One-Electron Model for the Electronic Response of Metal Surfaces to Subfemtosecond Photoexcitation

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The recent work of Cavalieri \textit{et al.} [Nature (London) \textbf{449}, 1029 (2007)] has provided the first experimental observation of electron dynamics at metal surfaces in the subfemtosecond range. We explain the experimental findings using a full time-dependent approach within a one-dimensional model that includes the main ingredients of the short time physics involved in the experiment.

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The study of real-time dynamics of electrons in condensed-matter systems is pertinent for progress in nanotechnology. The electron processes in nanosystems are very fast and their investigation in real time requires the application of experimental tools with subfemtosecond time resolution. Recently the first experiment with streaking observation of electron dynamics in metal in the subfemtosecond range was performed [1]. In this experiment, the surface of the solid was illuminated by two pulses. The first pulse was a short extreme ultraviolet (XUV) pulse with the frequency $\omega_X$ of about 90 eV and duration (FWHM for the field envelope) $\tau_X$ of about 0.3 fs. Intensity of this pulse is quite low. Another pulse was a relatively strong (power $W$ in $10^9$–$10^{10}$ W/cm\textsuperscript{2} range) near-infrared (NIR) laser pulse with the frequency $\omega_L$ about 1.5 eV and with the full duration $\tau_L$ about 10 fs. The energy spectra of the electrons ejected from the localized $f$ state and delocalized $d$ band through the (110) surface of tungsten in the direction normal to this surface were measured. The time delay between the two pulses was varied in [1] and the energy spectra of the ejected electrons were monitored as a function of this delay. The energy acquired by the ejected electron from the NIF field depends on the time of the electron passage across the metal surface. Thus, measuring the dependence of the ejected electron energy spectrum on the time delay between the pulses, one can keep track of the process dynamics in the time domain; this is the idea of the “streaking camera” [2]. The streaking effect had been well established as an experimental tool, and a theory for the experiments with isolated inert-gas atoms had also been developed [3]. The first experiment on a metal surface [1] is a very important proof-of-principle experiment, in which a number of difficulties intrinsic for the streaking studies at the metal surfaces were overcome. Some preliminary theoretical studies [4,5] of nonstationary fast processes in metals have also been undertaken.

In [1], the experimental results were shown to be consistent with concepts derived from the static band structure. In the supplementary information to [1], the main approximations of the calculations were listed. A key issue remaining is whether the static band structures can be employed in this very dynamical process. Using a simple one-dimensional model that is fully time dependent, we show that for the small times there is no time for the group velocity in the final state to be established and therefore the picture of static band structure is not valid. We also find that the delay time arising from the different character (localized versus delocalized) of the initial state is in agreement with the experimental results [1].

The processes triggered by instantaneous excitation of an electron in solid are very complicated and a number of various mechanisms can be of paramount importance. First, electrons in the metal are moving in the field of the lattice. This could in principle change the group velocity of the excited electron packet inside the bulk, as was described in [1]. Second, a localized electron after its ejection leaves in the bulk a positively charged hole which is then screened by the itinerant electrons. Third, the ejected electrons suffer inelastic collisions with electrons of the metal. This determines the depth from which the ejected electrons can reach the surface without inelastic collisions and thus carry direct information on the processes in the bulk. Fourth, the normal component of the laser field decreases in the bulk abruptly to a very small value under the condition of the experiment [1]. This determines the peculiarity of streaking effect in the system considered.

Here we formulate a simple and versatile model which includes these essential features of the phenomenon and allows one to estimate the magnitudes of the possible effects and analyze the influence of the parameters of the system on the output. The purpose of this study is to compute the delay time dependence of the energy spectra of electron ejected from a given initial state in the metal.
Basically, two features are of importance in the theoretical investigation. First, the ejected electron moves in the lattice field, and this could produce some effect in the ejected electron spectra [1]. Another point of attention is related to screening of the streaking IR field in the solid. Considering the first effect, one has to keep in mind that the electrons of few tens eV energy, being ejected from deep layers, suffer inelastic collisions with other electrons. The corresponding mean free path (MFP) is about 5–7 Å [6]. Thus, experimentally, information can be obtained only on the events occurring in a very few external layers of the metal. On the other hand, variation in streaking for the electrons ejected from various layers can be observed only if the normal component of the streaking field inside the bulk is promptly screened to quite a small value and thus the IR field is not uniform. The frequency of the NIR laser, 1.5 eV, is lower than the plasmon frequency in metals and thus the screening length must be less than the MFP.

In our model, we consider a 1D slab of the metal of thickness \( L \) = 300 a.u. The time evolution of the ejected electron wave packet \( \Psi(z, t) \) is governed by the nonstationary Schrödinger equation (atomic units are used)

\[
\frac{i}{\hbar} \frac{\partial}{\partial t} \Psi(z, t) = \left( -\frac{1}{2} \frac{\partial^2}{\partial z^2} + \left[ U_s(z) - E \right] + U_h(z, t) - i\gamma(z) \right) \times \Psi(z, t) + E_L(z) \epsilon_L(t) \cos(\omega_L t + \phi) \Psi(z, t) + \hat{V}_X(z, t) \Phi_0(z), \quad z > -L.
\]

This equation is written within the rotating wave approximation for the weak XUV pulse (for some details, see [3]). The quantity \( E \) is the energy (with respect to the vacuum level) at the center of the energy spectrum of the ejected electron. It is a sum of the electron energy in the initial state, \( -|E_0| \), and the carrier frequency \( \omega_X \) of the XUV pulse. The wave function of the electron in the initial state is \( \Phi_0(z) \). The term \( \hat{V}_X(z, t) \Phi_0(z) \) in Eq. (1) describes the interaction of the XUV pulse with the initial electron state; it is taken in the length form \( \hat{V}_X(z, t) \Phi_0(z) = \epsilon_X(t) z \Phi_0(z) \). Here \( \epsilon_X(t) \) is an envelope of the electric field of the XUV pulse. We assume it to be Gaussian \( \epsilon_X(t) = \exp(-t - t_{\text{delay}})^2/\tau_X^2) \) with \( \tau_X = 125 \) a.u. FWHM = \( \tau_X = 0.21 \) fs. The \( E_L(z) \) in Eq. (1) describes the NIR laser electric field:

\[
E_L(z) = \begin{cases} 
\xi + (z - z_{\text{im}}) & z > z_{\text{im}} \\
\xi \exp((z - z_{\text{im}})/\xi) & z < z_{\text{im}},
\end{cases}
\]

with the screening length \( \xi = 4 \) a.u. [7]. The parameter \( z_{\text{im}} \) in Eq. (2) is a position of the image plane, it enters the parametrization of the pseudopotential \( U_s(z) \) [see [8], Eqs. (2)–(5)]. In the present case \( z_{\text{im}} = 2.105 \) a.u. In the experiment [1] the streaking field was incident on the surface at Brewster’s angle (\( \sim 75^\circ \)). Thus, the normal component of this field in the metal is about 16 times weaker than the incident field. In our model we set the streaking field in the metal equal to zero.

The envelope of the NIR pulse is taken as \( \epsilon_L(t) = 0.5 \epsilon_0 \{1 - \cos[\pi t/\tau_L]\} \) with the FWHM \( \tau_L = 5 \) fs and \( \omega_L = 1.6 \) eV, \( \phi = 0 \) in Eq. (1). The field strength \( \epsilon_0 \) is conventionally related to the intensity of the pulse \( W \). It was quite difficult to control the intensity of the NIR laser pulse in the experiment [1]. In the previous experiments in the gas phase, the intensity \( W \) was greater than \( 10^{13} \) W/cm\(^2\). In experiments with the solids the intensity is restricted by a number of requirements to be much smaller than in the gas phase. By comparing the experimental results with the results of our computation, we have estimated the intensity of the NIR laser field in the experiment [1] as \( W = 6 \times 10^9 \) W/cm\(^2\).

The (pseudo)potential \( U_s(z) \) in Eq. (1) mocks the interaction of an electron with a lattice in a finite metal. For this potential, we take the parametrization by Chulkov et al. [8] with the parameters corresponding to the Cu(111) surface. The function \( U_s(z, t) \) in Eq. (1) describes the interaction between the ejected electron and the hole left in the solid by this electron. We assume a static approximation for this potential as a screened softened Yukawa potential with the screening length \( \xi \), the same is in Eq. (2):

\[
U_s(z) = \exp(-|z - z_{\text{at}}|/\xi)/\sqrt{(z - z_{\text{at}})^2 + a_0^2},
\]

with \( a_0 = 0.4 \) a.u. Softening of this interaction allows us to apply in solving the nonstationary task a more advantageous fast-Fourier algorithm. Our study can adopt any given time-dependent screening of the hole. The damping function \( \gamma(z) \) in Eq. (1) is nonzero at \( z < z_{\text{im}} \), where \( \gamma(z) \) for the electron with energy \( E \) in the bulk is approximated as \( \sqrt{2E}/2\lambda_f \) with \( \lambda_f \) being electron elastic MFP [6] near the metal surfaces. The quantity \( \lambda_f \) effectively takes into account attenuation of the ejected electron wave packet by inelastic collisions with other electrons in the bulk. It weakly depends on the electron energy, being close to 5 Å at a few tens eV range [6]. We have set \( \lambda_f = 10 \) a.u. The initial wave function \( \Phi_0(z) \) for the case of initial delocalized state has been computed as an eigenfunction of the potential \( U_s(z) + U_h(z) \) localized in the vicinity of an atom placed at \( z_{\text{at}} \) [the atoms are nested at the maxima of the potential energy \( U_s(z) \)]. For ionization from an initial delocalized state, the wave function \( \Phi_0(z) \) has been computed as an eigenfunction of the potential \( U_s(z) \); in this case the term \( U_h(z) \) in Eq. (1) has been omitted in the wave propagation. Note that the initial electron states are assumed to be below Fermi level. They are not perturbed by inelastic collisions with other electrons, and in the computation of the initial functions \( \Phi_0(z) \) the damping \( \gamma(z) \) must be omitted. In Fig. 1 the relevant functions of the model are plotted.
of the wave packet there is negligibly small at the Fourier transform of the final wave packet. It is im-
absorbing potential starts to work. The amplitudes of the wave packet is yet pretty far from the region where the
initial from the metal is noticeable, but the principle part of when the wave packet has left the region where the poten-
tial from the very surface is well synchronized. Then, the curves for deeper atoms are shifted to the earlier times. The shift depends both on the position of the atom and on the energy \( E \) considered. The reason for this shift is obvious: the electron ejected from an atom in the solid at time \( t \) starts to feel the laser electric field only at \( t' = t + \tau_E(z_{\text{so}}; E) \), where \( \tau_E \) is the time for electron passing from \( z_{\text{so}} \) to the surface \( z = 0 \). It is noteworthy that the curves in Fig. 2 for \( E = 3 \) a.u. are more dense than for \( E = 2 \) a.u.; this means that the electrons with larger energy move faster in the bulk. The position of the COE for the sum of the spectra of electrons ejected from different atoms corresponds roughly to the COE of the spectrum ejected from the third atom; this atom is placed at the distance close to \( \lambda_j \) from the surface. It is then obvious that the COE for the higher final energy is shifted to the right with respect to the COE of the spectrum for lower energy. The shift in our case is about 12 as. The shifts of the extrema of the COE curves for different atoms with respect to the COE from the topmost atom can be effectively represented as \( \tau_E(z_{\text{so}}) = z_{\text{so}}/v(E) \). The effective velocities \( v(E) \) read as \( v(E = 3 \) a.u.\) = 2.68 \( \pm 0.01 \) a.u. and \( v(E = 2 \) a.u.\) = 2.29 \( \pm 0.01 \) a.u. These values of the velocities give for the effective potential energy in the bulk \( U_{\text{av}} = E - v^2(E)/2 \) the values \( -0.62 \) a.u. for \( E = 2 \) a.u. and \( -0.60 \) a.u. for \( E = 3 \) a.u. These values are quite close to each other and are in good correspondence with the minimal value of the potential energy \( U_j(z) \) in the bulk. These results evidence that the effect of the group velocity does not reveal itself within the present model. Actually, the group velocity in the bulk is formed by the interference of the wavelets arising from scattering of the incident wave by the atoms in the lattice. Taking into account a small

Our computations have been performed with the split-
propagation algorithm with the fast-Fourier computation of the kinetic energy. The mesh comprises 16384 knots and
covers uniformly the interval \( z \in [-300 \) a.u., 1340 \) a.u.\]. The time step has been set equal to 0.03 a.u. The outgoing
wave asymptotic condition has been provided by the arti-
ficial absorbing potentials at the edges of the mesh. Propagation has been performed until \( t_{\text{fin}} = \tau_T + 10 \) a.u.,
when the wave packet has left the region where the poten-
tial from the metal is noticeable, but the principle part of the wave packet is yet pretty far from the region where the absorbing potential starts to work. The amplitudes of population of the final states have been computed with the Fourier transform of the final wave packet. It is im-
portant that, due to the inelastic collisions in the bulk, a part
of the wave packet there is negligibly small at \( t = t_{\text{fin}} \).

Let us first consider excitation of the electrons from localized initial states. This case corresponds to the ejection
of electrons from the 4\( f \) band in the experiment [1]. In this case, the energy spectrum is computed as a sum of the spectra of the electrons ejected from the atoms at various positions in the bulk; we take into account 17 consecutive atoms. Because of the inelastic collisions, the relevant electron yield decreases exponentially with the depth of the atom, following the dependence \( I = I_0 \exp(-|z_{\text{so}}|/\lambda_j) \), where \( I_0 \) is the total electron yield from the topmost atom.

![FIG. 1 (color). The potential energies and the wave functions of the localized states. Solid lines: the potentials in the bulk \( U_j(z) \) with account for attraction of the electron to the positive hole, for electrons ejected from the topmost (blue) line, for electron ejected from the fifth atom (black line); the dashed lines show the corresponding initial wave functions \( \Phi_j(z) \); dashed-dotted (red) line shows the profile of the laser pulse potential \( E_L(z) \) screened in the bulk.](image)

![FIG. 2 (color). The center of energy (COE) of the spectra of ejected electrons. (a) \( E = 2 \) a.u., (b) \( E = 3 \) a.u. Black dashed line: the topmost atom; red dashed line: the second atom; green dashed line: the third atom; blue dashed line: the fourth atom. The orange solid line: the COE of the total spectrum.](image)
value of the MFP in the metal at the final energies considered, one may conclude that under these conditions the group velocity of the wave packet in the bulk hardly can be formed. In our computations, the forming of the group velocity could reveal itself in a nonlinear dependence of the time $\tau_s(z_0; E)$ on the atom distance from the surface. We do not notice this effect.

Now let us turn to the problem of ionization from the continuous band. This band for the considered system covers the interval from $-12.27$ to $-5.92$ eV. In a restricted metal this continuum is represented with 75 discrete states. As a center of the continuous band we take the 45th state. This state has an energy $\epsilon_{45} = -9.46$ eV. We took as initial 15 states in the band and propagated them in time with Eq. (1) taking various energies in vacuum $E(k) = E_0 + \epsilon_n - \epsilon_{45}$ for the various initial states $\Phi_k(z)$. This corresponds to the excitation of the band by such XUV pulse that the center of the spectrum of electrons ejected from the center of the allowed band lies at 3 a.u. with respect to the vacuum level. First, the electron spectrum obtained with excitation from the selected states from the band have been calculated. Then the total spectrum was obtained with the integration over the entire energy band of the delocalized electrons. The computed reduced centers of masses of the total electron spectra in their dependence on the delay between XUV and the laser pulses are shown in Fig. 3 for a few initial states. One can see that the results are practically unshifted to each other.

The principal results of the present study are collected in Fig. 3. One may see that the COEs from the first atom are synchronized pretty well. The COEs obtained with the initial states from the band are almost synchronized with the COEs obtained from the topmost atom. The COEs for the spectra calculated with the initial localized states are noticeably delayed with respect to the COEs for the delocalized states. This shift is about 85 as, while the shift obtained here for the COEs from localized states at final energies $E = 2$ a.u. and $E = 3$ a.u. is about 10 as. The experimental result [1] is $110 \pm 70$ as.

In conclusion, the results of a time-dependent approach that goes beyond the static model [1] are presented. Our model includes the main ingredients of the short time physics involved in the experiment [1]. Its main limitations are that it is a one-dimensional model and uses an energy-independent pseudopotential that does not take into account the fact that the electrons in the final state would penetrate different regions of the ionic cores and therefore feel an energy-dependent interaction potential. In addition, our model neglects the hole in the delocalized state. These effects should be investigated further. What would be needed is a full time-dependent version of the calculations [1]. This is not computationally feasible at the moment. However, the calculations presented here, despite using a one-dimensional model potential, use a time-dependent approach and take into account all relevant effects leading to a reasonable agreement with experiment. In addition, our model can also benefit a broad audience by stimulating theoretical time-dependent investigation of complex problems in the condensed-matter physics such as the influence of dynamical image potential screening effects on charge transfer at surfaces and in strongly correlated oxide nanostructures [9,10].

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