Revisiting the paper "Using radiometric surface temperature for surface energy flux estimation in Mediterranean drylands from a two-source perspective"

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1 Abstract:

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3 The recent paper by Morillas et al. [Morillas, L. et al. Using radiometric surface temperature for

4 surface energy flux estimation in Mediterranean drylands from a two-source perspective, Remote

5 Sens. Environ. 136, 234-246, 2013] evaluates the two-source model (TSM) of Norman et al.

6 (1995) with revisions by Kustas and Norman (1999) over a semiarid tussock grassland site in

- 7 southeastern Spain. The TSM in its current incarnation, the two-source energy balance model
- 8 (TSEB) was applied to this landscape using ground-based infrared radiometer sensors to
- 9 estimate both the composite surface radiometric temperature and component soil and canopy
- 10 temperatures. Morillas et al. (2013) found the TSEB model substantially underestimated the
- 11 sensible *H* (and overestimated the latent heat *LE*) fluxes. Using the same data set from Morillas
- 12 et al. (2013), we were able to confirm their results. We also found energy transport and
- 13 exchange behavior derived from primarily the observations themselves to differ significantly

14 from a number of prior studies using land surface temperature for estimating heat fluxes with 15 one-source modeling approaches in semi-arid landscapes. However, revisions to key vegetation inputs to TSEB and the soil resistance formulation resulted in a significant reduction in the bias 16 and root mean square error (RMSE) between model output of H and LE and the measurements 17 compared to the prior results from Morillas et al (2013). These included more representative 18 ground-based vegetation greenness and local leaf area index values as well as modifications to 19 20 the coefficients of the soil resistance formulation to account for the very rough (rocky) soil 21 surface conditions with a clumped canopy. This indicates that both limitations in remote estimates of biophysical indicators of the canopy at the site and the lack of adjustment in soil 22 23 resistance formulation to account for site specific characteristics, contributed to the earlier findings of Morillas et al. (2013). This suggests further studies need to be conducted to reduce 24 the uncertainties in the vegetation and land surface temperature input data in order to more 25 26 accurately assess the effects of the transport exchange processes of this Mediterranean landscape on TSEB formulations. 27

28 Introduction

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Reporting errors in the modeled latent heat flux (LE) of approximately 90% mostly due to 30 31 a significant underestimate of the sensible heat flux (H) (70 Wm⁻²), the recent study by Morillas 32 et al. (2013) suggests that the two-source energy balance (TSEB) model, which has been successfully applied to a wide variety of landscapes and climates (Kustas and Anderson, 2009), 33 could not produce reliable estimates of LE in a semiarid Mediterranean tussock grassland site in 34 southeast Spain (Balsa Blanca). The Balsa Blanca site is representative of arid regions which 35 cover ~25 % of the Earth's land surface (Fensholt et al., 2012) and are characterized by having 36 37 low LE fluxes resulting in H being the dominant turbulent flux during most of the year (Ryu et 38 al. 2008). To better understand the factors adversely affecting the utility of the TSEB model in this very heterogeneous semiarid environment, where the average daytime LE was about 115 W 39 m⁻², an analysis of the local flux-gradient relationship was conducted using a combination of the 40 measurements from the eddy covariance flux tower and the observed surface-air temperature 41 42 differences. In addition, based on other observations from the Balsa Blanca site suggesting 43 modification of TSEB resistance and canopy transpiration formulations from the standard, the TSEB results are re-analyzed. Reaffirming an earlier study by Villagarcia et al. (2007) that 44 45 suggested that this landscape has some unique aerodynamic characteristics, the results of the analysis presented here indicate that the flux-gradient behavior observed at the Balsa Blanca site 46 is quite different from what has been observed in prior studies over semiarid areas using surface-47 air temperature differences to estimate surface fluxes (e.g., Stewart et al., 1994; Troufleau et al., 48 1997; Verhoef et al., 1997). However, using local observations of vegetation cover conditions in 49 combination with revisions to some of the TSEB formulations, the unique flux-exchange 50

characteristics suggested by the observations can be accommodated by the model and the bias in
the *H* and *LE* greatly reduced.

In this investigation, the measurements from the Balsa Blanca flux tower are used to 53 compute the effective resistances to the transport of sensible heat, following the single-source 54 approach with radiometric surface temperature as the boundary condition (Stewart et al. 1994). 55 By examining values of the ratio of roughness lengths for momentum (z_{om}) and heat (z_{oh}) 56 57 exchange with the single-source approach, which is indicative of the relative efficiency of momentum versus heat transport, we found that the ratio of roughness lengths at this site departs 58 significantly from that at many other semi-arid sites analyzed by Stewart et al. (1994) among 59 60 others. This difference in momentum versus heat transport in many past studies is quantified in terms of the variable kB^{-1} [= ln(z_{om}/z_{oh})], which is discussed below, and its magnitude for the 61 Balsa Blanca is found to be similar to values derived theoretically and from observations for 62 63 fully vegetated surfaces (Brutsaert, 1982; Massman, 1999). Consequently, any current thermally-based single-source technique using the measurements from Morillas et al. (2013) 64 would likely produce large errors in H and LE without a priori calibration of kB^{-1} . 65 It is important for the reader to understand that kB^{-1} originally accounted for the higher 66

efficiency of momentum versus heat transport from soil and vegetated surfaces, which comes from the fact that very close to the surface elements heat transfer occurs by diffusion while momentum transfer occurs by both viscous and pressure forces (Thom, 1972). With the use of radiometric surface temperature in single-source approaches there is added complexity in defining a kB^{-1} to account not only for key factors affecting aerodynamic transport of heat versus momentum but also surface properties (notably fractional vegetation cover) and sensor viewing angle affecting radiometric surface temperature observations (see discussion below).

74 We also find with TSEB that using ground-based local estimates of leaf area index (LAI) and local green vegetation fraction (f_G) , as opposed to using MODIS-derived estimates of local 75 LAI and f_G as in the Morillas study, there is a significant reduction in bias between TSEB model 76 and measured fluxes. In addition, adjustments to the empirical coefficients in the TSEB soil 77 resistance formulation based on visual inspection of the site indicating a rocky rough soil surface 78 further improved agreement between measured and modeled fluxes. This result indicates that 79 80 modifications to model inputs as well as some of the algorithms for modeling the turbulent 81 exchange are required in order to markedly improve model-measurement agreement at this semiarid flux site. 82

83 Methodology

As shown in Fig. 1a, single-source or bulk transfer schemes for modeling sensible heat 84 flux (H) often employ an additional resistance term (R_H) because heat transport is less efficient 85 than momentum transport from land surface (see e.g., Garratt and Hicks, 1973). However, in 86 87 applications of remotely sensed land surface temperature, an additional radiative resistance term is added (represented by R_R) so that the total excess resistance (R_{EX}) is defined, namely $R_{EX} = R_H$ 88 + R_R and accounts for the numerous factors that cause differences between the remotely-sensed 89 surface temperature and the aerodynamic surface temperature, most notably sensor view angle 90 91 and vegetation cover effects. The aerodynamic surface temperature is defined in Fig. 1 as either 92 T_{AEROH} or T_{AEROM} , which is physically coupled to the sensible heat exchange and associated 93 aerodynamic resistance R_{AERO} . If it is assumed there is no difference in the efficiency in heat and momentum transport ($z_{oh} = z_{om}$ or $kB^{-1}=0$) then T_{AEROM} is associated with R_{AERO} while assuming 94 additional resistance to heat exchange results in computing T_{AEROH} from R_{AH} (= R_{AERO} + R_H), 95 requiring $z_{oh} < z_{om}$ or $kB^{-1} > 0$ (Kustas et al., 2007). 96

97 Due to the difficulty in parameterizing R_{EX} robustly and parsimoniously in the application of the one-source scheme for different landscapes, climates, and observational configurations, 98 the two-source modeling approach was developed. Because it considers vegetation and soil 99 layers separately (Fig. 1b), this approach can accommodate the major factors that influence 100 differences between radiometric or remotely-sensed surface temperature and the aerodynamic 101 surface temperature which is explicitly defined in the two-source formulation (Kustas, 1990; 102 103 Norman et al., 1995). The different roles of soil and vegetation in the convective and radiometric 104 processes can be represented in a simplified form by a two-source model, such as TSEB, without requiring any additional input information beyond that needed by single-source models using 105 more sophisticated kB⁻¹ parameterizations (Norman et al., 1995; Kustas and Norman, 1999). 106

107 *Single-source formulation:*

108 According to Merlin and Chebhouni, (2004) one-source model formulations can provide reliable fluxes, if the excess resistance term, R_{EX} is calibrated for a given site. The problem is 109 that applying the R_{EX} formulation to another landscape often leads to poor results, indicating a 110 lack of generality to the relationships (e.g., Verhoef et al., 1997). On the other hand, there have 111 been several formulations derived from applying more complex soil-vegetation-atmosphere-112 transfer (SVAT) models for estimating R_{EX} or kB^{-1} based on vegetation cover conditions and 113 114 radiometer viewing angle (Boulet et al., 2012; Lhomme et al., 2000; Matsushima, 2005) yielding satisfactory results using a single-source approach. Such attempts to relate R_{EX} to vegetation and 115 surface properties are shown to mainly affect the value of R_R (Kustas et al., 2007). However, 116 regardless of whether or not R_{EX} values appropriate for a particular landscape can be estimated 117 118 from SVAT-derived formulations, computing R_{EX} from the remotely sensed surface temperature

and heat flux measurements does provide a metric quantifying the efficiency of heat exchange
from the observations, themselves. In the context of the one-source model, *H* can be expressed
as:

122
$$H = \rho C_p \frac{T_{COMP} - T_A}{R_{AERO} + R_{EX}}$$
(1)

where ρC_p is the volumetric heat capacity of air, T_{COMP} is the "composite radiometric (remotelysensed) land surface temperature", T_A is the air temperature in the surface layer, and R_{AERO} is the aerodynamic resistance (Verma, 1989). Given measurements of T_{COMP} and T_A , H and estimates of R_{AERO} , which can have several forms as described by Verma (1989; see also e.g., Stewart et. al., 1994; Verhoef et al., 1997), the value of the excess resistance term, R_{EX} , can be computed via Eq. (1). Two commonly used forms for estimating R_{AERO} , which differ in the stability correction functions applied to the logarithmic expressions, are:

130
$$R_A = \frac{\left[ln\left(\frac{(z-d)}{z_{om}}\right) - \psi_m\right]\left[ln\left(\frac{(z-d)}{z_{om}}\right) - \psi_h\right]}{uk^2}$$
(2a)

131
$$R_{AM} = \frac{\left[ln\left(\frac{(z-d)}{z_{om}}\right) - \psi_m\right] \left[ln\left(\frac{(z-d)}{z_{om}}\right) - \psi_m\right]}{uk^2}$$
(2b)

where z is the measurement height of mean wind speed, u, and air temperature, T_A , d is the displacement height, z_{om} is the aerodynamic roughness length (momentum roughness length), k is von Karman's constant (k = 0.4), ψ_m is the surface layer stability correction function for wind, and ψ_h is the stability correction function for temperature. Since the friction velocity (u_*) is defined as $u_* = uk\{ln[(z - d)/z_{om}] - \psi_m\}^{-1}$, R_{AM} can be computed directly from the measurements of u and u* collected via a three-dimensional sonic anemometer according to 138 $R_{AM} = u/u*^2$. To calculate R_A , the roughness parameters were estimated from canopy height (h_c) 139 using well-established empirical relationships, namely $z_{om} = 0.13h_c$ and $d=0.6h_c$ (Brutsaert, 140 1982), and the stability correction functions proposed by Brutsaert (1992).

141 As discussed by Stewart et al. (1994), among others, a single resistance (R_{AH}) formulation 142 that relates to the aerodynamic surface temperature T_{AEROH} to the heat flux-temperature gradient 143 relationship (see Fig. 1a) has often historically been defined as follows:

144
$$R_{AH} = \frac{ln\left(\frac{(z-d)}{z_{om}}\right) - \psi_h}{u_* k} + \frac{ln\left(\frac{z_{om}}{z_{oh}}\right)}{u_* k}$$
(3)

145 which then gives the following one-source formulation for sensible heat flux exchange:

146
$$H = \rho C_p \frac{T_{AEROH} - T_A}{R_{AH}}$$
(4)

where R_{AERO} is represented in Eq. (3) by the first RHS term and R_H is represented by the second 147 148 RHS term $(R_{AH=} R_{AERO+} R_H)$. The R_H term is often expressed as the inverse of the Stanton number, B^{-1} , which is defined as $B^{-1} = k^{-1} \ln(z_{om}/z_{oh})$ (Owen and Thompson, 1963), normalized by 149 *u*^{*}. Further, the product, kB^{-1} [= ln(*z*_{on}/*z*_{oh})], characterizes the difference in the efficiency of heat 150 and momentum transport. As mentioned above, others do not make a distinction between the 151 roughness length for heat and momentum and only relate the sensible heat exchange to the 152 aerodynamic resistance R_{AERO} , so that in Eq. (4) T_{AEROM} defines the aerodynamic surface 153 temperature (see Fig. 1). However this often results in even greater discrepancies between 154 aerodynamic surface temperature computed via Eq. (4) and radiometric (remotely-sensed) 155 surface temperature (Kustas et al., 2007). 156

157 *Two-source formulation:*

158	Within the TSEB scheme, there is flexibility to evaluate alternative formulations for the
159	resistances from soil (R_S) and canopy (R_X) and sensitivities to uncertainties in resistance
160	coefficients (McNaughton and van den Hurk, 1995; Choudhury and Monteith, 1988; Kustas and
161	Norman, 1999; Cammalleri et al., 2010) as well as different methods to parameterize the canopy
162	transpiration in order to obtain a solution based on the partitioning of radiometric temperature
163	and energy balance between soil and canopy elements (e.g., Colaizzi et al., 2014). Using the
164	standard TSEB parameterizations for R_S and R_X , we have the following

165
$$R_{S} = \frac{1}{c(T_{SOIL} - T_{CANOPY})^{1/3} + bu_{S}}$$
(5)

166

167 and

168
$$R_X = \frac{C'}{LAI} \sqrt{\left(\frac{l_W}{u_{d+z_{OM}}}\right)}$$
(6)

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In the formulation for R_s , u_s is wind speed near soil surface (~0.05 m), T_{SOIL} and T_{CANOPY} are radiometric temperatures and default values are c = 0.0024 (m s⁻¹ K^{-1/3}) and b = 0.012 for moderately rough soil surfaces (Kustas and Norman 1999). However, values up to $c \sim 0.0038$ m s⁻¹ K^{-1/3} and b ranging from 0.034 to 0.087 are proposed in the literature (Kondo and Ishida 1997; Sauer et al. 1995) for rough soil and partially vegetated surfaces. This is the case in the Balsa Blanca, where there is considerable rock content on the soil surface and strongly clumped 176 vegetation. For R_X , l_W is the leaf size/width, and u_{d+zom} the wind speed at the level of effective 177 momentum absorption by the canopy. A value for $C'=130 \text{ s}^{1/2} \text{ m}^{-1}$ was suggested by 178 McNaughton and van den Hurk (1995), in comparison with the 90 s^{1/2} m⁻¹ adopted by Norman et 179 al. (1995). In the original version of the TSEB, an initial solution for the canopy transpiration 180 component, *LE_C*, is obtained using the Priestley-Taylor formulation,

181
$$LE_{C} = \propto_{PTC} f_{G} \frac{\Delta}{\Delta + \gamma} R_{NC}$$
(7)

where $\alpha_{PTC} \sim 1.3$, Δ is the slope of the temperature-saturation vapor pressure curve, γ is the psychrometric constant, R_{NC} is the canopy net radiation, and f_G is the green vegetation fraction. Recent ground-based observations from the Balsa Blanca site indicate f_G was significantly lower than what was derived from the MODIS data and used in the Morillas study.

186 **Results with One-Source Model: Evaluating** kB^{-1} Parameter

In most studies evaluating one-source modeling approaches, no distinction is made between R_{EX} and R_H and the value of kB^{-1} is parameterized so that T_{COMP} and T_{AEROH} agree. Studies by Stewart et al. (1994), Verhoef et al. (1997), and Troufleau et al. (1997) evaluated kB^{-1} using Eq. (1) with R_{EX} approximated as $kB^{-1}/(u_* k)$ (based on $R_{EX} \approx R_H$ assumption) for several semiarid and arid sites. Since R_{AERO} computed using R_A and R_{AM} yielded similar results for the Balsa Blanca field site, the former was used in Eq. (1) to estimate kB^{-1} at this site for consistency with these previous studies.

194 Compared to the values of kB^{-1} from these earlier studies, the data from Balsa Blanca site 195 yield values that are atypically low (Table 1). The values of kB^{-1} at the Balsa Blanca site, which 196 averaged near 2, are more typical of those observed when the heat exchange occurs primarily 197 with permeable vegetative roughness elements (Brutsaert, 1982, Fig. 4.24) that make up fullyvegetated surfaces (Garratt and Hicks, 1973). Based on both field observations (e.g., Kustas, 198 1990; Stewart et al., 1994) and modeling studies using a two-source model based on Lagrangian 199 theory (McNaughton and van den Hurk; 1995), the value of kB^{-1} can be as much as a factor of 200 ten larger when the soil surface also contributes significantly to heat exchange. The increase in 201 the value of kB^{-1} is due to the lower relative efficiency of heat exchange from the soil compared 202 to the exchange from the canopy elements that results from the greatly diminished winds near the 203 soil surface. Stated differently, larger kB^{-1} values reflect a reduction in the overall coupling 204 between the surface and the atmosphere, a behavior which is typically observed in semi-arid 205 sparsely vegetated landscapes. However, with a $kB^{-1} \sim 2$ this does not appear to be the case for 206 the Balsa Blanca site. Apart from the fractional cover and structural characteristics of the 207 vegetation, kB^{-1} values are also strongly affected by plant stress levels and micrometeorological 208 conditions causing kB^{-1} to change by a factor of 10 during the course of a day at the same site 209 (Lhomme et al., 1997). The uniqueness of this dataset is further demonstrated in Figure 2, 210 showing a histogram of kB^{-1} values derived from the Balsa Blanca data along with the mean and 211 standard deviations of the kB^{-1} values for all the sites listed in Table 1. A Z-test at the 95% 212 confidence level indicates the mean kB^{-1} value from Balsa Blanca data does not come from the 213 population of samples that generated the mean kB^{-1} values from the other sites in Table 1. In 214 other words, the mean $kB^{-1}=2.2$ falls outside the likely range of mean values observed at the 215 other semi-arid and arid sites. 216

The data set can also be visualized in terms of the implied ratio of the roughness lengths for heat and momentum, z_{oh}/z_{om} . As can be seen in Figure 3, this ratio from the Balsa Blanca site is an order of magnitude larger than the ratio observed for nearly all of the other sites. This suggests the relative efficiency of heat exchange is much greater than has been typically
observed for sparsely-vegetated arid sites, if the radiometric temperature observations are indeed
representative of the entire site composite surface.

223 The "aerodynamic surface temperature", T_{AEROH} , can be computed by inverting Eq. (4) 224 and using an *a priori* formulation for R_H (i.e., $R_H = kB^{-1}/u_* k$) according to:

225
$$T_{AEROH} = T_A + \frac{HR_{AH}}{\rho C_p}$$
(8)

Using the observed values of H, T_A and u_* along with estimates of R_{AERO} using Eq. (2a), and 226 assuming kB^{-1} has a value of either 2, indicative of vegetated surfaces (Brutsaert, 1982), or 7, an 227 228 average from the semi-arid sites analyzed in Stewart et al. (1994), T_{AEROH} was calculated via Eq. (8). As one would expect with kB^{-1} equaling ~2, the derived T_{AEROH} is approximately equal to 229 T_{COMP} since for the Balsa Blanca site the average value of kB^{-1} equals 2.2, with T_{AEROH} values 230 falling slightly above and below the 1:1 line (Fig. 4a). However, when kB^{-1} is set equal to 7, 231 T_{AEROH} is significantly greater than T_{COMP} (Fig. 4b). This would suggest an unusual case where 232 233 the effective emitting surface temperature is *hotter* than the observed surface temperature during 234 the daytime hours.

At the Balsa Blanca site, having perennial grasses, the vegetation fractional cover remains fairly constant, $f_C \sim 0.6$ (Morillas et al., 2013), hence midday soil - canopy temperature

differences (T_{SOIL} - T_{CANOPY}), by assuming $T_{COMP} = [f_c T_{CANOPY}^4 + (1 - f_c) T_{SOIL}^4]^{\frac{1}{4}}$, ranged from 238 2 °C to 12 °C over the growing season. This range in temperature difference between T_{SOIL} and 239 T_{CANOPY} is relatively small compared to soil - canopy temperature differences typically observed 240 in semi-arid environments, often exceeding 20 °C (e.g., Chebhouni et al., 2001; Humes et al., 1994; Kustas et al., 2004). This is likely due in large part to the fact that plant green-up coincides with the wet season in many semi-arid environments whereas in Mediterranean ecosystems, the rainy period tends to be over the winter months while green-up of the vegetation happens during the dry season. This leads to the vegetation generally having higher stress conditions resulting in relatively higher values of T_{CANOPY} (Were et al., 2007; Verhoef et al., 1996).

Applying Lhomme et al. (2000) expression for estimating B^{-1} with LAI adjusted for clumped 247 248 vegetation yields a kB^{-1} value of ~3.7 which results in a z_{oh}/z_{om} ratio of ~1/40 whereas kB^{-1} from the observations yields a z_{oh}/z_{om} ratio of ~1/9. This again points to other measurement factors 249 250 and/or landscape features at Balsa Blanca that is affecting the efficiency of heat transport from its surface. In a recent single-source model application using remotely sensed surface 251 temperature, modification to the soil resistance or the kB^{-1} expression for bare soil heat transfer 252 253 was required to improve heat flux predictions in the semi-arid Tibetan Plateau region (Chen et al., 2013). Indeed, the single-source expression for heat transfer over bare soil surfaces derived 254 theoretically by Brutsaert (1975) shows a strong dependency of kB^{-1} on roughness Reynolds 255 number, and has been validated using remotely sensed surface temperature and sensible heat flux 256 observations (Cahill et al., 1997; Yang et. al., 2008). 257

258 Results from TSEB --Before and After Modifications of Inputs: LAI and f_G and R_S

- 259 Morillas et al. (2013) used the effective values of LAI from MODIS LAI/fAPAR
- 260 (fAPAR: fraction of absorbed photosynthetically active radiation) estimates (average between
- the Terra MOD15A and Aqua MYD15A products), with a $f_C = 0.6$ from site measurements. The

value of f_G was estimated based on the empirical approach of Fischer et al (2008), with fAPAR defined as well from MODIS LAI/fAPAR data.

Using recent observations made in the Balsa Blanca study site from a different year but 264 similar weather conditions, estimates of local green LAI were derived from monthly NDVI data 265 measured using a multi-spectral camera and field LAI sampling at the study site. The one-sided 266 leaf area index (LAI) was estimated for Stipa tenacissima from reflectance measurements with a 267 268 Tetracam ADC camera (Tetracam, Inc., Gainesville, FL, USA¹). This camera records images 269 with 2048×1536 pixels using an 8 mm lens and 8 mm focal length. The pictures were taken at a height of 2 m to cover all the surface of the plants in one or two images. The plant canopy 270 271 reflectance was divided in red, green and NIR band of wavelengths by the optical filters of the camera. The images were processed with the specific software delivered with the camera 272 273 (PixelWrench II) that allows adjust the factory calibration to the spectral balance of the ambient 274 light selecting in the picture a training area (a White Teflon Calibration Plate located near each plant, also provided with the camera) and calculate NDVI or other vegetation indices. After this 275 correction, the pictures with the NDVI index were exported to the ESRI ArcMap software in 276 277 TIFF format to select only the pixels that represented the plant canopy, thereby eliminating the noise caused by the surrounding soil. In our study, LAI values were calculated from an NDVI-278 LAI relationship obtained by correlating NDVI values from the Tetracam ADC camera with LAI 279 280 values from destructive sampling.

Assuming total (green+dead) LAI is a constant value of ~1.75 over the growing season (study period), which appears reasonable based on visual observations of the site (Fig. 5c), we derived new values of f_G (Fig. 6) based on Tetracam ADC camera derived green LAI (Fig. 6b).

¹ The mention of trade names of commercial products in this article is solely for the purpose of providing specific information and does not imply recommendation or endorsement by the US Department of Agriculture.

284 Here, f_G was allowed to vary from 0, if the green LAI reached 0, up to 0.7 when green LAI reached its maximum value, considering that there are always dead/senescent material in the 285 tussock grass over all seasons (Fig. 5b and 5c). The results of changing the LAI and f_G inputs in 286 TSEB from those used originally in the TSEB model run by Morillas et al. (2013) are illustrated 287 in Figure 7. There is a considerable reduction in the bias and RMSE for H and LE estimates 288 using the new LAI and f_G inputs in TSEB, which highlights the limitations of using MODIS 289 290 derived values of LAI and f_G at this site and the need of ground-based biophysical measurements at the same spatial resolution as the radiometric surface temperature measurements for evaluating 291 TSEB model performance under such conditions. 292

293 Modifications to the empirical parameters c and b used to estimate soil resistance, R_s , were also made to better capture a more efficient heat exchange due to the rough soil surface and 294 greater intensity in the turbulence based on the significant rock content of the soil surface and 295 clumpiness of the vegetation (see Fig. 5). The values used in Eq.5 were c = 0.0038 (Kondo and 296 297 Ishida, 1997) and *b*=0.065 (average of the range in value reported by Sauer et al., 1995 for small 298 and developing canopies). This modification in R_s resulted in a further significant reduction in H and LE bias, with TSEB estimates much closer to the 1:1 line, and considerably lower RMSE for 299 both fluxes (Fig. 7e and f). However for LE it resulted in a lower R² as a result of an increase in 300 scatter in H estimates. Using a larger resistance to heat exchange from the canopy with C'=130301 302 instead of 90 in Eq. (6) as proposed by McNaughton and van den Hurk (1995) had little effect on TSEB output of H and LE (results not shown). The implication of these results is that while the 303 bulk heat transport expressed in terms of the kB^{-1} parameter at the Balsa Blanca differs 304 significantly from earlier findings over most other semi-arid and arid surfaces using one-source 305 modeling approaches, the TSEB indicates that there are physical factors related to soil and 306

307 vegetation properties that largely contribute to this result. By using local observations of LAI 308 and f_G as inputs to TSEB and changing the soil resistance coefficients to be more representative 309 of the surface characteristics, the TSEB model achieves good agreement with *H* and *LE* 310 measurements.

311 Conclusions

While there can be limitations in applying TSEB in complex heterogeneous water-limited 312 313 environments having natural vegetation without modifications to the canopy transpiration formulations (Agam et al., 2010; Guzinski et al., 2013; Chirouze et al., 2014), caution needs to 314 be exercised interpreting and using measurements made over such surfaces. In the case of the 315 316 Morillas et al. (2013) paper, the relationship of the radiometric surface temperature-air temperature differences and heat flux exchange differ significantly from other semiarid areas 317 with partial vegetation cover as defined by the kB^{-1} variable used in single-source modeling 318 approaches. 319

For example, applying a mean value of kB⁻¹ =7, typical for semi-arid sparsely vegetated surfaces derived by Stewart et al (1994), Stewart (1995) showed significant improvement in heat flux estimation using T_{COMP} for a sparsely vegetated grassland site with LAI ~0.5 and fractional vegetation cover ~75% in the in the Konza Prairie, Kansas, USA. However, the Konza Prairie site is not strongly clumped as the Mediterranean tussock grassland in the Balsa Blanca nor has as dry a climate.

Obviously, this same value for kB^{-1} would not be appropriate for the Balsa Blanca and is indicative of the fact that while one-source modeling approaches using radiometric surface temperature can provide a diagnostic tool for evaluating the efficiency of heat exchange, they are not reliable in general for heat flux estimation without *a priori* calibration, particularly for heterogeneous sites. However, their utility for heat flux estimation has improved through the development of kB^{-1} formulations that account for fractional vegetation cover or LAI (Su et al., 2001; Lhomme et al., 2000; Boulet et al., 2012) and variation in kB^{-1} for bare soil heat transport (e.g., Chen et al., 2013).

The current findings require flux-gradient parameterization that is not typically observed 334 in any other previously studied semi-arid and arid sites, and with modifications to the TSEB soil 335 resistance parameters for a very rough soil surface and more efficient heat exchange as well as 336 337 modifications to the LAI and estimate of $f_{\rm G}$ based on ground observations, the significant 338 underestimate of H and overestimate of LE is greatly reduced. These revisions to both soil resistance parameterizations and input data emphasize the need for detailed local measurements 339 to better understand model limitations and/or refinements necessary for different land cover 340 341 types.

While regional to global scale application of TSEB land surface scheme using a modeling 342 system based on coarse resolution satellite data called the Atmosphere Land Exchange Inverse 343 (ALEXI) model, which also has a Disaggregation scheme (DisALEXI) when using higher 344 345 resolution imagery (Anderson et al., 2011) is currently producing continental scale flux fields, 346 studies like the current one suggest this model is not applicable with a single set of resistance 347 parameterizations for all landscapes. On the other hand, results of such local studies can be entered into a land use data base at satellite resolutions to refine model parameterizations for 348 certain regions found to be especially challenging. 349

350	This study also cautions on the use of local observations (radiometric surface
351	temperature) with non-local or larger scale estimates of other key inputs which are not
352	necessarily representative of local conditions (i.e., leaf area index, green fraction). Clearly,
353	additional measurements and analyses for this landscape are needed to confirm that these
354	modifications to TSEB resistances are warranted, which in addition should include more ground-
355	based infrared radiometer measurements as well as simultaneous local observations of LAI and
356	$f_{\rm G}$. At the same time, application with satellite data for all model inputs should also be
357	performed to evaluate the limitations of remote sensing algorithms used in defining key model
358	inputs (e.g., Guzinski et al., 2013).
359	Finally other two-source resistance formulations from Choudbury and Monteith (1988)
000	many, only the source resistance formulations from choudhary and montenin (1900)

and McNaughton and van den Hurk (1995) should be evaluated to see if there is a consistency in
results using different two-source resistance formulations, which may help better understand the
observations and findings of Morillas et al. (2013).

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514 515	List of Figure Captions
515 516 517 518 519 520 521 522 523 524 525 526 527	Figure 1. Schematic diagram of one-source and two-source thermal-based models of sensible heat flux. See text for definition of the symbols used in the one-source model formulations. For the two-source model (TSEB), T_{SOIL} is the soil surface temperature with associated soil surface aerodynamic resistance (R_S) and heat flux from the soil (H_S) and T_{CANOPY} is the vegetation canopy temperature with associated aerodynamic canopy resistance (R_X) and heat flux from the canopy (H_C). T_{SOIL} and T_{CANOPY} are derived from T_{COMP} and an estimate of fraction vegetation cover with an initial assumption of canopy transpiration and T_{AC} is the temperature in the canopy air space which is related to the surface aerodynamic temperature via the surface layer aerodynamic resistance (R_{AERO}) For details of the TSEB formulations see Norman et al. (1995). Figure 2. Histogram (grey bars) of kB^{-1} values computed for the Balsa Blanca site using $R_{AERO} = R_A$. Also plotted are the mean (filled circles) and standard deviation (horizontal bars) of the kB^{-1}
528 529 530 531 532	values listed in Table 1 staggered in the vertical with the Balsa Blanca identified with the solid star symbol. Figure 3. The ratio of z_{oh}/z_{om} by inverting the kB^{-1} expression, namely, $z_{oh}/z_{om}=\exp(-kB^{-1})$ for all the kB^{-1} values listed in Table 1.

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535

- 536 Figure 4. The composite radiometric temperature measured by the thermal infrared radiometer,
- 537 T_{COMP} versus the surface aerodynamic temperature T_{AEROH} computed from Eq. (5) using
- 538 measurements of *H*, and *u** and estimates of R_{AH} from Eq. (3) with a) $kB^{-1} = 2.2$ derived for the
- Balsa Blanca site (see Table 1) and b) $kB^{-1} = 7$, an average value from the semi-arid sites
- analyzed by Stewart et al. (1987). Line is 1:1 relationship with T_{COMP} .
- 541

Figure 5. Photos of a) typical rock cover in non-canopy covered soil surface at the Balsa Blanca
site and b) photo illustrating the strongly clumped nature of the semiarid Mediterranean
tussock grassland in southeast Spain during green-up and c) at senescence in late September.

- 545
- 546 Figure 6. Estimated Leaf area index (LAI) and fraction of green LAI (Green LAI) versus Day of
- 547 Year (DOY) a) from Morillas et al. (2013) using MODIS LAI/fAPAR and a green vegetation
- fraction, f_G , derived from Fisher et al. (2008); and b) produced using monthly NDVI data from
- 549 multi-spectral camera and destructive sampling performed at the site between 2009 and 2010.
- 550
- Figure 7. Sensitivity in the output from TSEB for a) H and b) LE using original LAI and f_G
- inputs from Morillas et al (2013) and with the standard soil resistance formulation coefficients c
- and b (c=0.0024, b=0.012), with c) H and d) LE computed using modifications to LAI
- 554 (LAI~1.75) and green LAI ($f_G *$ LAI) inputs (see Figs. 5 and 6) based on ground observations
- and with the standard soil resistance formulation coefficients c and b, and with e) H and f) LE
- computed using modfied LAI and green LAI inputs along with assuming a rough soil surface
- 557 with clumped vegetation which resulted in revising the values of the soil resistance coefficients c
- 558 and b (c=0.0038, b=0.0605). See text for more details.

Table 1. Average (avg) and standard deviation (σ) of the kB^{-1} variable based on Eq. (1) and $R_{EX} \sim B^{-1}/u_*$ using the Balsa Blanca site from Morillas et al (2013) and study sites from Stewart et al. (1994), Troufleu et al. (1997) and Verhoef et al. (1997) having vegetation cover (not bare soil). Where available measurements or indirect estimates (*) from the literature of leaf area index (LAI), canopy height (h_C), fractional canopy cover (f_C) are provided from the literature as well as number of data point (n) in the statistics. The symbol NO indicates the authors found no observations or estimates provided.

Project	Surface	LAI	h _C	f _C	n	KB ⁻¹	KB ⁻¹
	type	(-)	(m)	(-)		avg	σ
Balsa Blanca	Tussock grass	1.75	0.7	0.6	4803	2.2	1.7
SEBEX	Fallow Savannah	0.2→0.7 (grass)	0.6 (grass)	0.3*	507	5.8	2.9
		0.1→0.6 (shrub)	2.5 (shrub)	0.2*			
SEBEX	Open forest	1.3*	4.5	0.3	1142	8.3	3.3
MONSOON 90	Grassland	0.8	0.1	0.35	95	3.8	2.8
MONSOON 90	Shrubland	0.5	0.5	0.26	98	5.6	2.8
Owens Valley	Shrubland	0.48	1	0.25	22	8.0	3.8
Smith Creek	Shrubland	1*	0.75	0.25	69	12.4	5.9
Valley							
Smoke Creek	Shrubland	NO	0.5*	0.30	79	8.4	4.9
Desert							
La Crau	Stone/grass	NO	0.1*	0.05	40	4.5	2.1
EFEDA	Vineyard	0.4	1	0.10	246	8.1	2.8
HAPEX-Sahel	Savannah	NO (shrub)	$2\rightarrow 2.5 \text{ (shrub)}$	0.2 (shrub)	285	12.4	4.6
		NO (grass)	0.5< (grass)	NO (grass)			
HAPEX-Sahel	Fallow Savannah	0.5 (shrub)	3.5 (shrub)	0.2* (shrub)	1229	8.8	5.6
		NO (grass)	0.2→0.6 (grass)	NO (grass)			
HAPEX-Sahel	Millet 1992	0.41→2.81	0.76→2.53	0.19→0.56	1011	4	4.4
HAPEX-Sahel	Millet 1991	1.9→2.8	0.72→2.2	0.20→0.30	648	6.7	5.1



a) One-source model

b) Two-source model













