

The South Atlantic Circulation Between 34.5°S, 24°S and Above the Mid-Atlantic Ridge From an Inverse Box Model



Key Points:

- The upper layers present the course of the anticyclonic South Atlantic subtropical gyre and the northeast route of the Benguela Current
- The deep layers present the southward flowing boundary currents and an eastward interbasin flow close to 24°S above the Mid-Atlantic Ridge
- The heat transport flows northward across the subtropical South Atlantic Ocean, where evaporation dominates over precipitation

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Abstract The South Atlantic Ocean plays a key role in the heat exchange of the climate system, as it hosts the returning flow of the Atlantic Meridional Overturning Circulation (AMOC). To gain insights on this role, using data from three hydrographic cruises conducted in the South Atlantic Subtropical gyre at 34.5°S, 24°S, and 10°W, we identify water masses and compute absolute geostrophic circulation using inverse modeling. In the upper layers, the currents describe the South Atlantic anticyclonic gyre with the northwest flowing Benguela Current (26.3 ± 2.0 Sv at 34.5°S, and 21.2 ± 1.8 Sv at 24°S) flowing above the Mid-Atlantic Ridge (MAR) between 22.4°S and 28.4°S (-19.2 ± 1.4 Sv), and the southward flowing Brazil Current (-16.5 ± 1.3 Sv at 34.5°S, and -7.3 ± 0.9 Sv at 24°S); the deep layers feature the southward transports of Deep Western Boundary Current (-13.9 ± 3.0 Sv at 34.5°S, and -8.7 ± 3.8 Sv at 24°S) and Deep Eastern Boundary Current (-15.1 ± 3.5 Sv at 34.5°S, and -16.3 ± 4.7 Sv at 24°S), with the interbasin west-to-east flow close to 24°S (7.5 ± 4.4 Sv); the abyssal waters present northward mass transports through the Argentina Basin (5.6 ± 1.1 Sv at 34.5°S, and 5.8 ± 1.5 Sv at 24°S) and Cape Basin (8.6 ± 3.5 Sv at 34.5°S– 3.0 ± 0.8 Sv at 24°S) before returning southward (-2.2 ± 0.7 Sv at 24°S to -7.9 ± 3.6 Sv at 34.5°S), without any interbasin exchange across the MAR. In addition, we compute the upper AMOC strength (14.8 ± 1.0 and 17.5 ± 0.9 Sv), the equatorward heat transport (0.30 ± 0.05 and 0.80 ± 0.05 PW), and the freshwater flux (0.18 ± 0.02 and -0.07 ± 0.02 Sv) at 34.5°S and 24°S, respectively.

Plain Language Summary The location of the South Atlantic subtropical gyre plays a critical role in the Atlantic Meridional Overturning Circulation, which controls the Earth's climate system. We have examined the South Atlantic subtropical gyre's circulation between 34.5°S and 24°S and above the Mid-Atlantic Ridge using data from three hydrographic cruises (34.5°S, 24°S, and 10°W). From these cruises, we have identified the water masses present on this region and computed their transport. Thus, we describe the path of the anticyclonic gyre and the northeast route of the Benguela Current in the upper water masses (<1,440 m depth); the southward flowing western and eastern boundary currents and an eastward interbasin flow close to 24°S above the Mid-Atlantic Ridge in the deep water masses (those on the depth range from 1,440 to 3,800 m depth); and the northward flow of the abyssal water masses (>3,800 m depth). We have also reported the characteristic heat transport flowing northward across the subtropical South Atlantic Ocean, where evaporation dominates over precipitation.

1. Introduction

The Earth's climate system is regulated by both ocean and atmosphere, which on average transfer heat from the equator to the subpolar regions. The South Atlantic Ocean plays an important and distinctive role in this heat exchange, as it hosts the returning flow of the Atlantic Meridional Overturning Circulation (AMOC), with its warm upper-ocean currents transporting heat northward from the subtropics to the tropics, hence compensating the southward flow of the cold and dense North Atlantic Deep Water (NADW) (Ganachaud & Wunsch, 2000; Garzoli et al., 2013; Talley, 2003). The Atlantic Ocean is different from all ocean basins because of the resulting net northward heat transport at all latitudes (Kelly et al., 2014), and it plays a major role in modulating

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European (e.g., Moffa-Sánchez & Hall, 2017; Palter, 2015) and global (e.g., Buckley & Marshall, 2016; Lynch-Stieglitz, 2017) climates.

The AMOC's upper limb is predominantly supplied by waters entering the South Atlantic via the Drake Passage and the Malvinas Current, the so-called “cold water route,” or via the Agulhas Current and the Agulhas leakage, the “warm water route” (Gordon, 1986; Speich et al., 2001). Off the west coast of southern Africa is found the Benguela Current is found in the upper and intermediate layers, which forms the eastern boundary current of the anticyclonic South Atlantic subtropical gyre. The Benguela Current is supplied by both the South Atlantic Current, flowing along the southern margin of the South Atlantic subtropical gyre (≈ 5 Sv), and by South Indian Ocean waters via the Agulhas Current (≈ 10 Sv) in the upper $\sim 1,500$ m of the South Atlantic Ocean (Gordon et al., 1992; Guo et al., 2023; Peterson & Stramma, 1991).

The Deep Western Boundary Current (DWBC) carries deep water from the Labrador Sea and the North Atlantic's Overflow Water layers to the southern latitudes (Talley & McCartney, 1982). The DWBC is the primary southward pathway for the cold and lower limb of the AMOC and has been extensively studied in the North Atlantic Ocean (e.g., Meinen & Garzoli, 2014; Toole et al., 2011). The deep pathways of the AMOC in the South Atlantic Ocean, however, are not as well documented (Garzoli et al., 2015). Arhan et al. (2003) confirmed two eastward pathways of NADW near the equator. Arhan et al. (2003) and Reid (1989) suggested similar circulation patterns in the South Atlantic at 2,500 m depth, indicating that most of the NADW enters the eastern basin between 20°S and 25°S, and then turns southeastward and flows above the Walvis Ridge through passages south of 28°S, entering the Cape Basin.

The zonal transports at the Mid-Atlantic Ridge (MAR) are crucial for connecting the eastern and western South Atlantic basins. There is one single realization of a meridional hydrographic section in the South Atlantic Ocean close to the MAR, which was done along 9°W (A14), from 4.3°N to 45.5°S during January and February 1995, as part of the World Ocean Circulation Experiment (WOCE) (Arhan et al., 2003; Mercier et al., 2003). To monitor flows across the MAR, the South Atlantic GAteway (SAGA) Array was deployed at the MAR at 10°W, between 34°S and 19°S at about 4,000 m depth. The array configuration consists of four pressure-equipped inverted echo sounders (PIES) separated by about 5° of latitude, with deep instrumented moorings located in between.

Our main goal in this study is to use these hydrographic measurements along 10°W along with an inverse model in order to describe the circulation above the MAR between 34.5°S and 24°S in the South Atlantic (Figure 1). To achieve this objective, we must determine the mass transport of the Brazil Current flowing southward and the northwestward flow of the Benguela Current, in both the thermocline and intermediate layers; the deep ocean currents that carry cold waters from the North Atlantic toward the southern latitudes in the western and eastern basins; as well as the northward flow of the abyssal layers. A significant result of the present study is that we will be able to determine the upper AMOC strength, including the heat and freshwater transports, at both latitudes.

The structure of this paper is outlined as follows. The hydrographic and Ocean General Circulation Model (OGCM) data are described in Section 2. Section 3 presents the vertical sections of different ocean properties to describe

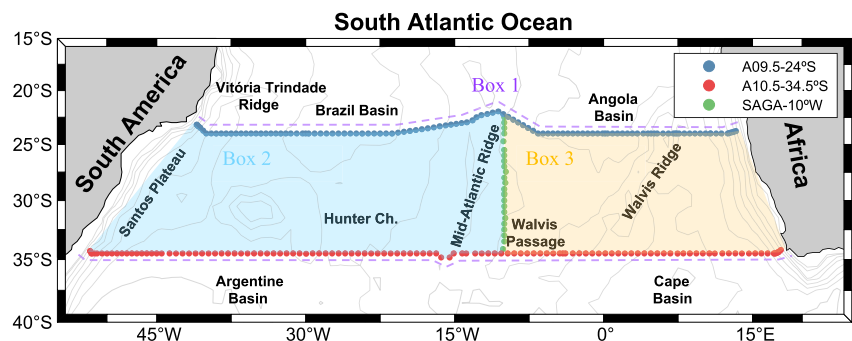


Figure 1. Positions of the hydrographic stations for the three South Atlantic cruises carried out at nominally 24°S, 34.5°S, and 10°W. The different boxes used in this study are identified as Box 1 (purple dashed lines), Box 2 (light blue), and Box 3 (light orange).

the water masses along 34.5°S, 24°S, and 10°W in the South Atlantic Ocean. The initial geostrophic transports and the inverse model characteristics are presented in Section 4. This is followed by the final adjusted transports and the resulting AMOC estimate in Section 5. The resulting horizontal circulation for the upper, deep and bottom layers are described in Section 6, the heat and freshwater transports obtained for both latitudes are provided in Section 7, and a scheme of the upper, deep and bottom pathways is shown in Section 8. Finally, Section 9 provides a discussion and concluding remarks on this work.

2. Hydrographic and Ocean General Circulation Model (OGCM) Data

For our study we use three hydrographic cruises carried out in the South Atlantic Ocean: 34.5°S in 2017, 24°S in 2018, and 10°W in 2021 (Figure 1). The hydrographic data at 34.5°S were collected during the expedition of the German Research Vessel *Maria S. Merian* conducted in summer 2017 (MSM60); the hydrographic data at 24°S were collected in fall 2018 on the RRS *James Cook* (JC159) as part of the Ocean Regulation of Climate by Heat and Carbon Sequestration and Transports (ORCHESTRA) project and the international Global Ocean Ship-Based Hydrographic Investigations Program (GO-SHIP) (Talley et al., 2016); and the hydrographic data at 10°W were collected in fall 2021 as part of the SAGA project onboard the R/V *Sarmiento de Gamboa*. The distance between stations was generally ≈ 50 km, with narrower spacing over boundary currents and steep topographic slopes. At each station, we use vertical profiles of potential temperature and salinity every two dbars as obtained from the conductivity-temperature-depth (CTD) probes. For the three hydrographic cruises, a shipboard acoustic Doppler current profiler (SADCP, of 38 kHz for MSM60 and the SAGA cruise, and 75 kHz for JC159) was employed at each station pair to provide a velocity profile from the sea surface down to depths between 800 and 1,500 m. Also, for the 34.5°S and 10°W cruises, a velocity profile from the sea surface to the seafloor at each station was obtained from a paired (at 34.5°S, 300 kHz upward-looking and 150 kHz downward-looking) or single (at 10°W, 150 kHz downward-looking) lowered acoustic Doppler current profiler (LADCP). As in Hernández-Guerra and Talley (2016) and Hernández-Guerra et al. (2019), the ADCP data will prove to be useful in the inverse model to constrain the boundary currents.

Our hydrographic data are complemented by simulations from two different numerical ocean models. ECCOV4r4 (Estimating the Circulation and Climate of the Ocean Version 4 Release 4; ECCO, hereafter) is a data-assimilating model developed by the Jet Propulsion Laboratory. It incorporates oceanographic observations, such as altimetry-derived sea surface height, hydrography from Argo profilers, ocean bottom pressure from the Gravity Recovery and Climate Experiment (GRACE) and hydrographic and current data from moorings, among others (Fukumori et al., 2020). The adjoint method is applied to repeatedly minimize the squared sum of weighted model-data misfits and control adjustments, improving the fit of the numerical data to the observations (Wang et al., 2020). ECCO provides the state of the ocean's evolution over time on a monthly data basis, with 50 standard levels and a nominal $1/2^\circ$ (≈ 48 km in our region) horizontal resolution configuration of the Massachusetts Institute of Technology general circulation model over the entire world, covering 26 years from 1992 to 2017 (ECCO Consortium et al., 2020, 2021; Forget et al., 2015).

The GLORYS12V1 (Global Ocean Physics Reanalysis; GLORYS, hereafter), an ocean model developed by Mercator and distributed by the European Copernicus Marine Environment Monitoring Service (CMEMS), is an eddy-resolving global ocean reanalysis that describes ocean circulation and includes sea-level forcing from satellite altimetry measurements covering the period of 1993–2019. GLORYS is developed using the current real-time global forecasting CMEMS system and the Nucleus for European Modeling of the Ocean (NEMO) model-based hydrodynamics. The CORA4 database and the ERA-Interim data are used for assimilating in situ observations and atmospheric forcing, respectively. Additionally, in situ temperature and salinity vertical profiles, altimeter data (sea level anomaly), sea ice concentration and satellite sea surface temperature are assimilated together. This numerical model provides monthly gridded data sets at $1/12^\circ$ (≈ 8 km in our region) horizontal resolution and 50 vertical levels (Drévillon et al., 2018).

To summarize, the ocean models used (ECCO and GLORYS) are data-assimilating models varying from coarse to eddy-permitting horizontal resolution ($1/2^\circ$ and $1/12^\circ$, respectively). After applying the inverse model, mass transports from hydrographic data are compared with monthly data for the whole water column in the South Atlantic Ocean, along 24°S and 34.5°S for 2017–2019 (GLORYS) and 2017 (ECCO). No data from these models are yet available for 2021, the year of the 10°W expedition.

3. Vertical Sections and Water Masses

The existing water masses are identified using the zonal (34.5°S and 24°S) and meridional (10°W) vertical sections of potential temperature, salinity, and oxygen for the three hydrographic cruises following Katsumata and Fukasawa (2011) and Talley et al. (2011) (Figure 2). The meridional section at 10°W, just east of and roughly parallel to the MAR, divides the transatlantic sections into western and eastern basins.

In the upper layers, the South Atlantic Central Water (SACW) is found between the sea surface and the neutral density $\gamma^n = 27.23 \text{ kg/m}^3$ (above $\approx 730 \text{ m}$ depth), with relatively high potential temperature ($>5^\circ\text{C}$; Figures 2a–2c), relatively high salinity (>34.7 ; Figures 2d–2f), and high dissolved oxygen of about 210–235 $\mu\text{mol/kg}$ (Figures 2g and 2h). This water mass is formed by the subduction of fluid via Ekman pumping out of the mixed layer in the Subtropical Convergence region (Gordon, 1981, 1989; Sprintall & Tomczak, 1993). The SACW is conveyed to the eastern basin by the South Atlantic Current and northward through the Benguela Current (Stramma & England, 1999), with a high contribution from the Indian Ocean through the Agulhas Current (warm water route) (Gordon, 1985; Poole & Tomczak, 1999; Sprintall & Tomczak, 1993), including the large and slow contribution of Agulhas rings transporting warm and salty waters into the Atlantic (Casanova-Masjoan et al., 2017).

The upper thermocline layers ($\gamma^n < 27.23 \text{ kg/m}^3$) of the transoceanic vertical sections present titled isotherms and isopycnals that allow us to identify the signals of the Brazil and Benguela Currents in the western and eastern margins, respectively (Figures 2a, 2b, 2d, and 2e). The thermohaline isolines in the ocean interior indicate equatorward mass transport, as they descend to the west. Below this upper layer, we find the Antarctic Intermediate Water (AAIW) ($27.23 \text{ kg/m}^3 < \gamma^n < 27.58 \text{ kg/m}^3$, which corresponds to depths between 730 and 1,140 m). This water mass presents relatively cold waters of potential temperatures of 3–5°C (Figures 2a–2c), profile-minimum salinity values (34.3–34.5; Figures 2d–2f). Its dissolved oxygen concentration is relatively low at 24°S ($<200 \mu\text{mol/kg}$; Figure 2g) and higher at 34.5°S ($>220 \mu\text{mol/kg}$ at 34.5°S; Figure 2h). The AAIW is formed in the Southern Ocean, near the Subantarctic Front of the Antarctic Circumpolar Current (ACC) (Talley, 1996). Its formation is driven by a combination of cooling and mixing processes, as well as interactions between ocean currents, such as the ACC, before spreading into the South Atlantic (Matano et al., 2010; Sloyan & Rintoul, 2001). The main AAIW sources to the Atlantic Ocean are from the Southeastern Pacific, entering through the northern Drake Passage, the narrowest gap connecting the South Atlantic and Pacific Oceans between the Antarctic Peninsula and South America, and the Malvinas Current loop, a large clockwise circulation feature in the South Atlantic that flows around the Falkland Islands (Suga & Talley, 1995). At 34.5°S in the eastern basin of the South Atlantic Ocean, the high salinity of the AAIW density class is attributed to the mixing of older AAIW with the Red Sea Water coming from the Indian Ocean, which has a much higher salinity than that of the AAIW layers located in the southwestern Atlantic Ocean (Shannon & Hunter, 1988). The lower oxygen levels ($<180 \mu\text{mol/kg}$) in the eastern basin also point to an Indian Ocean source. This is supported by the fact that the Indian deep waters, which originate from upwelled bottom waters of greater age than those from the Atlantic Ocean sourced from surface waters (Gordon et al., 1992; Talley, 1996, 2013). Specifically, the Indian Ocean presents oxygen levels of 160–220 $\mu\text{mol/kg}$ between 600 and 1,200 m depth (McDonagh et al., 2008). The low oxygen concentrations are more noticeable in the 24°S section, further suggesting that these waters originate from the Indian Ocean and spread westward as they flow north in the Atlantic, before feeding the NADW overturn (Talley, 2013). Also, the minimum salinity patches (<34.3) in the western basin at 34.5°S suggest that the northward flow in the ocean interior transports more recently ventilated AAIW (Hernández-Guerra et al., 2019).

In the deep layer, with a neutral density range of $27.58 \text{ kg/m}^3 < \gamma^n < 27.84 \text{ kg/m}^3$, extending from about 1,140 to 1,600 m, we find the core of the Upper Circumpolar Deep Water (UCDW). The UCDW originates from the mixture of deep waters from the Indian, Pacific and Southern Oceans. This is a relatively oxygen-poor (180–200 $\mu\text{mol/kg}$; Figures 2g and 2h), fresh (34.5–34.7; Figures 2d–2f), and cold water mass (2.5–3°C; Figures 2a–2c).

NADW is also found in the deep layers, below the UCDW, at depths ranging from about 1,600 to 3,800 m ($27.84 \text{ kg/m}^3 < \gamma^n < 28.15 \text{ kg/m}^3$). This water mass is formed as a result of the mixing and aging of deep waters flowing latitudinally toward the Southern Ocean. NADW is identified in the vertical by relatively low potential temperature (1.5–2.5°C; Figures 2a–2c), high salinity (34.85–34.9; Figures 2d–2f), and high dissolved oxygen

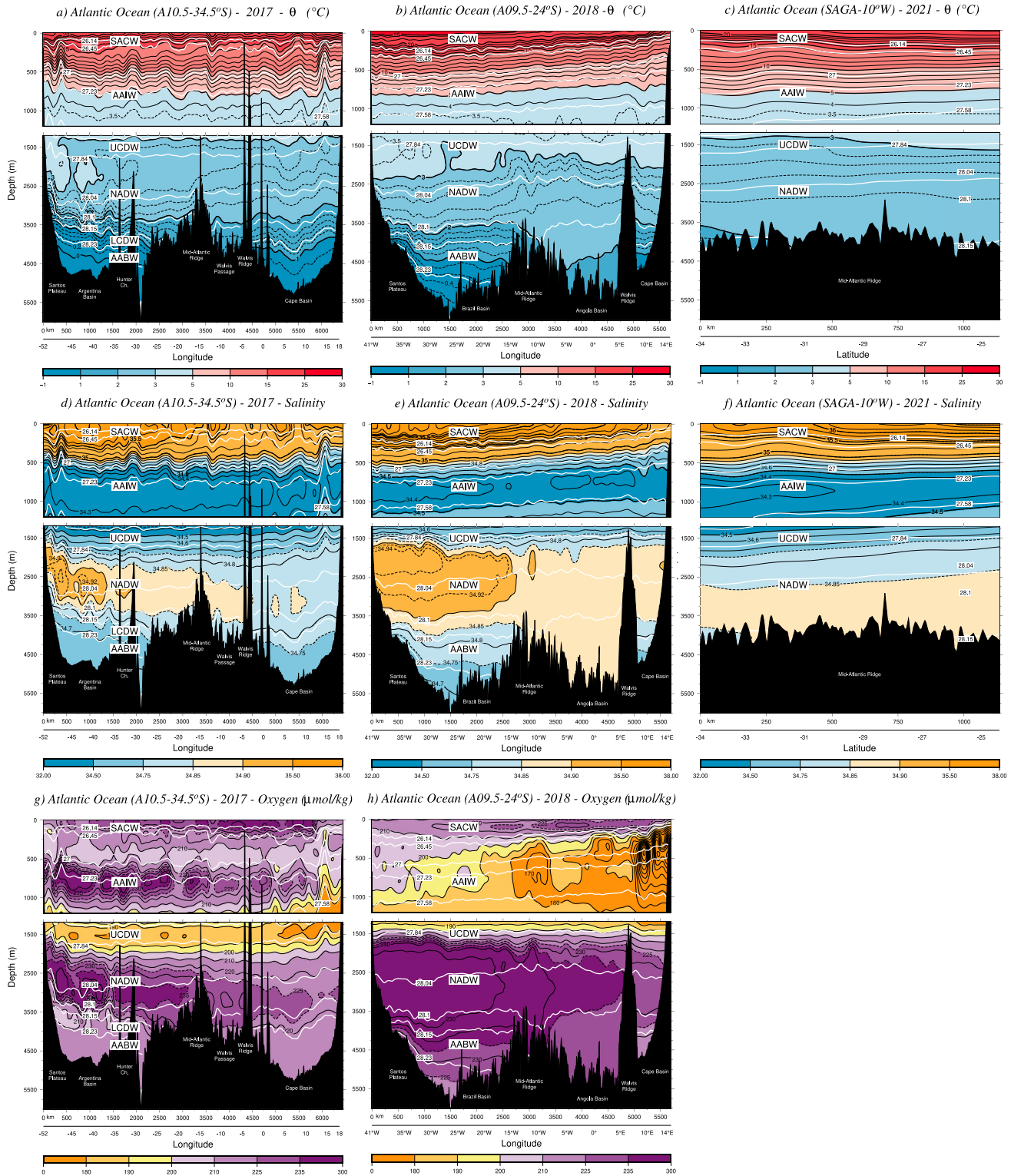


Figure 2. Vertical sections of (a–c) θ ($^{\circ}\text{C}$), (d–f) salinity, and (g, h) oxygen ($\mu\text{mol/kg}$) in the South Atlantic Ocean for data collected at 34.5°S in 2017, at 24°S in 2018 and at 10°W in 2021, respectively. The water masses identified are: South Atlantic Central Water (SACW), Antarctic Intermediate Water (AAIW), Upper Circumpolar Deep Water (UCDW), North Atlantic Deep Water (NADW), Lower Circumpolar Deep Water (LCDW), and Antarctic Bottom Water (AABW). The location of stations is indicated with the tick-marks on the top axis indicate the location of stations. The γ^{σ}_θ layers identified by isoneutral labels (white lines) are those used to compute the geostrophic transport.

concentration (200–250 $\mu\text{mol/kg}$; Figures 2g and 2h). The properties of the NADW are best observed in the western region, due to the eastward decrease in salinity and oxygen, toward the MAR. Additionally, the presence of the Deep Western Boundary Current (DWBC) shows up as anomalous values of potential temperature (1.53°C), salinity (34.7) and oxygen (206.7 $\mu\text{mol/kg}$) near the seafloor ($\approx 2,800$ m depth) at about 50°W, which contrasts with the respective values of 3.2°C, 34.9, and 228.9 $\mu\text{mol/kg}$ observed at 2,110 m depth (e.g., Reid et al., 1977; Zemba, 1991) (Figure 2).

The AABW is the densest water mass in the Atlantic, from $\approx 3,800$ m to the seafloor ($\gamma^n > 28.15 \text{ kg/m}^3$). The AABW is colder ($\theta < 1.5^\circ\text{C}$; Figures 2a and 2b), fresher (34.7–34.75; Figures 2d and 2e) and has lower dissolved oxygen concentrations (220–240 $\mu\text{mol/kg}$; Figures 2g and 2h) than the NADW. The main source of the AABW is the mixed Antarctic waters and the NADW (de Carvalho Ferreira & Kerr, 2017; Heywood & King, 2002; Mantyla & Reid, 1983; Peterson & Whitworth, 1989; Reid et al., 1977). The Walvis Ridge limits the northward flow of AABW in the eastern basin. The hydrographic section at 10°W is on the MAR with shallower depths than the AABW and, therefore, is not present in this section (Figures 2c, 2f, and 2i). The AABW can be separated into two different components at 34.5°S. The upper part of the AABW is formed in the Antarctic Circumpolar Current, which is a combination of AABW and NADW, resulting in a new water mass called Lower Circumpolar Deep Water (LCDW) (Mantyla & Reid, 1983; Stramma & England, 1999). The LCDW is the primary water mass in contact with the AABW within the Argentine Basin (Coles et al., 1996), between $28.15 \text{ kg/m}^3 < \gamma^n < 28.23 \text{ kg/m}^3$, between about 3,800 and 4,700 m. These water masses differ only slightly in most of the properties so that they are not clearly separated in the water column (Vanicek & Siedler, 2002). However, at 34.5°S the LCDW has slightly higher temperatures (≈ 1.0 – 1.5°C ; Figure 2a), higher salinity (34.75–34.8; Figure 2d) and lower dissolved oxygen concentrations (210–220 $\mu\text{mol/kg}$; Figure 2g) than the AABW ($\theta < 1^\circ\text{C}$, $S \approx 34.7$, $O_2 \approx 220 \mu\text{mol/kg}$; Figures 2a, 2d, and 2g).

4. Relative Geostrophic Transport and Inverse Model

At each station pair, the relative geostrophic velocity is computed using the thermal wind equation so the absolute velocity depends on the chosen reference layer. For section 34.5°S we choose the NADW-LCDW interface at $\gamma^n = 28.15 \text{ kg/m}^3$ ($\approx 3,800$ m depth) as reference layer (Figure 2). Similarly, for sections 24°S and 10°W we select the interface UCDW-NADW, located at the neutral density $\gamma^n = 27.84 \text{ kg/m}^3$ ($\approx 1,600$ m depth) (Figure 2). If the reference layer is deeper than the deepest common depth of a pair of stations, the bottom is selected as the reference level of no motion.

Otherwise, the SADCPC and LADCP data from the sections at 34.5°S and 10°W are used to estimate the velocities at the reference level, and only SADCPC data from the section at 24°S (Comas-Rodríguez et al., 2010; Joyce et al., 2001). Figure 3 presents the initial geostrophic velocity (dashed black lines), the average SADCPC velocity along the station-station track segment (red line), the mean LADCP velocity from each hydrographic station pair LADCP velocities (blue line), and the geostrophic velocity adjusted to the ADCPC velocity (black solid line). The velocity adjustments are performed under four different cases (a through d) for the sections at 34.5°S, 10°W, and 24°S. First, if either both SADCPC and LADCP (case a) or just SADCPC (case b) match the geostrophic velocity profile, then SADCPC data is used to adjust the initial geostrophic velocity. Next, if only the LADCP matches the profile of the geostrophic velocity but SADCPC does not, then LADCP data is used to adjust the initial geostrophic velocity (case c). When neither the SADCPC nor LADCP patterns match the geostrophic velocity profile, then the initial geostrophic velocity is not adjusted (case d). Notice that the LADCP velocities are located at each station rather than over the whole interval over which the geostrophic velocity is computed, while the underway SADCPC continuously collects data, so SADCPC can better match the location of the geostrophic calculation. Consequently, SADCPC data is considered to be more appropriate for estimating the reference level velocities in most cases (Arumí-Planas et al., 2022). Then, the adjusted reference velocity is estimated as the average velocity of the selected depths in the range of the dashed horizontal lines.

Mass transports are computed for 11 isoneutral layers following Arumí-Planas et al. (2022), Hernández-Guerra and Talley (2016), Hernández-Guerra et al. (2019), and Talley (2008) (Figures 2 and 4). The NCEP wind stress is used to calculate the Ekman transports (Kalnay et al., 1996) at the time of each hydrographic cruise (Arumí-Planas et al., 2022; Hernández-Guerra & Talley, 2016; Hernández-Guerra et al., 2019). The resulting Ekman transports, of $-1.6 \pm 0.1 \text{ Sv}$ at 24°S, $0.1 \pm 0.2 \text{ Sv}$ at 34.5°S, and $0.1 \pm 0.1 \text{ Sv}$ at 10°W, are included in the uppermost layer of each section.

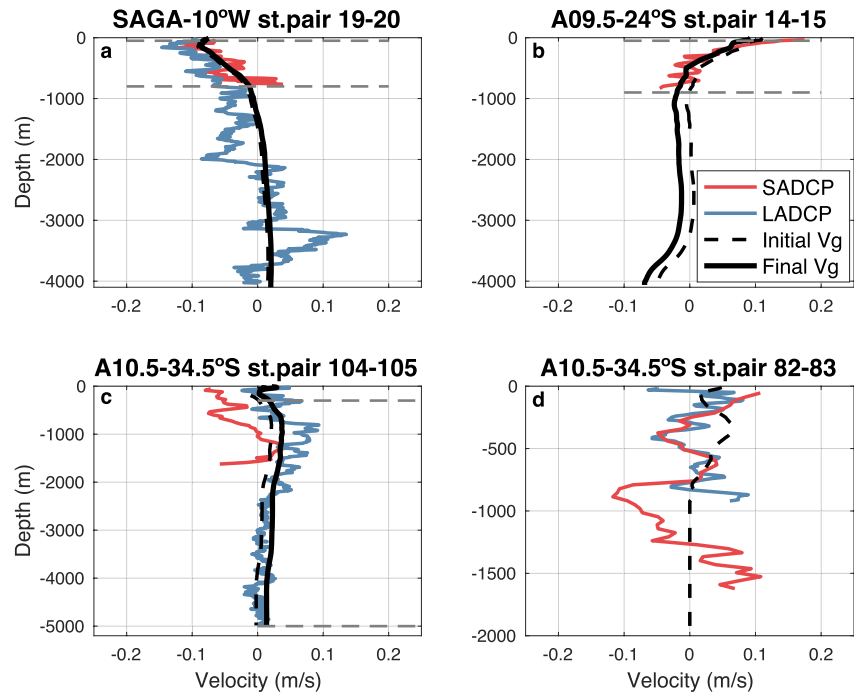


Figure 3. Comparison between the profiles of the initial geostrophic velocity (dashed black lines), the SADCP (red line) and LADCP (blue line) velocity normal to the station pairs, and the geostrophic velocity adjusted using the SADCP or LADCP data (black solid line) for four different cases of adjustment: (a) geostrophic velocities agree with both SADCP and LADCP data, (b) only SADCP data agree, (c) only LADCP data agree, and (d) neither SADCP nor LADCP data agree.

In our study, there are three enclosed regions (Figure 1): Box 1 is formed by the combined transatlantic sections at 34.5°S and 24°S, and Boxes 2 and 3 are respectively formed by the eastern and western stations of sections 34.5°S and 24°S combined with section 10°W. Figure 4 presents the initial integrated mass transports per layer for each enclosed region in the Atlantic Ocean; these initial estimates use the velocity at the reference layer as obtained from the ADCP data. There is an initial imbalance, integrated over all layers, of 5.3 Sv in Box 1, 30.4 Sv in Box 2, and -25.0 Sv in Box 3 (Table 1; positive and negative values represent divergence and convergence, respectively). The initial fields for the upper and bottom layers have a northward mass transport, while the deep layers present a southward mass transport across both the 34.5°S and 24°S transoceanic sections, and a westward and eastward mass transport for upper and deep layers through the 10°W meridional section, respectively.

The inverse box model (Wunsch, 1978, 1996) uses constraints on transports to adjust the reference velocities and produce a consistent solution for each enclosed region, reducing the large initial imbalances. The following equation for mass transport is solved:

$$\iint \rho b dx dz = - \iint \rho v_r dx dz + E_k$$

where ρ is the seawater density, b designates the unknown reference velocity, v_r is the initial estimate for the geostrophic velocity derived from the thermal wind equation and after incorporating the reference velocities through an adjustment to the SADCP or LADCP data, E_k is the normal Ekman transport to the section, and the along-section and vertical coordinates are denoted by x and z , respectively. Appendix A provides the full matrix equation and its derivation, while the constraints used are given in Table 1.

The approach used for the inverse model solution is the same approach as the one developed by Joyce et al. (2001) and later applied by Arumí-Planas et al. (2022), Casanova-Masjoan et al. (2020), and Hernández-Guerra et al. (2014). The unknown geostrophic reference velocity at each station pair, as well as the section adjustment to the Ekman velocity, along with their standard deviations, are estimated using a system of mass conservation equations, which requires an enclosed region. This procedure provides 48 equations for the vertically integrated mass constraints with 262 unknowns (the total number of station pairs of the three hydrographic sections combined).

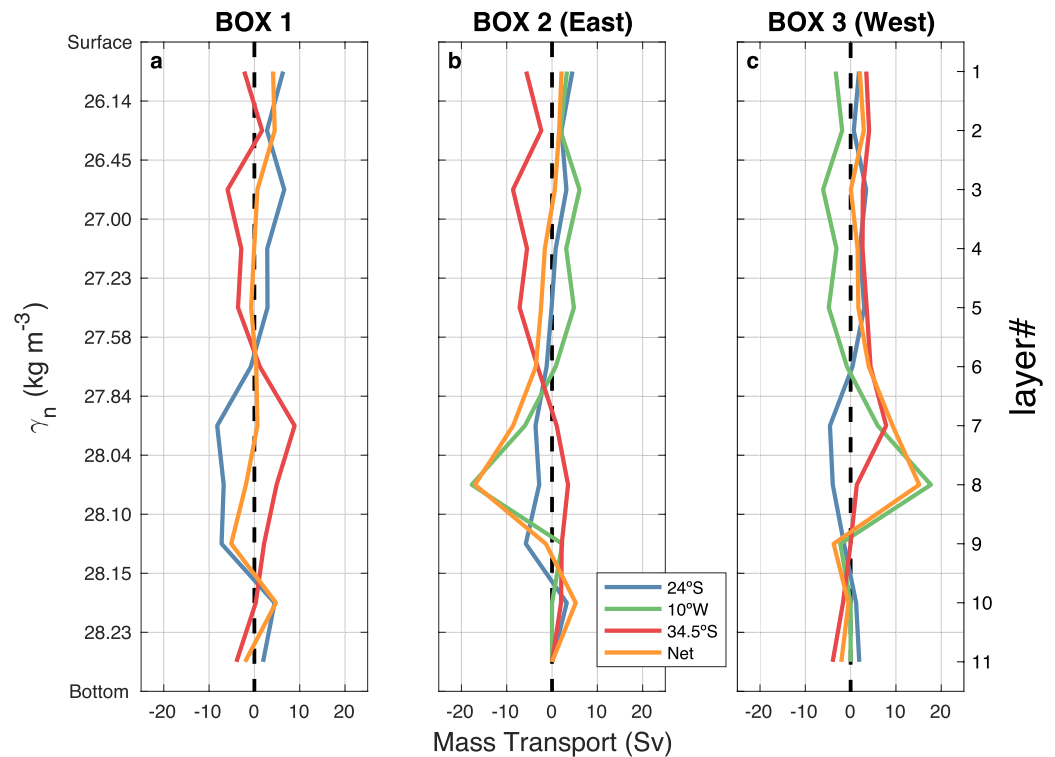


Figure 4. Initial integrated mass transports (Sv) per neutral density layer at 24°S (blue line), 10°W (green line) and 34.5°S (red line), and the net (orange line) in the South Atlantic Ocean. The three panels correspond to the mass transport in (a) Box 1, (b) Box 2, and (c) Box 3. The sign of the transports is changed as to maintain the same sign convention in all boxes: positive mass transports flow out of the box and negative mass transports flow into the box.

For each box, both total mass and mass in each neutral density layer are conserved, with the Ekman transport adjustment included in the first layer. The next four constraints are the mass balance (based on the Bering Strait transport) for sections 24°S and 34.5°S separately, as well as mass balance for two transatlantic sections composed of the western/eastern station pairs section 24°S plus section 10°W and the eastern/western station pairs of section 34.5°S, respectively. In addition to the total mass constraints, eight regional constraints across several longitude and depth ranges were introduced to reduce this underdetermined system (Table 1). These constraints have been previously applied in earlier studies of the South Atlantic Ocean as in other inverse models (Table 1; Hogg et al., 1982; Warren & Speer, 1991; Zenk et al., 1999), although the recent study of Finucane and Hautala (2022) suggested that the bottom transport estimated in the Hunter Channel by Zenk et al. (1999) could be overestimated. We have also included new constraints for 34.5°S from recent studies by Chidichimo et al. (2021), Kersalé et al. (2019), and Meinen et al. (2017) using data from the moored arrays deployed along this section as part of the South Atlantic MOC Basin-wide Array (SAMBA) (Ansorge et al., 2014; Garzoli & Matano, 2011; Meinen et al., 2013, 2017, 2018). Moreover, we use ADCP data from section 24°S to constrain the Brazil Current (as previously done for the hydrographic section at 30°S by Hernández-Guerra et al. (2019)).

The Gauss-Markov method is used to solve the inverse problem (Wunsch, 1996), which requires a priori variances for each equation and solution. The a priori variances for each equation, corresponding to each regional constraint, are expressed as standard deviations (Table 1), except the Brazil Current at 24°S where we have assigned 5 Sv to consider the uncertainty of the Brazil Current transport based on the differences between hydrographic sections at 24°S in 2009 (Bryden et al., 2011) and 2018, as also considered in Hernández-Guerra et al. (2019) for a 30°S section. Furthermore, we have assigned a priori variances for the layer mass conservation equations: 3.6 Sv in each of layers 1–4, 2.2 Sv for layers 5–7, and 1.1 Sv for layers 8–11. The a priori velocity variance for the ocean interior's solution is set to $(2 \text{ cm/s})^2$, while it is raised to $(4 \text{ cm/s})^2$ in regions with strong shear, which corresponds to both eastern and western boundaries. The a priori variances are large enough to adjust the mass transports for every oceanographic cruise condition with the inverse model (Table 1). The Gauss-Markov method solves the underdetermined system of equations by selecting the solution with the least variance, given the reference level

Table 1
Constraints and Results of the Inverse Model for the South Atlantic Ocean as Obtained Using the 34.5°S, 24°S, and 10°W Sections

South Atlantic ocean	Property	Longitude	Layers	Constraint (Sv)	Initial (Sv)	Final (Sv)
A10.5–34.5°S	Bering imbalance ^a	All	All	-0.8 ± 0.6	-0.5	-0.7 ± 2.9
	Vema Channel ^b	50.8°W–34.9°W	9:11	4.0 ± 0.4	6.5	4.0 ± 0.9
	Hunter Channel ^c	33.6°W–27.0°W	9:11	2.9 ± 1.2	-0.7	2.8 ± 1.0
	Brazil Current ^d	Coast to 49.2°W	1:5	-14.0 ± 8.8	-20.0	-16.5 ± 1.3
	Benguela Current ^e	10.9°E to coast	1:5	24.0 ± 17.0	27.5	26.3 ± 2.0
	DEBC ^e	13.6°E to coast	6:9	-12.0 ± 17.0	-8.3	-15.1 ± 3.5
	DWBC ^f	Coast to 47.3°W	6:9	-15.0 ± 23.0	-18.7	-13.9 ± 3.0
	DWBC _{rec}	47.3°W–46.8°W	6:9	NC	3.3	3.0 ± 1.3
A09.5–24°S	Bering imbalance ^a	All	All	-0.8 ± 0.6	4.8	-0.7 ± 3.1
	Walvis R. North ^g	4.6°E to coast	9:11	0.0 ± 1.0	5.0	-0.7 ± 0.7
	Brazil Current ^h	Coast to 40.5°W	1:5	-8.4 ± 5.0	-8.4	-7.3 ± 0.9
	Benguela Current	27.6°W to coast	1:5	NC	25.8	21.2 ± 1.8
	DEBC	2.6°E to coast	6:9	NC	-3.5	-16.3 ± 4.7
	DWBC	Coast to 35.2°W	6:9	NC	-9.2	-8.7 ± 3.8
	DWBC _{rec}	35.2°W–33.7°W	6:9	NC	6.5	6.4 ± 2.7
34.5°S (West)–10°W–24°S (East)	Bering imbalance ^a	Coast to 10.6°W (34.5°S)	All	-0.8 ± 0.6	22.7	-0.9 ± 11.0
		All (10°W) 9.9°W to coast (24°S)				
24°S (West)–10°W–34.5°S (East)	Bering imbalance ^a	Coast to 10.4°W (24°S)	All	-0.8 ± 0.6	29.9	-1.9 ± 9.4
		All (10°W) 10.0°W to coast (34.5°S)				
34.5°S–24°S	Total mass conserved in Box 1	All (34.5°S)All (24°S)	All	0.0 ± 1.0	5.3	0.0 ± 15.5
34.5°S (West)–10°W–24°S (West)	Total mass conserved in Box 2	Coast to 10.4°W (34.5°S)	All	0.0 ± 1.0	30.4	1.2 ± 10.2
		All (10°W) Coast to 10.6°W (24°S)				
34.5°S (East)–10°W–24°S (East)	Total mass conserved in Box 3	10.0°W to coast (34.5°S)	All	0.0 ± 1.0	-25.0	-1.2 ± 12.6
		All (10°W) 9.9°W to coast (24°S)				

Note. Positive transports are northward-eastward, and negative are southward-westward; while in the box imbalances, positive/negative values represent divergence/convergence. Initial and final transports relative to the reference layer (at $\gamma^n = 28.15 \text{ kg/m}^3$ for the 34.5°S section and $\gamma^n = 27.84 \text{ kg/m}^3$ for the 24°S and 10°W sections) are listed. The constraints set in the inverse model for the regional transports are also shown; NC stands for non-constraint.

^aBering imbalance in Total Mass Conservation from Coachman and Aagaard (1988). ^bBottom transport constraint in the Vema Channel from Hogg et al. (1982). ^cBottom transport constraint in the Hunter Channel from Zenk et al. (1999). ^dBrazil Current constraint from Chidichimo et al. (2021). ^eBenguela Current and Deep Eastern Boundary Current (DEBC) constraints from Kersalé et al. (2019). ^fDeep Western Boundary Current (DWBC) constraint from Meinen et al. (2017). ^gBathymetric constraint from Warren and Speer (1991). ^hBoundary current constraints from cruise-based ADCP profiles.

velocities along with their corresponding uncertainties. Finally, we compute the adjusted mass transports and their uncertainties.

The initially adjusted velocities estimated at the reference level, those from the SADC and LADC data, and as produced by the inverse model are shown in Figure 5. The velocities adjusted using the ADCP data (Figure 5a) are greater than those obtained from the inverse model (Figure 5b). The inverse solution velocities are not significantly different from zero (i.e., $-0.02 \pm 0.08 \text{ cm/s}$) in most ocean interior stations, as in earlier inverse models (Arumí-Planas et al., 2022; Hernández-Guerra & Talley, 2016; Hernández-Guerra et al., 2019), as well as on the eastern and western boundaries (i.e., $-0.04 \pm 0.08 \text{ cm/s}$). The inverse model adjustment does not produce a significant change to initial Ekman transports on any section (inverse estimates of $-1.6 \pm 0.2 \text{ Sv}$ at 24°S, $0.1 \pm 0.2 \text{ Sv}$ at 34.5°S, and $0.1 \pm 0.1 \text{ Sv}$ at 10°W).

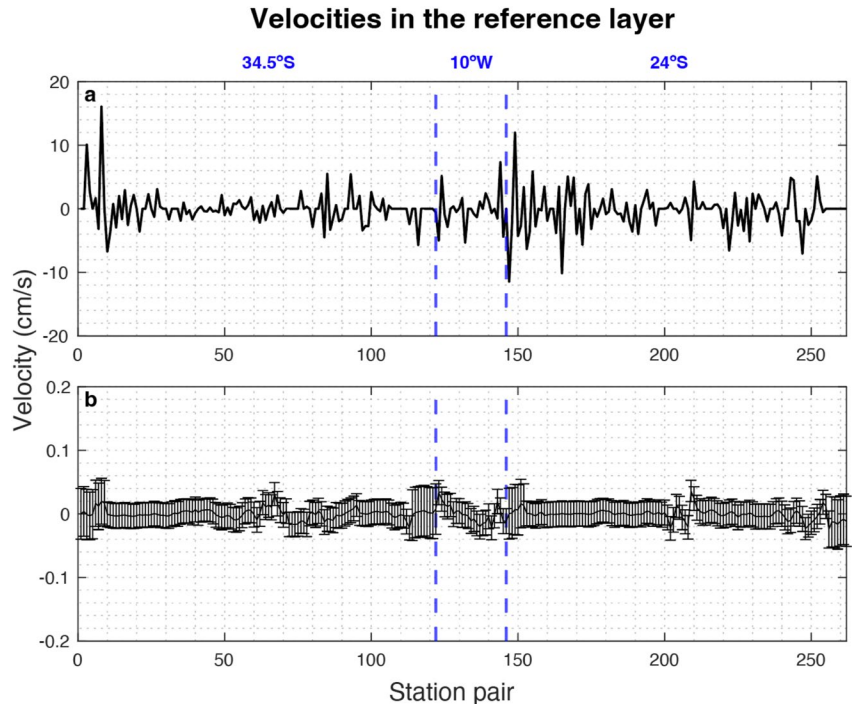


Figure 5. (a) Reference velocities (cm/s) as adjusted using ADCP data and (b) velocity adjustment from the inverse model with error bars as a function of station pair numbers for the three hydrographic sections: 34.5°S (station pair from 1 to 122), 10°W (stations pair from 123 to 146), and 24°S (station pair from 147 to 262). The blue dotted lines separate the transect, as shown in the upper legend. Positive and negative velocities are north/east or south/west, respectively.

5. Adjusted Meridional and Zonal Transports

After applying the inverse model, the final adjusted mass transports per neutral density layer in each enclosed region model are presented in Figure 6. The total mass imbalance in each closed box is insignificantly different from zero, well within the corresponding uncertainties (0.0 ± 15.5 Sv in Box 1, 1.2 ± 10.2 Sv in Box 2, and -1.2 ± 12.6 in Box 3). Therefore, we may say that mass transport is conserved in all three closed regions.

The meridional overturning transports across the transatlantic sections at 34.5°S and 24°S are computed by zonally and vertically integrating the mass transport from the bottom to the sea surface (Figure 7). The strength of the AMOC at each latitude is defined as the vertical maximum of the stream function, which is always found in the upper cell (Buckley & Marshall, 2016). The AMOC intensity at 24°S is 17.5 ± 0.9 Sv, which is stronger than the 14.8 ± 1.0 Sv estimated at 34.5°S. Based on Figure 7, we may divide the Atlantic Ocean in a three-layer system at 24°S and 34.5°S, with mass transports flowing northward in the uppermost layers (1–5), southward in the deep layers (6–9), and northward in the abyssal layers (10–11); it is the upper cell that differs most between 24°S and 34.5°S. In contrast, in the meridional 10°W section (not shown) there is no mass transport in the abyssal layers (Figures 6b and 6c), hence it can be viewed as a two-layer system, with mass transports flowing westward in the uppermost layers (1–5) and eastward in the deep layers (6–9).

6. Horizontal Circulation From Adjusted Transport

Figure 8 presents the horizontally accumulated mass transport for different isoneutral layers along 24°S (a, b, c), 34.5°S (d, e, f), and 10°W (g, h). The inverse model results are presented with positive northward/eastward transports and negative southward/westward transports. For sections 24°S and 34.5°S, the mass transport is accumulated integrating eastward, whilst for section 10°W, it is accumulated integrating northward. As the inverse box solution finds a solution that satisfies mean constraints and uses hydrographic data from different

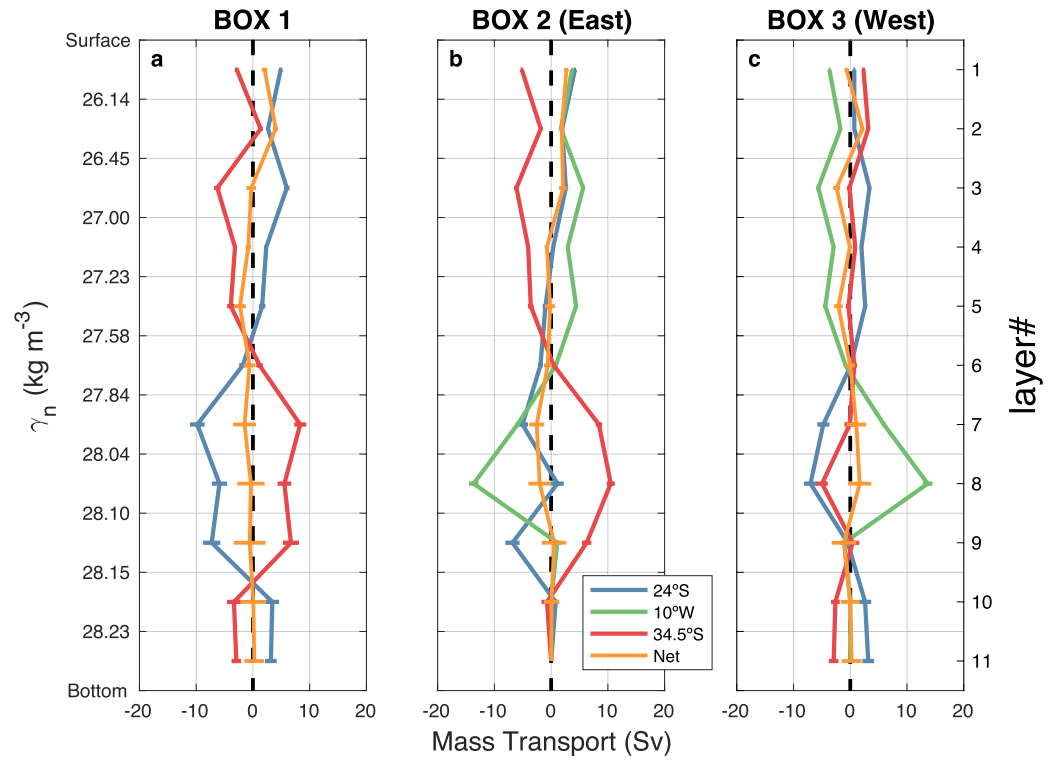


Figure 6. Final integrated mass transports (Sv) per neutral density layer at 24°S (blue line), 10°W (green line), 34.5°S (red line) and the net (orange line) with the corresponding error bars, in the South Atlantic Ocean; the net imbalance per layer is also shown. The three panels correspond to the mass transport in (a) Box 1, (b) Box 2, and (c) Box 3. The sign of the transports is changed as to maintain the same sign convection in all boxes: positive mass transports flow out of the box and negative mass transports flow into the box.

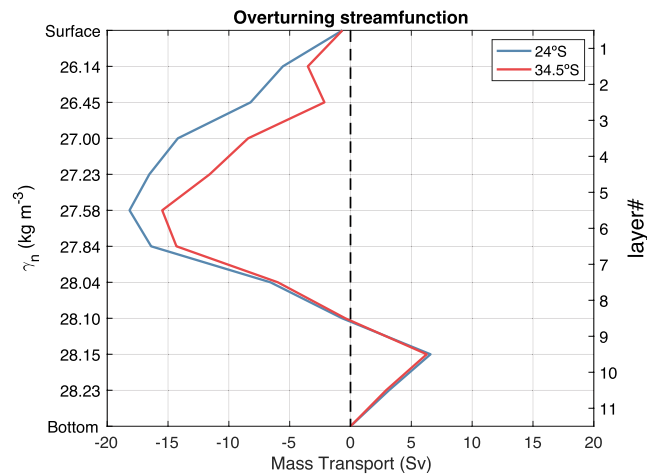


Figure 7. Overturning streamfunction of mass transport across 24°S (red line) and 34.5°S (blue line) in the Atlantic Ocean for 2018 and 2017, respectively. The function is computed by integrating the mass transport vertically and horizontally in isoneutral layers, from the seafloor to the sea surface across the entire section.

years, they represent in some sense a time mean circulation. For this reason, we have included in Figure 8 the accumulated transports using ECCO (2017) and GLORYS (2017–2019) to examine averages over the time period from both models for 24°S and 34.5°S sections, and none for 10°W because no models are available for 2021.

6.1. Upper Ocean

The SACW-AAIW stratum includes the thermocline and intermediate waters (from the sea surface down to $\sigma^{\theta} = 27.23 \text{ kg/m}^3$, approximately down to 730 m; Figures 8a, 8d, and 8g). The mass transport in these upper layers presents a northward recirculation near the western boundary, a net northward mass transport through the ocean interior, and a wide and slow Benguela Current in the eastern boundary, rendering the typical pattern of the subtropical gyre (Figures 8a and 8d). The alternating mass transports in the entire subtropical gyre are caused by mesoscale eddies, bringing the saw-like streamfunction described in Hernández-Guerra et al. (2005).

In the western boundary, off the east coast of South America, a relatively strong Brazil Current flows poleward. The Brazil Current has been previously described by Garzoli et al. (2013) from XBTs at 35°S, by Müller et al. (1998) from current moorings between 20°S and 28°S, and by McDonagh and King (2005) and Hernández-Guerra et al. (2019) from hydrographic data at 30°S. In our study, the Brazil Current shows up clearly by the tilting isopycnals, at 24°S as a narrow jet ($\approx 37 \text{ km}$) from the coast to about 40.5°W with a southward mass transport of $-7.3 \pm 0.9 \text{ Sv}$ at 24°S, and at 34.5°S as a much wider jet that extends from the coast to about 49.2°W (127 km) with a southward transport of $-16.6 \pm 1.3 \text{ Sv}$ (see also Manta et al., 2021) (Table 1). Thus, the Brazil Current increases its mass transport to the south. In these upper layers, the OGCM reproduces reasonably well the inverse model transports at 24°S and 34.5°S (Figures 8a and 8d, respectively), but with some significant differences in the extension and intensity of the boundary transports. Specifically, at 24°S GLORYS do not show a western boundary current, while ECCO presents a similar Brazil Current transport of $-6.8 \pm 1.5 \text{ Sv}$ from the coast to 38.3°W. The OGCM transports at 34.5°S are stronger ($-28.7 \pm 12.7 \text{ Sv}$ from the coast to 49.3°W in GLORYS and $-21.5 \pm 1.9 \text{ Sv}$ from the coast to 46.5°W) than the inverse model.

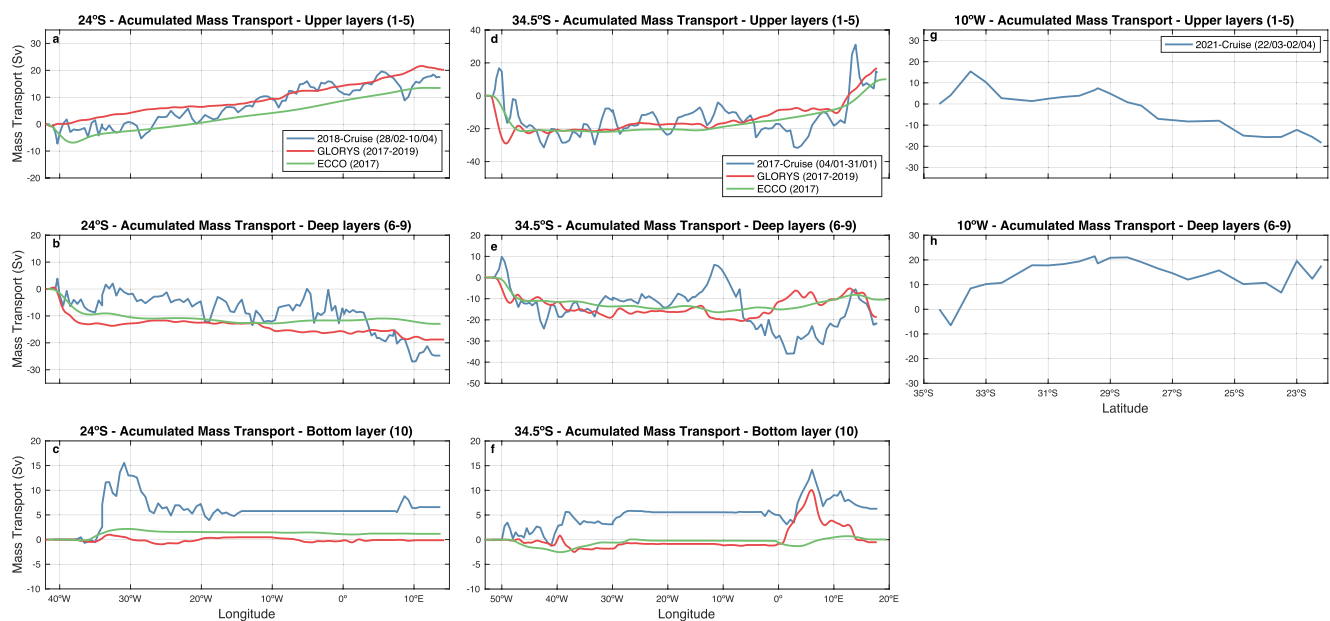


Figure 8. Eastward accumulated mass transports (Sv) at 24°S (a–c) and 34.5°S (d–f), and northward accumulated mass transport (Sv) at 10°W (g, h) in the Atlantic Ocean for the upper (1:5), deep (6:9), and bottom (10:11) layers; the positive/negative mass transports are northward/southward at 24°S and 34.5°S, and eastward/westward at 10°W. The mass transports obtained from the inverse model (blue curves) are compared with the available simulations from the ECCO (green curves) and GLORYS (red curves) circulation models averaged over time.

In the eastern margin, between the African coast to about 10.9°E (Reid, 1989), the Benguela Current is observed as a relatively wide and strong northward eastern boundary current of the South Atlantic Subtropical Gyre. The Benguela Current flows northward becoming wider at 24°S (from 27.6°W to the coast). The strength of the Benguela Current, from above ~730 m depth (layers 1–5, between the surface and $\gamma^{\theta} = 27.23 \text{ kg/m}^3$), is estimated to be $26.4 \pm 2.0 \text{ Sv}$ at 34.5°S, which is slightly stronger than the much wider Benguela Current of $21.2 \pm 1.8 \text{ Sv}$ at 24°S (Table 1). The mass transport at 10°W, between 28.4° and 22.4°S, is $-19.2 \pm 1.4 \text{ Sv}$, which corresponds to the branch of the Benguela Current that runs above the MAR (Figure 8g). At 24°S, GLORYS and ECCO represent a weaker Benguela Current in the western boundary of 14.6 ± 2.7 and $15.3 \pm 0.8 \text{ Sv}$, respectively, from 27°W to the coast. Furthermore, at 34.5°S OGCM presents a similar Benguela Current transport to the hydrographic data from 9.3°E to the coast of $26.9 \pm 14.1 \text{ Sv}$ and from 8.5°E to the coast of $28.1 \pm 0.7 \text{ Sv}$ in GLORYS and ECCO, respectively.

6.2. Deep Layers

The mass transport for the UCDW-NADW deep layers flows southward and eastward (layers 6–9, from 27.58 to 28.1 kg/m^3) (Figures 8b, 8e, and 8h). The accumulated poleward mass transport in these layers presents no significant differences through 24°S ($-24.7 \pm 2.5 \text{ Sv}$) and 34.5°S ($-21.7 \pm 2.2 \text{ Sv}$). Moreover, the accumulated mass transport for these layers at 10°W presents a net mass transport of $17.7 \pm 1.1 \text{ Sv}$, which reflects that part of the deep waters flow eastward from 34.5°S to 33.5°S ($10.2 \pm 2.8 \text{ Sv}$) before recirculating in the south, an eastward flow close to 24°S ($7.5 \pm 4.4 \text{ Sv}$), and other recirculation routes along the meridional section (Figure 8h).

According to multiple research studies (e.g., Ganachaud, 2003; Meinen & Garzoli, 2014; Meinen et al., 2017; Müller et al., 1998), NADW is principally transported southward in the Atlantic Ocean by the DWBC. Based on the hydrographic sections examined in the present study, the DWBC presents a southward mass transport of $-8.7 \pm 3.8 \text{ Sv}$ from the coast to 35.2°W at 24°S and $-13.9 \pm 3.0 \text{ Sv}$ from the coast to 47.3°W at 34.5°S (Table 1). The northward recirculation of the DWBC is found just east of these longitudes (to about 33.7°W and 46.8°W at 24°S and 34.5°S, respectively), presenting an equatorward mass transport of $6.4 \pm 2.7 \text{ Sv}$ at 24°S and $3.0 \pm 1.3 \text{ Sv}$ at 34.5°S (Table 1). In the deep layers, at 24°S GLORYS presents a stronger DWBC poleward mass transport ($-13.0 \pm 3.8 \text{ Sv}$) than the inverse model (Figure 8b), while ECCO presents a similar DWBC of $-9.4 \pm 2.6 \text{ Sv}$ both from the coast to 35.8°W. At 34.5°S, the OGCM replicates fairly well the intense DWBC ($-11.7 \pm 7.4 \text{ Sv}$ from the coast to 48.5°W in GLORYS, and $-11.1 \pm 1.6 \text{ Sv}$ from the coast to 46°W in ECCO). However, both numerical models have substantial differences from the inverse model in the ocean interior (Figure 8e). These differences could be explained by the fact that our inverse model results present higher resolution because they are based on observations. In contrast, OGCMs often use assumptions and parameterizations to simplify the complexity of ocean processes, introducing errors and biases into the model results, particularly in the ocean interior and deep layers where observational data are limited.

From our inverse model results, the DEBC presents a northward mass transport of $-16.3 \pm 4.7 \text{ Sv}$ at 24°S, which is similar to the $-15.1 \pm 3.5 \text{ Sv}$ obtained at 34.5°S. Therefore, the branch from the DWBC feeding the DEBC comes from latitudes north of 24°S, which is corroborated with the westward flow above the MAR close to 24°S at 10°W. At 24°S in the eastern boundary, GLORYS ($-3.0 \pm 3.3 \text{ Sv}$ from 3.8°E to the coast) and ECCO ($-1.8 \pm 1.8 \text{ Sv}$ from 7.3°E to the coast) present a weaker DEBC than the inverse model, and at 34.5°S ECCO also displays a weaker DEBC of $-2.3 \pm 0.5 \text{ Sv}$ from 14°E to the coast, while GLORYS estimates a similar transport ($-13.5 \pm 12.7 \text{ Sv}$ from 12.8°E to the coast) if compared with the inverse model.

6.3. Bottom Layers

The LCDW-AABW water masses (layers 10–11, below $\gamma^{\theta} = 28.15 \text{ kg/m}^3$) present a low net equatorward mass transport of $6.6 \pm 1.6 \text{ Sv}$ at 24°S and $6.3 \pm 1.5 \text{ Sv}$ at 34.5°S (Figures 8c and 8f). In the western basin, the northward transport over the Argentine Basin at 34.5°S ($5.6 \pm 1.1 \text{ Sv}$) passes through the Vema Channel ($3.5 \pm 0.7 \text{ Sv}$) and Hunter Channel ($2.3 \pm 0.9 \text{ Sv}$) to reach 24°S ($5.8 \pm 1.5 \text{ Sv}$). Whereas in the eastern basin, the equatorward flow over the Cape Basin at 34.5°S ($8.6 \pm 3.5 \text{ Sv}$) barely reaches 24°S ($3.0 \pm 0.8 \text{ Sv}$), as some flow recirculates ($2.2 \pm 0.7 \text{ Sv}$) and some flow turns back to 34.5°S ($-7.9 \pm 3.6 \text{ Sv}$). Additionally, the MAR limits the east/westward

flow of the abyssal waters at 10°W, presenting no mass transport in these layers. At 24°S, GLORYS shows no mass transport in the abyssal layers (Figure 8c) but does fairly well at 34.5°S, reproducing the alternating mass transport between both basins, while the ECCO output differs greatly from the inverse results at both latitudes.

7. Heat and Freshwater Transports

The heat transport is computed by using the following expression:

$$HT = \sum_i \sum_j \rho_{ij} c_{p_{ij}} \theta_{ij} v_{ij} \Delta x \Delta z$$

where ρ_{ij} is the density, $c_{p_{ij}}$ is the heat capacity of the seawater, θ_{ij} is the potential temperature, and v_{ij} is the absolute cross-section velocity, and the i, j subindexes identify the station pair and layer, respectively. Positive values indicate a northward heat flux, while negative values imply a southward heat flux.

The positive values estimated from the meridional heat transports after the inverse model at 34.5°S (0.30 ± 0.05 PW) and 24°S (0.80 ± 0.05 PW) indicate an increase in the equatorward flux in the subtropical South Atlantic. In addition, these results reflect the northward direction of the warm waters in the upper layers at both latitudes in the South Atlantic Ocean. The heat transport in GLORYS agrees with the inverse model results at these latitudes (0.43 ± 0.26 PW and 0.71 ± 0.14 PW at 24°S and 34.5°S, respectively), while ECCO presents a similar heat transport at 34.5°S (0.34 ± 0.15 PW) and weaker at 24°S of 0.44 ± 0.10 PW than our inverse model results at this latitude but yet reproduces the increase in northward heat transport.

The freshwater flux (in FSv, Sverdrup for freshwater transport without mass balance) is estimated according to Joyce et al. (2001), taking into account the precipitation over evaporation:

$$\bar{F} = - \sum_i \sum_j T_{ij} S'_{ij} / S_0$$

where T_{ij} is the absolute mass transport, S'_{ij} is the anomaly of salinity (Salinity- S_0), both in layer i at station pair j , and S_0 is the global ocean mean salinity set to 34.9 as in Arumí-Planas et al. (2022), Hernández-Guerra & Talley. (2016), and Talley (2008). At 24°S there is a southward transport of freshwater (-0.07 ± 0.02 FSv), while at 34.5°S there is a northward transport of freshwater (0.18 ± 0.02 FSv). Therefore, our results suggest that in the 24°S–34.5°S domain, evaporation predominates over precipitation (as in Cañzós et al. (2022)). The freshwater transports from the OGCM and the inverse model are not significantly different. The GLORYS freshwater transports have the same direction as the inverse model at 24°S (-0.05 ± 0.07 FSv) and 34.5°S (0.25 ± 0.11 FSv), while ECCO presents a slightly higher value at 24°S (0.01 ± 0.05 FSv) and weaker freshwater transport at 34.5°S (0.07 ± 0.07 FSv) than the inverse model.

8. South Atlantic Schematic Circulation

Figure 9 sketches a circulation in the upper, deep and bottom layers in the South Atlantic between 24°S and 34.5°S and above the MAR that is coherent with the mass transports as inferred from our inverse box model. The net mass transport from the inverse model indicates that the predominant northward path of the upper layers is found in the easternmost region of the 34.5°S section (26.3 ± 2.0 Sv), expanding to a wider area at 24°S (8.1 ± 0.7 Sv east of the 10°W). It also shows that a fraction of the northward flow turns west through the MAR in the northern stations of 10°W, between 22.4°S and 28.4°S (-19.2 ± 1.4 Sv), which then splits into two branches, one flowing north to 24°S (13.1 ± 1.6 Sv west of 10°W, summing a total northward flow of 21.2 ± 1.8 Sv at 24°S) and the second branch reaching the western boundary (6.1 ± 1.4 Sv). These mass transports together with the southward flow at the westernmost part of the 24°S section to 34.5°S describe the anticyclonic course of the South Atlantic subtropical gyre.

In the deep layers, the DWBC and DEBC flow southward from 24°S (-8.7 ± 3.8 Sv and -16.3 ± 4.7 Sv, respectively) to 34.5°S (-13.9 ± 3.3 Sv and -15.1 ± 3.5 Sv, respectively). The scheme turns more complicated as an eastward branch flows over the MAR (7.5 ± 4.4 Sv) near 24°S and several recirculation routes appear to take place throughout the entire 10°W section (Figure 8).

Finally, the abyssal waters present a northward mass transport from the Argentine Basin (5.6 ± 1.1 Sv at 34.5°S) to the Brazil Basin (5.8 ± 1.5 Sv at 24°S), as well as an equatorward flow from the Cape Basin (8.6 ± 3.5 Sv at

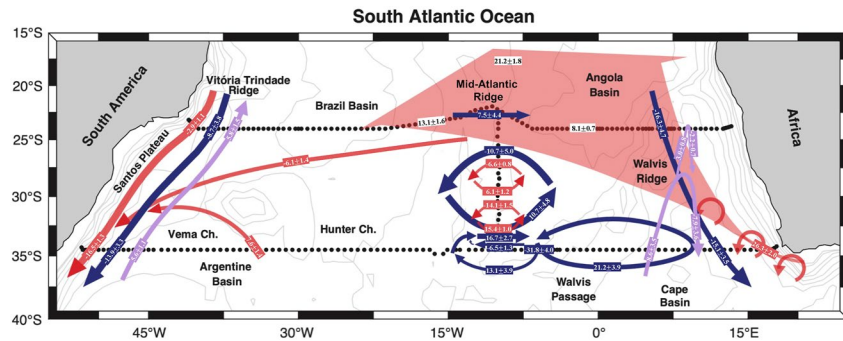


Figure 9. Schematic circulation in the upper (red), deep (blue) and bottom (purple) layers of the South Atlantic Ocean, consistent with the mass transports calculated across 24°S, 10°W, and 34.5°S. The net mass transports (in Sv) are indicated, with the positive transports northward and eastward and the negative transports southward and westward.

34.5°S), which barely reaches the 24°S (3.0 ± 0.8 Sv) section before returning southwards (-2.2 ± 0.7 Sv) until 34.5°S (-7.9 ± 3.6 Sv).

9. Discussion and Concluding Remarks

We have used hydrographic data sampling three enclosed regions for inverse modeling in the South Atlantic subtropical gyre. The initial geostrophic velocity is first adjusted to the velocities from ADCP data, and subsequently with the reference velocities as obtained from an inverse box model, such as to satisfy water mass balances in the three enclosed regions.

In the upper layers, the Brazil Current flows as a relatively intense western boundary current, increasing southward from -7.3 ± 0.9 Sv at 24°S to -16.6 ± 1.3 Sv at 34.5°S. The GLORYS and ECCO models do not properly represent the Brazil Current at 24°S, but both represent a slightly weaker (GLORYS: -12.7 Sv in January; ECCO -9.8 Sv in 2017 mean) or stronger (GLORYS -29.1 Sv in 2017–2019 mean; ECCO -22.5 Sv in January) Brazil Current transport at 34.5°S. Our result at 24°S agrees with the 4.9–12.3 Sv estimated by Bryden et al. (2011) but is slightly higher than the 5.8 ± 0.1 Sv estimated by Evans et al. (2017). Further, our estimates for the Brazil Current are consistent with a recirculation cell south of 28°S in the western South Atlantic, found both by Stramma (1989) (from -9.6 Sv at 24°S to -17.5 Sv at 33°S) and by Garzoli et al. (2013) (from -8.6 ± 4.1 Sv at 24°S to -19.4 ± 4.3 Sv at 35°S). Moreover, Schmid and Majumder (2018) combined Argo-float and sea surface height data to propose that the Brazil Current intensifies to the south, but with weaker mean mass transports (-2.3 ± 0.9 at 24°S and -12.6 ± 2.6 Sv at 35°S).

The Benguela Current flows in the upper layers as a broad and relatively strong equatorward eastern boundary current, which changes from 26.4 ± 2.0 Sv at 34.5°S to 21.2 ± 1.8 Sv at 24°S. The GLORYS and ECCO models present a similar transport at 34.5°S, of 21.6 and 20.3 Sv, respectively, and GLORYS shows a Benguela Current of 25.5 Sv at 24°S. Our transports at 34.5°S agree with the previously reported values by Kersalé et al. (2019) (24.0 ± 17.0), Garzoli et al. (2013) (22.5 ± 4.7 Sv), and Majumder and Schmid (2018) (19 ± 3 Sv). These results show that the Benguela Current is a relatively strong eastern boundary current, much stronger than the Canary Current in the North Atlantic (Casanova-Masjoan et al., 2020) and the Peru-Chile Current in the South Pacific (Arumí-Planas et al., 2022). The accumulated mass transport at 10°W presents a westward mass transport in the upper layers (-18.4 ± 0.4 Sv), consistent with the westward branch of the Benguela Current over the MAR (Garzoli & Gordon, 1996; Richardson & Garzoli, 2003; Rodrigues et al., 2007; Stramma, 1991).

The accumulated mass transport in the deep layers presents a net northward mass transport of UCDW-NADW through 24°S and 34.5°S of -24.7 ± 2.5 Sv and -21.7 ± 2.2 Sv, respectively. In the western boundary, the deep waters are transported southwards by the DWBC, which presents a southward mass transport of -8.7 ± 3.8 Sv at 24°S and -13.9 ± 3.0 Sv at 34.5°S. At 24°S, the GLORYS output presents a stronger DWBC poleward mass transport (-19.1 Sv) than the inverse model. While at 34.5°S, neither of the two ocean models properly represents the interior circulation in the deep layers, but both display the intense poleward DWBC (-13.4 Sv in GLORYS and -13.2 Sv in ECCO). Adjacent to the DWBC, we find a northward transport of 6.4 ± 2.7 Sv at 24°S and 3.0 ± 1.3 Sv at 34.5°S. Further, the interior NADW pathway, which originates close to the Vitória-Trindade Ridge

at about 20°S, extends eastward crossing the MAR between 20° and 25°S (Arhan et al., 2003; Garzoli et al., 2015; Speer et al., 1995; van Sebille et al., 2012), then it moves to the Cape Basin and flows southward across the African continental slope as a DEBC (Arhan et al., 2003; Palma & Matano, 2017; Stramma & England, 1999). In the eastern boundary, the deep waters are transported southward by the DEBC (-16.3 ± 4.7 Sv at 24°S and -15.1 ± 3.5 Sv at 34.5°S). For comparison, at 24°S, GLORYS presents a weaker DEBC (-6.8 Sv) than the inverse model, while at 34.5°S both GLORYS and ECCO have weaker transports than the inverse model (-6.0 and 1.4 Sv, respectively). At 10°W, the deep layers display a net eastward transport of 17.7 ± 1.1 Sv, with some 10 Sv recirculating between the eastern and western basins. An eastward transport is found close to 24°S (7.5 ± 4.4 Sv), reflecting the NADW pathway into the eastern basin between 20°S and 25°S previously described by Arhan et al. (2003) and Reid (1989).

In this study, we find a northward heat transport in the subtropical South Atlantic, both at 34.5°S (0.30 ± 0.05 PW) and 24°S (0.80 ± 0.05 PW), which reflects the equatorward mass transport in the warm upper layers. The northward heat transport in GLORYS is similar to our estimate at both latitudes (0.43 ± 0.26 PW and 0.71 ± 0.14 PW at 24°S and 34.5°S, respectively), while the heat transport in ECCO is similar at 34.5°S (0.34 ± 0.15 PW) but weaker at 24°S (0.44 ± 0.10 PW) than our inverse model results. The heat transport estimated at 34.5°S agrees with the 0.27 ± 0.10 PW estimated by Manta et al. (2021) using the same hydrographic section, the 0.49 ± 0.23 PW from altimetry data computed by Dong et al. (2015), the 0.5 ± 0.2 PW from acoustic inversion reported by Kersalé et al. (2021), as well as with the 0.42 ± 0.18 PW from numerical model data obtained by Perez et al. (2011). In the same way, our result at 24°S presents no significant differences from previous estimations with hydrographic data— 0.64 ± 0.18 PW (Fu, 1981) and 0.7 ± 0.1 PW (Bryden et al., 2011)—but is higher values than the 0.4 ± 0.1 PW estimated by Evans et al. (2017) and slightly higher than the 0.66 ± 0.07 PW reported by Caínzos et al. (2022). Some of these differences are likely the result of the differences in years and months when the cruises were carried out (Caínzos et al., 2022).

The negative freshwater flux at 24°S (-0.07 ± 0.02 FSv) and the positive freshwater transport at 34.5°S (0.18 ± 0.02 FSv) indicate a convergence of freshwater in the 24°S–34.5°S domain, pointing out that this is a region where evaporation predominates over precipitation. The freshwater transports from GLORYS present no significantly different values from the inverse model at both latitudes (-0.05 ± 0.07 FSv and 0.25 ± 0.11 FSv at 24°S and 34.5°S, respectively), while ECCO presents slightly higher (0.01 ± 0.05 FSv at 24°S) and weaker (0.07 ± 0.07 FSv at 34.5°S) freshwater transports than the inverse model. Our result at 24°S agrees with the weak northward freshwater transport (0.01 ± 0.09 FSv) obtained by Caínzos et al. (2022) using WOCE and GO-SHIP data for the period 2010–2019. The freshwater flux obtained at 34.5°S is moderately lower than the freshwater transport of 0.23 ± 0.02 Sv obtained by Manta et al. (2021) at this same latitude.

The comparison of the circulation patterns as deduced from the inverse model with two different OGCM (ECCO and GLORYS) suggests that these ocean models are useful to study these sections in the upper layers ($\gamma^{\theta} < 27.58$ kg/m³, 1,140 m depth) with some differences in the estimated boundary currents. However, the ECCO and GLORYS patterns of circulation in the deep and, especially, bottom layers ($\gamma^{\theta} > 27.58$ kg/m³) do not properly resemble the circulation pattern of the hydrographic data at 24°S and 34.5°S in the Atlantic Ocean. The comparison of the heat and freshwater transports from the inverse model with the OGCM suggests that ECCO presents noticeable differences from our results, but GLORYS can be useful for determining the direction and strength of these deep ocean fluxes.

Our inverse model results show an AMOC strength of 17.5 ± 0.9 Sv at 24°S and 14.8 ± 1.0 Sv at 34.5°S. The AMOC strength at 24°S agrees fairly well with previous estimates at 24°S by Evans et al. (2017) (20.2 ± 2.0 Sv), and Bryden et al. (2011) ($21.5/16.5$ Sv in 2009/1983). Furthermore, our estimate of the AMOC strength at 34.5°S agrees well with earlier estimates at this latitude, 15.6 ± 1.4 Sv (Manta et al., 2021), 17.3 ± 5.0 Sv (Kersalé et al., 2021), 14.7 ± 8.3 Sv (Meinen et al., 2018), 15.6 ± 3.1 Sv (Perez et al., 2011), and 18.1 ± 2.3 Sv (Garzoli et al., 2013). However, it is weaker than transports obtained by Dong et al. (2015) and Majumder et al. (2016), 19.5 ± 3.5 Sv and 20.7 ± 4.1 Sv, respectively. The weaker upper AMOC strength and heat transport at 34.5°S as compared with 24°S could be partly explained by the intense southward transport of the Brazil Current (-16.6 ± 1.3 Sv at 34.5°S and -7.3 ± 0.9 Sv at 24°S) during the period of this hydrographic cruise (Kersalé et al., 2019; Manta et al., 2021). Furthermore, mesoscale eddies also probably play a role in upper limb transport, as the mesoscale activity at 34.5°S is higher than at 24°S (Laxenaire et al., 2018).

Our inverse box model has provided a detailed view of the South Atlantic circulation by estimating the different ocean current transports at each layer set through 24°S and 34.5°S, as well as over the MAR between these two latitudes. The transports in the upper layers are consistent with the course of the subtropical South Atlantic

anticyclonic gyre and the northwest route of the Benguela Current. The deep waters show the southward flow of the DWBC and DEBC, together with an eastward interbasin flow at the northern stations (close to 24°S) of the 10°W section, and different recirculation routes linking both basins. The abyssal layers exhibit northward mass transports through the Argentina and Cape basins, before the latest returns southward in the ocean interior, with no flow crossing above the MAR. Our results have also confirmed the characteristic northward heat transport across the subtropical South Atlantic Ocean, as well as the dominance of evaporation over precipitation.

Appendix A: Inverse Box Model

The absolute geostrophic velocity (v_a) for a given station pair, as a function of depth (z), is the summation of the relative velocity (v) and the velocity (b) at the reference level:

$$v_a(z) = v(z) + b$$

The inverse model finds the optimal solution for b at each station pair. First, the mass conservation is applied to the entire water column:

$$\iint \rho v_a dS = 0 \quad (\text{A.1a})$$

$$\iint \rho(v + b) dS = 0 \quad (\text{A.1b})$$

$$\sum_{j=1}^N \sum_{q=1}^Q \rho_{jq}(v_{jq} + b_j) a_{jq} = 0 \quad (\text{A.1c})$$

where the area integral dS is over the entire section area, a_{jq} is the area for each station pair j and isoneutral layer q . In Equation A.1 and the next equations, the term $\rho_{jq} v_{jq}$ is first summed over each 2 dbar interval within layer q . When mass transport is constrained to a particular non-zero value, M , Equation A.1c becomes:

$$\sum_{j=1}^N \sum_{q=1}^Q \rho_{jq}(v_{jq} + b_j) a_{jq} = M \quad (\text{A.1d})$$

where M is the mass transport constraint including the Bering Imbalance, and the limits for layers and station pairs are related to the constraint (Table 1). The total mass conservation is not exact because of the noise from eddies, internal waves, aliasing, measurements errors, etc.:

$$\sum_{j=1}^N \sum_{q=1}^Q \rho_{jq} b_j a_{jq} + n_{\text{Total}} = - \sum_{j=1}^N \sum_{q=1}^Q \rho_{jq} v_{jq} a_{jq} + M_{\text{Total}} \quad (\text{A.2})$$

where n_{Total} is the noise.

The following equations are obtained considering mass conservation in each layer q :

$$\sum_{j=1}^N \rho_{jq} b_j a_{jq} + n_q = - \sum_{j=1}^N \rho_{jq} v_{jq} a_{jq} + M_q \quad q = 1, 2, \dots, Q \quad (\text{A.3})$$

where M_q is the layer transport constraint and n_q is the layer noise. Next, this equation is written as:

$$\sum_{j=1}^N e_{jq} b_j + n_q = -y_q \quad q = 1, 2, \dots, Q \quad (\text{A.4})$$

where:

$$e_{jq} = \rho_{jq} a_{jq}$$

$$y_q = \sum_{j=1}^N \rho_{jq} v_{jq} a_{jq} - M_q \quad (\text{A.5})$$

The matrix equation is rewritten as:

$$\mathbf{A}\mathbf{b} + \mathbf{n} = -\mathbf{Y} \quad (\text{A.6})$$

where \mathbf{b} is a $N \times 1$ vector of the unknowns (reference velocities and adjustment of the Ekman transport), \mathbf{A} is a $(Q + 1) \times N$ matrix, \mathbf{n} is a $(Q + 1) \times 1$ vector, and \mathbf{Y} is a $(Q + 1) \times 1$ vector of values calculated from the CTD data and the externally imposed mass transports. (Q is for the equations for each layer and the +1 is the equation for conservation of the whole water column.)

The Ekman transport is included in the first layer, leading to the following system:

$$\begin{pmatrix} e_{11} & \dots & e_{1n} & 1 \\ e_{21} & & e_{2n} & 0 \\ \vdots & \ddots & \vdots & \vdots \\ e_{q,1} & \dots & e_{q,n} & 0 \\ e_{q+1,1} & & e_{q+1,n} & 1 \end{pmatrix} \begin{pmatrix} b_1 \\ \vdots \\ b_n \\ \Delta T_{\text{EK}} \end{pmatrix} = \begin{pmatrix} y_1 + T_{\text{EK}} \\ y_2 \\ \vdots \\ y_q \\ y_{q+1} + T_{\text{EK}} \end{pmatrix}$$

To solve this matrix, the Gauss-Markov estimator is applied (Wunsch, 1996), as in Hernández-Guerra and Talley (2016).

For this inverse model, 15 different constraints are applied, corresponding to the mass conservation in each Box (three enclosed regions), plus 12 additional mass transport constraints based on previous studies of the boundary currents and deep flows (listed in Table 1).

Conflict of Interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: Cristina Arumí-Planas reports financial support was provided by Agencia Canaria de Investigación, Innovación y Sociedad de la Información (ACIISI). Cristina Arumí-Planas reports a relationship with Agencia Canaria de Investigación, Innovación y Sociedad de la Información (ACIISI) that includes: employment.

Data Availability Statement

The wind data were collected from NCEP Reanalysis Derived data can be found at <http://www.esrl.noaa.gov/psd/>. Hydrographic data were collected from the Carbon Hydrographic Data Office (CCHDO) website in the frame of International WOCE and GO-SHIP projects (<https://cchdo.ucsd.edu/>). The hydrographic data at 34.5°S were collected during the expedition of the German Research Vessel *Maria S. Merian* (MSM60) conducted in the summer of 2017 (Karstensen, 2020) can be found at <https://doi.org/10.1594/PANGAEA.915898>. The hydrographic data at 24°S were collected as part of the Ocean Regulation of Climate by Heat and Carbon Sequestration and Transports (ORCHESTRA) program funded by the UK Natural Environment Research Council (NERC, Grant NE/N018095/1). ECCO data are available for download at <https://ecco.jpl.nasa.gov/>. GLORYS data are available for download at <https://resources.marine.copernicus.eu/>. The satellite altimetry data were collected from the Aviso database (<http://las.aviso.oceanobs.com>).

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