Measurement of the Absolute Branching Fractions for $D_s^- \rightarrow \ell^- \nu_\ell$ and Extraction of the Decay Constant $f_{D_s}$


(The BABar Collaboration)

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The absolute branching fractions for the decays $D_s^- \to \ell^- \bar{\nu}_\ell$ ($\ell = e, \mu, \text{or } \tau$) are measured using a data sample corresponding to an integrated luminosity of 521 fb$^{-1}$ collected at center of mass energies near 10.58 GeV with the BABAR detector at the PEP-II $e^+e^-$ collider at SLAC. The number of $D_s^-$ mesons is determined by reconstructing the recoiling system $DKX_\gamma$ in events of the type $e^+e^- \to DKX_\gamma$, where $D_s^+ \to D^-\gamma$ and $X$ represents additional pions from fragmentation. The $D_s^- \to \ell^- \bar{\nu}_\ell$ events are detected by full or partial reconstruction of the recoiling system $DKX_\gamma$. The branching fraction measurements are combined to determine the $D_s^-$ decay constant $f_{D_s} = (258.6 \pm 6.4 \pm 7.5)$ MeV, where the first uncertainty is statistical and the second is systematic.

PACS numbers: 13.20.Fc, 12.38.Gc

The $D_s^-$ meson can decay purely leptonically via annihilation of the $\bar{c}$ and $s$ quarks into a $W^-$ boson [1]. In the Standard Model (SM), the leptonic partial width $\Gamma(D_s^+ \to \ell^- \bar{\nu}_\ell)$ is given by

$$\Gamma = \frac{G_F^2 M_{D_s}^3}{8\pi} \left( \frac{m_\ell}{M_{D_s}} \right)^2 \left( 1 - \frac{m_\ell^2}{M_{D_s}^2} \right)^2 |V_{cs}|^2 f_{D_s}^2,$$  

where $M_{D_s}$ and $m_\ell$ are the $D_s^-$ and lepton masses, re-
respectively, $G_F$ is the Fermi coupling constant, and $V_{cs}$ is an element of the Cabibbo-Kobayashi-Maskawa quark mixing matrix. These decays provide a clean probe of the pseudoscalar meson decay constant $f_{D_s}$.

Within the SM, $f_{D_s}$ has been predicted using several methods \cite{2}; the most precise value by Follana et al. uses unquenched LQCD calculations and gives $f_{D_s} = (241 \pm 3) \text{ MeV}$. Currently, the experimental values are significantly larger than this theoretical prediction. The Heavy Flavor Averaging Group combines the CLEO-c, Belle and $BaBar$ measurements and reports $f_{D_s} = (254.6 \pm 5.9) \text{ MeV}$ \cite{3}. Models of new physics (NP), including a two-Higgs doublet \cite{4} and leptoquarks \cite{5}, may explain this difference. In addition, $f_{D_s}$ measurements provide a cross-check of QCD calculations which predict the impact of NP on $B$ and $B_s$ meson decay rates and mixing. High precision determinations of $f_{D_s}$, both from experiment and theory, are necessary in order to discover or constrain effects of NP.

We present absolute measurements of the branching fractions of leptonic $D_s^-$ decays with a method similar to the one used by the Belle Collaboration \cite{6,7}. An inclusive sample of $D_s^-$'s is obtained by reconstructing the rest of the event in reactions of the kind $e^+e^- \rightarrow car{c} \rightarrow D_0^{*+}D_0^{-}$, where $D_s^+ \rightarrow D^- \gamma$. Here, $D$ represents a charm hadron ($D^0$, $D^+$, $D^*$, or $\Lambda^+_c$), $K$ represents the $K^0$ or $K^+$ required to balance strangeness in the event, and $X$ represents additional pions produced in the $car{c}$ fragmentation process. When the charm hadron is a $\Lambda^+_c$, an additional anti-proton is required to assure baryon number conservation. No requirements are placed on the decay products of the $D_s^-$ so that the selected events correspond to an inclusive sample. The 4-momentum of each $D_s^-$ candidate, $p_s$, is measured as the difference between the momenta of the colliding beam particles and the fully reconstructed $DKX\gamma$ system: $p_s = p_{e+} + p_{e-} − p_D − p_K − p_X − p_p$. The inclusive sample of $D_s^-$'s is obtained from a binned fit to the distribution in the recoil mass $m_r(DKX\gamma) = \sqrt{p_s^2}$. Within this inclusive sample, we determine the fraction of events corresponding to $D_s \rightarrow \mu^−\nu_\mu$, $D_s \rightarrow e^−\nu_e$, and $D_s \rightarrow \tau^−\bar{\nu}_\tau$ decays. In the SM, ratios of the branching fractions for these decays are $e^-\bar{\nu}_e : \mu^−\nu_\mu : \tau^−\bar{\nu}_\tau = 2 \times 10^{-5}$: $1 : 10$, due to helicity and phase-space suppression. The analysis is based on a data sample of $521 \text{ fb}^{-1}$, which corresponds to about $677 \text{ million } e^+e^- \rightarrow c\bar{c}$ events, recorded near $\sqrt{s} = 10.58 \text{ GeV}$ by the $BaBar$ detector at the SLAC PEP-II asymmetric-energy collider. The detector is described in detail in Refs. \cite{3,5}. Charged-particle momenta are measured with a 5 layer, double-sided silicon vertex tracker (SVT) and a 40 layer drift chamber (DCH) inside a 1.5 T superconducting solenoidal magnet. A calorimeter consisting of 6580 CsI(Tl) crystals (EMC) is used to measure electromagnetic energy. Measurements from a ring-imaging Cherenkov radiation detector, and of specific ionization $(dE/dx)$ in the SVT and DCH, provide particle identification (PID) of charged hadrons. Muons are mainly identified by the instrumented magnetic flux return, and electrons are identified using EMC and $dE/dx$ information. The analysis uses Monte Carlo (MC) events generated with EvtGen and JETSET \cite{10,11} and passed through a detailed GEANT4 \cite{12} simulation of the detector response. Final state radiation from charged particles is modeled by PHOTOS \cite{13}. Samples of MC events for $e^+e^-$ annihilation to $q\bar{q}$ ($q = u, d, s, c, b$) (generic MC) are used to develop methods to separate signal events from backgrounds. In addition, we use dedicated samples for $D_s^-$ production and leptonically decaying signal MC to determine reconstruction efficiencies and the distributions needed for the extraction of the signal decays.

We reconstruct $D$ candidates using the following 15 modes: $D^0 \rightarrow K^-\pi^+(\pi^0)$, $K^-\pi^+\pi^-\pi^+(\pi^0)$, or $K^0_s\pi^+\pi^-\pi^+(\pi^0)$; $D^+ \rightarrow K^-\pi^+\pi^+(\pi^0)$, $K^0_s\pi^+\pi^-\pi^+(\pi^0)$, or $K^0_s\pi^+\pi^-\pi^+\pi^+(\pi^0)$; and $\Lambda^+_c \rightarrow pK^+\pi^+(\pi^0)$, $pK^0_s\pi^+$, or $pK^0_s\pi^-\pi^+\pi^+(\pi^0)$. All $\pi^0$'s and $K^0_s$'s used in this analysis are reconstructed from two photons or two oppositely charged pions, respectively, and are kinematically constrained to their nominal mass values \cite{14}. The $K^0_s$ in a $D$ candidate must have a flight distance from the $e^+e^-$ interaction point (IP) greater than 10 times its uncertainty. For each $D$ candidate we fit the tracks to a common vertex, and for each mode, we determine the mean and $\sigma$ of the reconstructed signal mass distribution from a fit to data. We then simultaneously optimize a set of selection criteria to maximize $S/\sqrt{S + B}$, where $S$ refers to the number of $D$ candidates after subtraction of the background $B$ within a mass window defined about the signal peak. Where $B$ is estimated from the sideband regions of the mass distribution. In addition to the size of the mass window, several other properties of the $D$ candidate are used in the optimization: the center-of-mass (CM) momentum of the $D$, PID requirements on the tracks, the probability of the $D$ vertex fit, and the minimum lab energy of $\pi^0$ photons. The CM momentum must be at least 2.35 GeV/c in order to remove $B$ meson backgrounds. After the optimization the relative contributions to the total signal sample are 74.0% $D^0$, 22.6% $D^+$, and 3.4% $\Lambda^+_c$. Multiple candidates per event are accepted.

To identify $D$ mesons originating from $D^*$ decays we reconstruct the following decays: $D^{∗+} \rightarrow D^0\pi^+$, $D^{0\pi^0} \rightarrow D^0\pi^0$, $D^{+\pi^0} \rightarrow D^+\pi^0$, and $D^{0\pi^0} \rightarrow D^0\gamma$. The photon energy in the laboratory frame is required to exceed 30 MeV for $\pi^0 \rightarrow \gamma\gamma$ and 250 MeV for $D^{0\pi^0} \rightarrow D^0\gamma$ decays. The $\gamma\gamma$ invariant mass must be within 3 sigma of the $\pi^0$ peak. For all $D^*$ decays, the mass difference $m(D^*) - m(D)$ is required to be within 2.5 sigma of the peak value.

A $K$ candidate is selected from tracks not overlapping with the $D$ candidate. PID requirements are applied to each $K^+$ candidate, and a $K^0_S$ candidate must have a flight distance greater than 5 times its uncertainty.

An $X$ candidate is reconstructed from the remaining
\(\pi^+\)'s and \(\pi^0\)'s not overlapping with the \(DK\) candidate. In the laboratory frame, a \(\pi^\pm\) must have a momentum greater than 100 MeV/c and each photon from a \(\pi^0\) decay must have energy greater than 100 MeV. We reconstruct X modes without \(\pi^0\)'s with up to three charged pions, and modes with one \(\pi^0\) with up to two charged pions. The total charge of the X candidate is not checked at this stage.

Finally, we select a \(\gamma\) candidate for the signal \(D_s^-\) decay by requiring a minimum energy of 120 MeV in the laboratory frame, and an angle with respect to the direction of the \(D\) candidate momentum in the CM frame greater than 90 degrees. This photon cannot form a \(\pi^0\) or \(\eta\) candidate when combined with any other photon in the event. In addition, the cluster must pass tight requirements on the shower shape in the EMC and a separation of at least 15 cm from the impact of any charged particle or the position of any other energy cluster in the EMC.

Only \(DKX\gamma\) candidates with a total charge of \(\pm\)1 are selected to form a right-sign (RS) sample, from which we extract the \(D_s^-\) signal yield. The charm and strange quark content of the \(DKX\) must be consistent with recoiling from a \(D^-\). The RS sample includes candidates for which consistency cannot be determined due to the presence of a \(K^0\). We define a wrong-sign (WS) sample with the same charge requirement above, but by requiring that the charm and strange quark content of the \(DKX\) be consistent with a recoil from a \(D^+\). The WS sample contains a small fraction of signal events due mainly to \(DKX\) candidates for which the total charge is misconstructed. The generic MC shows that the WS sample includes a small fraction of signal events due mainly to multiple photons that can be associated with the \(D_s^-\) decay. In order to properly count events in the fits described below, we assign weight \(1/n\) to each \(D_s^-\) candidate, where \(n\) is the number of \(D_s^-\) candidates in the event.

We define \(n_R^X\) and \(n_w^X\) to be the number of reconstructed and true pions in the X system, respectively. The efficiency for reconstructing signal events depends on \(n_R^X\). However, the \(n_R^X\) distribution is expected to differ from the MC simulation due to inaccurate fragmentation functions used by JETSET. To correct for these inaccuracies, we extract the \(D_s^-\) signal yields from a fit to the two-dimensional histogram of \(m_s(DKX\gamma)\) versus \(n_R^X\). The PDF for the signal distribution is written as a weighted sum of the MC distributions for \(j = n_R^X\).

\[
S(m, n_R^X) = \sum_{j=0}^{6} w_j S_j(m, n_R^X).
\]  

The weights \(w_j\) have to be extracted from this fit. To constrain the shape of the weights distribution, we introduce the parameterization \(w_j \propto (j - \alpha)^3 e^{-\beta j}\) together with the condition \(\sum_j w_j = 1\). This parametrization is motivated by the distribution of weights in the MC. The value \(\alpha = -1.32\) is taken from a fit to MC, whereas \(\beta\) and \(\gamma\) are determined from the fit to data.

The RS and WS samples are fitted simultaneously to determine the background. The fit to the WS sample uses a signal component similar to that used in the RS fit, except that due to the small signal component, the weights are fixed to the MC values and the signal yield is determined from MC to be 11.8% of the RS signal yield. The shapes remaining after the signal component is removed from the WS sample, \(B_i(m) (i = n_R^X)\), are used to model the RS backgrounds. A shape correction is applied to \(B_0\) to account for a difference observed in the MC. We add these components with free coefficients \((b_i)\) to construct the total RS background shape: \(B(m, n_R^X) = \sum_{i=0}^{3} b_i B_i(m) \delta(i - n_R^X)\). Thus in addition to \(\beta, \gamma\), and the total signal yield, there are 3 additional free parameters \(b_i (i = 0, 1, 2)\) in the RS fit.

Figure 1 shows the data and the results of the fit, and Fig. 2 shows the total RS and WS samples. The fit finds a minimum \(\chi^2/ndf = 216/182\) and the fitted parameter values are \(\beta = 0.27 \pm 0.17\) and \(\gamma = 0.28 \pm 0.07\). These are different from the MC values \(\beta = 3.38\) and \(\gamma = 1.15\) since there are more events at low values of \(n_R^X\) than in the MC.

Having constructed the inclusive \(D_s^-\) sample, we proceed to the selection of \(D_s^- \rightarrow \mu^- \bar{\nu}_\mu\) events within that sample. We use the \(m_s(DKX\gamma)\) range between 1.934 and 2.012 GeV/c\(^2\), which contains an inclusive \(D_s^-\) yield \((N_{D_s^-})\) of \((67.2 \pm 1.5) \times 10^3\). We require that there be exactly one more charged particle in the remainder of the event, and that it be identified as a \(\mu^+\). In addition, we require that the extra neutral energy in the event, \(E_{\text{extra}}\), be less than 1.0 GeV; \(E_{\text{extra}}\) is defined as the total energy of EMC clusters with individual energy greater than 30 MeV and not overlapping with the \(DKX\gamma\) candidate. Since the only missing particle in the event should be the neutrino we expect the distribution of \(E_{\text{extra}}\) to peak at zero for signal events. We determine the 4-momentum...
of the $\bar{\nu}_\mu$ candidate through a kinematic fit similar to that described earlier in the determination of the $D_s^-$ 4-momentum, but with the $\mu^-$ included in the recoil system. In this fit we constrain the mass recoiling against the $DKX\gamma$ system to the nominal value for the $D_s^-$ [14]. To extract the signal yield, we perform a binned maximum likelihood fit to the $m_r(DKX\gamma\mu)$ distribution using a signal PDF determined from reconstructed signal MC events that contain the signal decay chain $D_s^- \rightarrow D_s^-\gamma$ with $D_s^- \rightarrow \mu^-\bar{\nu}_\mu$. The background PDF is determined from the reconstructed generic MC events with signal events removed. The fit is shown in Fig. 3(a), and the number of signal events extracted, $N_{\mu\mu}$, is listed in Table I.

The $D_s^- \rightarrow \mu^-\bar{\nu}_\mu$ branching fraction is obtained from:

$$B(D_s^- \rightarrow \mu^-\bar{\nu}_\mu) = \frac{N_{\mu\mu}}{N_{D_s^-} \sum_{j=0}^{6} w_j \varepsilon_{D_s^-}^{j} \varepsilon_{\mu\mu}^{j}} = \frac{N_{\mu\mu}}{N_{D_s^-} \varepsilon_{\mu\mu}},$$

(3)

where the $D_s^- \rightarrow \mu^-\bar{\nu}_\mu$ reconstruction efficiency, $\varepsilon_{\mu\mu}$, is determined using the signal MC sample with $j = n_X$, and $\varepsilon_{D_s^-}^j$ is the corresponding inclusive $D_s^-$ reconstruction efficiency. The efficiency ratios $\varepsilon_{\mu\mu} / \varepsilon_{D_s^-}$ decrease from 87% to 33% as $j$ increases from 0 to 6. The weighted average, $\varepsilon_{\mu\mu}$, and the value determined for $B(D_s^- \rightarrow \mu^-\bar{\nu}_\mu)$ are listed in Table I. The statistical uncertainty includes contributions from $N_{D_s^-}$, $\varepsilon_{\mu\mu}$, and $N_{\mu\mu}$ (with correlations taken into account). The systematic uncertainty is determined by varying the parameter values in the inclusive $D_s^-$ fit which were fixed to MC values, by varying the resolution on the $D_s^-$ signal PDF (for both mass and $n_X$), and by estimating how well the MC models the long tail of the signal PDF observed in Figs. 1 and 2. Uncertainties are assigned for possible mismodeling of the signal or background $m_r^2(DKX\gamma\mu)$ distributions due to possible differences in the position or resolution of the mass distribution, or mismodelings of different $D_s^-$ decays. Uncertainties in the efficiencies due to tracking and $\mu^-$ identification are included. This measurement supercedes our previous result [12].

Using a procedure similar to that for $D_s^- \rightarrow \mu^-\bar{\nu}_\mu$ we search for $D_s^- \rightarrow e^-\bar{\nu}_e$ events. The fit to the $m_r^2(DKX\gamma e)$ distribution, shown in Fig. 3(b), gives a signal yield $N_{ee}$ consistent with 0. We obtain an upper limit on $B(D_s^- \rightarrow e^-\bar{\nu}_e)$ by integrating a likelihood function from 0 to the value of $B(D_s^- \rightarrow e^-\bar{\nu}_e)$ corresponding to 90% of the integral from 0 to infinity. The like-
likelihood function consists of a Gaussian function written in terms of the variable $BN_{D_s, \bar{\varepsilon}_{ee}}$ with mean and sigma set to $N_{\bar{\varepsilon}_{ee}}$ and its total uncertainty, respectively. To account for the uncertainties on $N_{D_s, \bar{\varepsilon}_{ee}}$, the main Gaussian is convolved with another Gaussian function centered at the measured value of $N_{D_s, \bar{\varepsilon}_{ee}}$ with sigma set to the $N_{D_s, \bar{\varepsilon}_{ee}}$ total uncertainty. The value obtained for the upper limit is listed in Table I.

We find $D_\tau^- \rightarrow \tau^- \bar{\nu}_\tau$ decays within the sample of inclusively reconstructed $D_\tau^-$ events by requiring exactly one more track identified as an $e^-$ or $\mu^-$, from the decay $\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau$ or $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$. We remove events associated with $D_\tau^- \rightarrow \mu^- \bar{\nu}_\mu$ decays by requiring $m_T^2(DKX) > 0.5$ GeV$^2/c^4$. Since $D_\tau^- \rightarrow \tau^- \bar{\nu}_\tau$ events contain more than one neutrino we use $E_{\text{extra}}$ to extract the yield of signal events; these are expected to peak towards zero, while the backgrounds extend over a wide range. The signal and background PDFs are determined from reconstructed MC event samples. The fits are shown in Figs. 3(c) and 3(d); the signal yields are listed in Table I. We determine $B(D_\tau^- \rightarrow \tau^- \bar{\nu}_\tau)$ from the $e^-$ and $\mu^-$ samples using Eq. (3) and accounting for the decay fractions of the $\tau^- [14]$. The values obtained are listed in Table I and are consistent with the previous Babar result [16]. The error-weighted average $B(D_\tau^- \rightarrow \tau^- \bar{\nu}_\tau) = (5.00 \pm 0.35(\text{stat}) \pm 0.49(\text{syst})) \times 10^{-2}$, the weights used in the average are computed from the total error matrix and account for correlations. As a test of lepton flavor universality we determine the ratio $B(D_\tau^- \rightarrow \tau^- \bar{\nu}_\tau)/B(D_\tau^- \rightarrow \mu^- \bar{\nu}_\mu) = (8.27 \pm 0.77(\text{stat}) \pm 0.85(\text{syst}))$, which is consistent with the SM value of 9.76.

As a cross-check of this analysis method, we measure the branching fraction for the hadronic decay $D_\tau^- \rightarrow K^- \pi^+ \pi^-$. Within the inclusive $D_\tau^-$ sample, we require exactly three charged particle tracks that do not overlap with the $DKX\gamma$ candidate. PID requirements are applied to the kaon candidates. The mass of the $K^- \pi^+ \pi^-$ system must be between 1.93 and 2.00 GeV/$c^2$, and the CM momentum above 3.0 GeV/$c$. We combine the $K^- \pi^+ \pi^-$ system with the signal $\gamma$ and extract the signal yield from the $m(KK\pi\gamma)$ distribution. For this mode we choose the loose selection $m_T(DKX) > 1.82$ GeV/$c^2$, because this variable is correlated with $m(KK\pi\gamma)$; this corresponds to an inclusive $D_\tau^-$ yield of $N_{D_\tau} = (108.9 \pm 2.4) \times 10^3$. We model the signal distribution using reconstructed MC events that contain the decay chain $D_\tau^- \rightarrow D_\pi^- \gamma$ and $D_\pi^- \rightarrow K^- K^+ \pi^-$. In the generic MC and a high statistics control data sample (for which the inclusive reconstruction was not applied) the background was found to be linear in $m(KK\pi\gamma)$. From a fit to the $m(KK\pi\gamma)$ distribution, shown in Fig. 3(c), we determine a signal yield of $N_{KK\pi\gamma} = 1866 \pm 40$ events.

We compute the $D_\tau^- \rightarrow K^- K^+ \pi^-$ branching fraction using Eq. (3). The efficiency for reconstructing signal events is determined from the signal MC in three regions of the $K^- K^+ \pi^-$ Dalitz plot, corresponding to $\phi \pi^-, K^- \pi^+ 0^-$, and the rest. A variation of $\sim 8$% is observed across the Dalitz plot, leading to a correction factor of 1.016 on $e^j_{KK\pi\gamma}$. The weighted efficiency ratio is found to be $e_{KK\pi\gamma} = 29.5\%$, and we obtain $B(D_\tau^- \rightarrow K^- K^+ \pi^-) = (5.78 \pm 0.20(\text{stat}) \pm 0.30(\text{syst}))\%$. The first uncertainty accounts for the statistical uncertainties associated with the inclusive $D_\tau^-$ sample and $N_{KK\pi\gamma}$. The second accounts for systematic uncertainties in the signal and background models, and the inclusive $D_\tau^-$ sample, as well as the reconstruction and PID selection of the $K^- K^+ \pi^-$ candidates. This result is consistent with the value $(5.50 \pm 0.23 \pm 0.16)\%$ measured by CLEO-c [18].

Using the leptonic branching fractions measured above, we determine the $D_\tau^-$ decay constant using Eq. (11) and the known values for $m_\tau$, $m_D$, $|V_{ud}|$ (we assume $|V_{us}| = |V_{ud}|$), and $D_\tau^-$ lifetime obtained from Ref. [14]. The $f_{D_\tau^-}$ values are listed in Table I; the systematic uncertainty includes the uncertainties on these parameters (1.9 MeV). Finally, we obtain the error-weighted average $f_{D_\tau^-} = (258.6 \pm 6.4(\text{stat}) \pm 7.5(\text{syst}))$ MeV.

In conclusion, we use the full dataset collected by the Babar experiment to measure the branching fractions for the leptonic decays of the $D_\tau^-$ meson. The measured value of $f_{D_\tau^-}$ is 1.8 standard deviations larger than the theoretical value [2], consistent with the measurements by Belle and CLEO-c [4, 19]. Further work on this subject is necessary to validate the theoretical calculations or to shed light on possible NP processes.

We are grateful for the excellent luminosity and machine conditions provided by our PEP-II colleagues, and for the substantial dedicated effort from the computing organizations that support Babar. The collaborating institutions wish to thank SLAC for its support and

<table>
<thead>
<tr>
<th>Decay</th>
<th>$\varepsilon$</th>
<th>Signal Yield</th>
<th>$B(D_\tau^- \rightarrow $ $\ell^- \bar{\nu}_\ell$)</th>
<th>$f_{D_\tau^-}$ (MeV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D_\tau^- \rightarrow e^- \bar{\nu}_e$</td>
<td>70.5%</td>
<td>$6.1 \pm 2.2 \pm 5.2$</td>
<td>$&lt; 2.3 \times 10^{-4}$ at 90% C.L.</td>
<td></td>
</tr>
<tr>
<td>$D_\tau^- \rightarrow \mu^- \bar{\nu}_\mu$</td>
<td>67.7%</td>
<td>$275 \pm 17$</td>
<td>$(6.02 \pm 0.38 \pm 0.34) \times 10^{-3}$</td>
<td>$265.7 \pm 8.4 \pm 7.7$</td>
</tr>
<tr>
<td>$D_\tau^- \rightarrow \tau^- \bar{\nu}_\tau$ ($\tau^- \rightarrow e^- \bar{\nu}<em>e \nu</em>\tau$)</td>
<td>61.6%</td>
<td>$408 \pm 42$</td>
<td>$(5.07 \pm 0.52 \pm 0.68) \times 10^{-2}$</td>
<td>$247 \pm 13 \pm 17$</td>
</tr>
<tr>
<td>$D_\tau^- \rightarrow \tau^- \bar{\nu}<em>\tau$ ($\tau^- \rightarrow \mu^- \bar{\nu}</em>\mu \nu_\tau$)</td>
<td>59.5%</td>
<td>$340 \pm 32$</td>
<td>$(4.91 \pm 0.47 \pm 0.54) \times 10^{-2}$</td>
<td>$243 \pm 12 \pm 14$</td>
</tr>
</tbody>
</table>

TABLE I: Average efficiency ratios, signal yields, branching fractions, and decay constants for the leptonic $D_\tau^-$ decays. The first uncertainty is statistical and the second is systematic.
kind hospitality. This work is supported by DOE and NSF (USA), NSERC (Canada), CEA and CNRS-IN2P3 (France), BMBF and DFG (Germany), INFN (Italy), FOM (The Netherlands), NFR (Norway), MES (Russia), MICINN (Spain), STFC (United Kingdom). Individuals have received support from the Marie Curie EIF (European Union), the A. P. Sloan Foundation (USA) and the Binational Science Foundation (USA-Israel).

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¶ Also with Università di Sassari, Sassari, Italy
[1] Use of charge conjugate reactions is implied in this paper.
[16] J.P. Lees et al. (BaBar Collab.), arXiv:1003.3063v2 (submitted to PRD-RC) (2010). Due to differences in the event reconstruction and analysis method we estimate this measurement to have a statistical error which is about 40% correlated with the present measurement and an uncorrelated systematic error.