .

Figure 3 shows the electronic density of states (DOS) for set N (top) and set B defects. Let us first discuss the latter type of defect (set B). Notice that, even for the high defect concentration considered in these simulations ($5 \times 10^6 \text{ cm}^{-1}$), the system remains half metallic, with a sharp peak in the DOS at the Fermi level. This peak corresponds to a defect-induced electronic state that is localized at the N edge rather than at the defect itself (placed at the B edge). Hence, electrons coming from these donor defects are transferred through the C domain to the region with lower electronic potential, as described in Ref. 15. This can be seen from the DOS projected on the carbon orbitals localized at the C-N interface (shaded regions in the figure). This localized band has some dispersion along the edge axis (there is slightly more contribution to the PDOS from C atoms directly opposite to the defect site), and a larger unit cell would be needed to address its localization length. The exchange splitting for this band is ~ 0.3 eV for all the set B defects, and the calculations give a total magnetic moment of $\sim 1\mu_B$ for C_B , N_B , and V_N^B , $2\mu_B$ for V_C^B , and $\sim 3\mu_B$ for V_B^B . Notice, however, that the supercell approach used here might not be appropriate to describe the long-range magnetic interactions between these defect-induced localized magnetic moments.³²

On the other hand, the missing electron (extra hole) for set N defects has a dramatic effect on the corresponding DOS, which does not show half-metallic properties. There is a similar defect-induced electronic state localized at the C-N interface for C_N , B_C , and V_N^N , but now it is unoccupied (~ 0.1 eV above the Fermi level) and not spin polarized (C_N and B_C have total magnetic moments of $\sim 0.5\mu_B$). V_C^N and V_B^N are slightly different, with an empty C-N interfacial state at ~ 0.4 eV above the Fermi level and a rather localized electronic state on the atoms surrounding the vacancy site (shaded light regions in the figure), which is spin polarized (total magnetizations of $\sim 1.8\mu_B$ and $1\mu_B$, respectively. The

FIG. 4. Density of states for substitutional defects as a function of defect concentration for planar C/BN superlattices (similar results are obtained for nanotube geometries). From left to right, supercells with three, four, and seven units of repetition along the interfacial axis, corresponding to concentrations of 13×10^6 , 10×10^6 , and $6 \times 10^6 \text{ cm}^{-1}$. Dark and light shaded regions correspond to projected DOS over C orbitals at the N/B interface.

lowering of the Fermi level means a partial depopulation of the π_B state¹⁵ and a weakening of the magnetic instability induced by electron-electron interactions.¹⁷ The reduction of the electronic occupation of the π_B state lowers the electronic potential at the *B* edge and significant decrease of the *induced* electric field in the graphene ribbon, so that half metallicity cannot survive.¹⁵

Let us focus in the following on those defects that have the lower formation energies, i.e., substitutionals. The effect of increasing the defect concentration even further is shown in Fig. 4, where the DOSs of different supercells of planar bidimensional superlattices are shown. Small differences arise between this planar geometry and the previous tubular case, mainly because of the different C:BN ratio, but the general results are equivalent. For *p*-type set *N* defects (B_C and C_N), the reduced number of electrons shifts the Fermi level toward lower values as we move toward higher defect concentrations (smaller supercells, from right to left), depopulating the initially fully occupied majority spin band, localized at the C-B interface (light shaded region), until the full spin polarization at the Fermi level is destroyed. On the other hand, for *n*-type set *B* defects (N_C and C_B), the extra electrons added to the system shift the Fermi level to higher values as we move toward higher concentrations, increasing the occupation of the C-N electronic

FIG. 5. Density of states for charged ($q = -1, 0, +1$) substitutionals. From top to bottom, B_C , C_N (set *N*), C_B , and N_C (set *B*). Dark (light) shaded regions correspond to the PDOSs on C orbitals localized at the *N* interface (*B* interface).

states, and eventually destroying half metallicity. Notice again that defects localized at the C-B interface add extra electrons that are transferred to the C-N interface, while defects localized at the C-N interface, which are electron deficient, tend to remove charge from the C-B interface.

For the limit of low concentration of defects, the semimetallic graphene domain could be considered as the electron reservoir so that μ_e is fixed by the position of the GNR's Fermi level, and hence only neutral defect calculations were considered up to now. However the donor or acceptor character of the defects became relevant when discussing their electronic properties, revealing the need to address charged defects. When charge states for defects in semiconductors and insulators are addressed, the value of μ_e in Eq. (1) ranges between zero (the top of the valence band) and the energy band gap, and a careful alignment of the reference energy has to be considered to compare energetics of neutral and charged defects. Here, however, the system is semimetallic regardless of the charge state, so that the position of the Fermi level can be used to align the energetics, and $\mu_e = 0$ can be used to compare formation energies.

As shown in Fig. 5, when an extra electron is added to the system ($q = -1$), it localizes at the *N*-edge state (dark peaks) close to the Fermi level, recovering half metallicity for the set *N* defects (the states become fully occupied for set *B* defects which remain half metallic). The formation energies for these charged defects are reduced by $\sim 2.3 \text{ eV}$ (at $\mu_e = 0 \text{ eV}$).

There is a decrease in the system's total magnetization for set N ($\sim 0.1\mu_B$) and an increase to $2\mu_B$ for set B . On the other hand, removal of an electron (giving defects with charge state $q = +1$) has negative effects on the electronic properties of substitutionals: the lowering of the Fermi level depopulates the N -edge state for set B defects (although the total DOS remains half metallic), and destroys magnetization for all defects (set N remains metallic). In this case, the formation energies are increased by ~ 3.6 eV, clearly destabilizing these positively charged defects.

Following the above results, a N-rich environment together with a high μ_e (providing electrons to the system) would increase the possibilities for subsistence of half metallicity in these hybrid C-BN structures. B -edge localized defects are favored by an N-rich atmosphere, and even at large defect concentrations (10^6 cm^{-1}) conducting electrons remain fully spin polarized. On the other hand, under these chemical conditions, there will be a lower concentration of defects localized at the N edge (higher formation energies), which although they hinder half metallicity when neutral do not in their negative charge state. It is interesting that similar conditions have been suggested to be best for manufacturing hybrid compounds through electron-beam-induced doping of BN nanostructures with C.³³

IV. CONCLUSIONS

First-principles density functional theory calculations have shown that intrinsic defects in hybrid C-BN nanostructures are more stable at the boundaries between C and BN domains. Both bidimensional superlattices of alternating graphene and BN nanoribbons and armchair nanotubes with axial domains of C and BN that have zigzag edges have been analyzed, giving similar results. In these systems, the electronic band structure close to the Fermi level is determined by characteristic zigzag-edge states localized at the boundary of the hexagonal lattice, as already discussed in the literature.

The stability of the honeycomb structure results in a higher formation energy for vacancies (V_C , V_B , or V_N) than for substitutionals. While a nitrogen-poor environment favors the formation of defects at C-N interfaces (mainly C_N and B_C), nitrogen-rich atmospheres favor defects localized at the C-B boundary (C_B and N_C), which can be classified as electron acceptors and donors, respectively. Extra electrons provided by the latter are transferred to a defect-induced partially occupied electronic state localized at the opposite edge (C-N) and the system remains half metallic, even for the large defect concentrations considered here. If extra electrons are added to the system, they are transferred to this electronic state, and the defects are further stabilized (in their negatively charged state), whereas electron deficiency drains the electronic level and increases the defect formation energy. On the other hand, substitutional defects localized at the C-N interface add one hole to the system, hence lowering the Fermi level and weakening the magnetic instability (through depopulation of the π_{C-B} orbital), resulting in the cancellation of half metallicity. The defect-induced electronic state localized at the C-N interface is still there, but unoccupied. Extra electrons added to the system will populate this level, recovering half metallicity and lowering the defect formation by a few eV.

Finally, the analysis of the magnetic properties reveals that half metallicity (i) could survive defect concentrations at the interfacial line of up to 10^7 cm^{-1} , and (ii) could be tuned through appropriate electronic doping that avoids an excessive charge depletion from the C-B interface for high concentrations of p -type substitutionals or excessive charge increase at the C-N interface for n -type substitutionals. Experimental investigation of magnetism in these hybrid nanostructures is encouraged.

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*miguel.pruneda@cin2.es

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