All-inclusive interacting dark sector cosmologies

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In this paper we explore possible extensions of interacting dark energy cosmologies, where dark energy and dark matter interact nongravitationally with one another. In particular, we focus on the neutrino sector, analyzing the effect of both neutrino masses and the effective number of neutrino species. We consider the *Planck* 2018 legacy release data combined with several other cosmological probes, finding no evidence for new physics in the dark radiation sector. The current neutrino constraints from cosmology should therefore be regarded as robust, as they are not strongly dependent on the dark sector physics, once all the available observations are combined. Namely, we find a total neutrino mass $M_\nu < 0.15$ eV and a number of effective relativistic degrees of freedom $N_{\text{eff}} = 3.03^{+0.33}_{-0.33}$, both at 95% C.L., which are close to those obtained within the Λ CDM cosmology, $M_\nu < 0.12$ eV and $N_{\text{eff}} = 3.00^{+0.36}_{-0.35}$, for the same data combination.

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I. INTRODUCTION

An overwhelming number of observations confirm that our Universe is undergoing a phase of accelerated expansion. Within the context of general relativity, this effect can be described by adding a dark energy (DE) component, characterized by a negative pressure. According to the observational evidence, nearly 68% of the total energy budget of the Universe consists of such a dark energy fluid. Observations further predict that around 28% of the total energy budget of the Universe corresponds to nonluminous dark matter (DM) [1–3]. Observations from different astronomical sources seem to point to a DE component that is very similar to a cosmological constant, and to a pressureless DM component, also known as cold dark matter (CDM). These two components are the basic ingredients of the so-called Λ CDM cosmology. However, given the fact that (a) the precise nature of the DE and DM fluids remains unknown, despite the large number of devoted measurements to unravel the underlying physics [4–8], and (b) due to a number of persisting tensions within the minimal Λ CDM scheme, there is still plenty of room for other possible scenarios with nonminimal dark sector physics. In this

regard, we shall consider here interacting dark sector cosmologies, in which the DE and the DM components interact nongravitationally [9–45]. Indeed, the dynamics of such a universe could have been present since early times, modifying other dark sector physics, such as that of dark radiation, i.e., that of the neutrinos. Therefore, the question we would like to address here is the following: are cosmological limits on the standard physics of dark radiation strongly dependent on the dark sector model?

In order to investigate this issue we use a set of observational data from various important cosmological sources. This set includes the cosmic microwave background radiation, baryon acoustic oscillation distance measurements, local measurements of the Hubble constant from the Hubble Space Telescope, the Pantheon sample of type Ia supernovae, and finally the Hubble parameter measurements at different redshifts from cosmic chronometers.

The structure of the paper is as follows. Section II introduces the cosmological model explored here, while Sec. III describes the methodology and measurements exploited in our data analyses. Section IV presents our results, and we conclude the paper in Sec. V.

II. INTERACTING DARK UNIVERSE

We consider an interacting dark sector scenario between cold DM and DE in a homogeneous and isotropic flat universe where the gravitational sector is described by Einstein's general relativity. The conservation of the

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energy-momentum tensor for cold DM and DE leads to the coupled equations

$$\dot{\rho}_c + 3H\rho_c = -Q, \quad (1)$$

$$\dot{\rho}_x + 3H(1 + w_x)\rho_x = Q, \quad (2)$$

where we have explicitly used the DE state parameter $w_x = p_x/\rho_x$ (here p_x is the pressure of the DE fluid and ρ_x is its energy density), while for DM we used its pressure p_c (which for a CDM component is 0) and energy density ρ_c . Note that here H denotes the Hubble rate of the prescribed homogeneous and isotropic universe, i.e., a Friedmann-Lemaître-Robertson-Walker universe. In Eq. (1) we have introduced the quantity Q , which is known as the interaction rate between the dark sectors. While the exact form of the interaction rate is not known, possible phenomenological descriptions at the classical and quantum levels have been developed in the literature (see Ref. [46] for a comprehensive review) in an attempt to recover some different interaction models from scalar field theories; see, e.g., the recent Ref. [47], or for other cosmological contexts see, e.g., Ref. [48]. In the present work, we restrict ourselves to the most well-known parametric form of the coupling function Q :

$$Q = 3H\xi\rho_x, \quad (3)$$

where ξ is the coupling parameter that characterizes the strength of the coupling. For convenience, the condition $\xi < 0$ corresponds to energy flow from DE to DM, and $\xi > 0$ represents the opposite case. We refer to Refs. [27,31,34,40,41] for details concerning the linear perturbation theory within these coupled cosmologies.

III. OBSERVATIONAL DATA AND METHODOLOGY

We now briefly describe the observational data sets that we use in the present work.

- (1) Cosmic microwave background (CMB): We make use of the latest CMB measurements from the final 2018 *Planck* legacy release [1–3].
- (2) Baryon acoustic oscillations (BAO): A number of BAO constraints from different astronomical missions are exploited, namely, those from the 6dFGS [49], SDSS-MGS [50], and BOSS DR12 [51] surveys, as considered by the *Planck* Collaboration [2].
- (3) R19: We adopt the latest measurement of the Hubble constant obtained by a reanalysis of the Hubble Space Telescope data using Cepheids as calibrators, i.e., $H_0 = 74.03 \pm 1.42$ km/s/Mpc at 68% C.L. [52].
- (4) Pantheon: We analyze the luminosity distance data of type Ia supernovae from the Pantheon catalog [53], including 1048 data points in the redshift region $z \in [0.01, 2.3]$.
- (5) Cosmic chronometers (CC): Thirty measurements of the Hubble parameter at different redshifts extracted

from cosmic chronometers in the redshift range $0 < z < 2$ (as tabulated in Ref. [54]) are also considered in our data analyses.

We consider a fiducial cosmology described by eight cosmological parameters: six from the standard Λ CDM model (the baryon and cold dark matter energy densities $\Omega_b h^2$ and $\Omega_c h^2$, the ratio between the sound horizon and angular diameter distance at decoupling $100\theta_{MC}$, the reionization optical depth τ , and the spectral index and amplitude of the scalar primordial power spectrum n_s and A_s), and two that account for the dark sector physics (the dark energy equation of state w_x and the strength of the coupling ξ). Therefore, the interacting dark energy (IDE) scenario is described by

$$\mathcal{P} \equiv \{\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, \tau, n_s, \log[10^{10} A_s], \xi, w_x\}. \quad (4)$$

We consider $\xi < 0$ in the phantom scenario ($w_x < -1$) and $\xi > 0$ in the quintessence regime ($w_x > -1$) to avoid early-time instabilities [13,14]; see Table I for the priors on all of the parameters. It is important to mention that the division of the parameter space into ($\xi < 0, w_x < -1$) or ($\xi > 0, w_x > -1$) is motivated by the doom factor analysis [14]. Following the notation of Refs. [26,27,40], the doom factor d is defined as $d = -Q[3H(1 + w_x)\rho_x]^{-1}$. The interacting model becomes stable for $d < 0$, which for the present model $Q = 3H\xi\rho_x$ requires either $\xi < 0, w_x < -1$ or $\xi > 0, w_x > -1$. Hence, as we can see this division is necessary to maintain the early-time instability in the perturbation evolution of the scalar modes of the dark species (DM and DE). In this paper, we refer to the scenario with a phantom-like DE equation of state ($w_x < -1$) as IDEp, and the IDE scenario with a quintessence-like DE equation of state ($w_x > -1$) as IDEq.

Then, we allow for freedom in the dark radiation sector by enlarging the fiducial cosmological scenario with the sum of the neutrino masses M_ν (IDE + M_ν),

$$\mathcal{P} \equiv \{\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, \tau, n_s, \log[10^{10} A_s], \xi, w_x, M_\nu\}, \quad (5)$$

TABLE I. List of the flat priors on the cosmological parameters assumed in this work.

Parameter	Prior phantom	Prior quintessence
$\Omega_b h^2$	[0.013, 0.033]	[0.013, 0.033]
$\Omega_c h^2$	[0.001, 0.99]	[0.001, 0.99]
$100\theta_{MC}$	[0.5, 10]	[0.5, 10]
τ	[0.01, 0.8]	[0.01, 0.8]
n_s	[0.7, 1.3]	[0.7, 1.3]
$\log[10^{10} A_s]$	[1.7, 5.0]	[1.7, 5.0]
w_x	$[-3, -1]$	$[-1, 0]$
ξ	$[-1, 0]$	$[0, 1]$
M_ν	$[0, 1]$	$[0, 1]$
N_{eff}	[0.05, 10]	[0.05, 10]

or with extra-relativistic species at recombination ($\text{IDE} + N_{\text{eff}}$),

$$\mathcal{P} \equiv \{\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, \tau, n_s, \log[10^{10} A_s], \xi, w_x, N_{\text{eff}}\}. \quad (6)$$

Finally, we also analyze the full scenario $\text{IDE} + M_\nu + N_{\text{eff}}$:

$$\mathcal{P} \equiv \{\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, \tau, n_s, \log[10^{10} A_s], \xi, w_x, M_\nu, N_{\text{eff}}\}. \quad (7)$$

For numerical purposes, we make use of the latest version of the publicly available Markov chain Monte Carlo code COSMOMC [55,56] package which supports the new 2018 *Planck* likelihood [1] and has been modified to include IDE scenarios. The convergence diagnostic follows the Gelman-Rubin criteria [57].

IV. RESULTS

Throughout this section we present the results obtained within the different IDE scenarios.

A. IDE with $w_x < -1$

Here we start by analyzing the constraints obtained under the assumption of a phantom-like dark energy equation of state $w_x < -1$.

1. IDE

The results for our baseline IDE scenario, based on eight parameters, with a dark energy equation of state $w_x < -1$ are shown in Table II and Fig. 1.

Notice that, regardless of the data set combination, the CDM energy density $\Omega_c h^2$ is larger than that in the Λ CDM

model. This is mainly due to the energy flow between the dark sectors which, for this phantom case with $\xi < 0$ (i.e., energy flux flowing from DE to DM), results in a larger density for cold dark matter at present; see also Ref. [58]. Also, the Hubble constant is always much larger than that in the canonical Λ CDM scenario when considering CMB only, due to the fact that in the phantom region there is a strong degeneracy between w_x and H_0 at the level of the CMB (see Fig. 1). When the dark energy equation of state is allowed to vary in the $w < -1$ region, H_0 must be larger to prevent a shift in the CMB peaks. Notice that here there is no preference for a nonzero dark sector coupling, and the so-called Hubble constant tension is greatly alleviated due to the phantom character of the DE component and not from the presence of a coupling. From CMB measurements alone, we find that a dark energy equation of state $w_x < -1$ is preferred at a significance above the 2σ level and a lower limit of $\xi > -0.090$ at 95% C.L. The value of S_8 is instead shifted in the right direction to solve the tension between *Planck* and the cosmic shear experiments DES [59,60], KiDS-450 [61–63], or CFHTLenS [64–66], i.e., $S_8 = 0.756 \pm 0.034$ at 68% C.L. for CMB in the IDE model, to be compared with $S_8 = 0.822 \pm 0.015$ at 68% C.L. in the Λ CDM scenario for the same data set, or $S_8 = 0.777^{+0.022}_{-0.036}$ at 68% C.L. for a w CDM cosmology. When including the BAO data (see the third column of Table II), the six parameters of the standard Λ CDM model are almost unmodified, while w_x is now perfectly consistent with a cosmological constant at the 2σ level. For CMB + BAO, H_0 shifts back towards a lower value ($H_0 = 68.7^{+2.7}_{-2.5}$ km/s/Mpc at 95% C.L.). The value of the clustering parameter σ_8 is still below those in Λ CDM and w CDM, due to the correlation with ξ (see Fig. 1). When considering the combination of CMB + R19 (shown in the fourth column of Table II), we find a value for the Hubble constant in agreement with the R19 measurement, together with a preference at more than 3σ for a phantom

TABLE II. 95% C.L. constraints within the minimal IDE model in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	$0.134^{+0.017}_{-0.015}$	$0.135^{+0.014}_{-0.014}$	$0.134^{+0.017}_{-0.015}$	$0.135^{+0.015}_{-0.014}$	$0.135^{+0.014}_{-0.014}$	$0.134^{+0.016}_{-0.015}$
$\Omega_b h^2$	$0.02239^{+0.00030}_{-0.00030}$	$0.02239^{+0.00014+0.00029}_{-0.00028}$	$0.02238^{+0.00029}_{-0.00029}$	$0.02236^{+0.00030}_{-0.00030}$	$0.02240^{+0.00028}_{-0.00028}$	$0.02242^{+0.00028}_{-0.00029}$
$100\theta_{MC}$	$1.0402^{+0.0011}_{-0.0011}$	$1.0401^{+0.0010}_{-0.0010}$	$1.0402^{+0.0010}_{-0.0011}$	$1.0401^{+0.0010}_{-0.0010}$	$1.0401^{+0.0010}_{-0.0010}$	$1.0402^{+0.0010}_{-0.0010}$
τ	$0.054^{+0.015}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$
n_s	$0.9652^{+0.0086}_{-0.0086}$	$0.9657^{+0.0081}_{-0.0082}$	$0.9648^{+0.0086}_{-0.0086}$	$0.9647^{+0.0086}_{-0.0086}$	$0.9660^{+0.0078}_{-0.0080}$	$0.9662^{+0.0085}_{-0.0085}$
$\ln(10^{10} A_s)$	$3.043^{+0.029}_{-0.031}$	$3.045^{+0.032}_{-0.030}$	$3.044^{+0.031}_{-0.030}$	$3.045^{+0.033}_{-0.031}$	$3.045^{+0.033}_{-0.031}$	$3.045^{+0.033}_{-0.031}$
w_x	$-1.58^{+0.49}_{-0.44}$	$-1.094^{+0.094}_{-0.099}$	$-1.27^{+0.11}_{-0.12}$	$-1.085^{+0.083}_{-0.078}$	$-1.080^{+0.078}_{-0.072}$	$-1.139^{+0.081}_{-0.083}$
ξ	> -0.090	> -0.101	> -0.094	> -0.100	> -0.101	> -0.099
Ω_{m0}	$0.23^{+0.11}_{-0.09}$	$0.336^{+0.044}_{-0.042}$	$0.286^{+0.038}_{-0.035}$	$0.338^{+0.040}_{-0.038}$	$0.339^{+0.037}_{-0.036}$	$0.318^{+0.038}_{-0.036}$
σ_8	$0.89^{+0.15}_{-0.16}$	$0.760^{+0.074}_{-0.070}$	$0.811^{+0.072}_{-0.077}$	$0.762^{+0.066}_{-0.063}$	$0.755^{+0.068}_{-0.064}$	$0.774^{+0.066}_{-0.066}$
H_0 [km/s/Mpc]	> 68	$68.7^{+2.7}_{-2.5}$	$74.2^{+2.8}_{-2.7}$	$68.3^{+2.0}_{-1.9}$	$68.3^{+1.6}_{-1.7}$	$70.3^{+1.7}_{-1.7}$
S_8	$0.756^{+0.064}_{-0.063}$	$0.802^{+0.036}_{-0.036}$	$0.790^{+0.040}_{-0.041}$	$0.808^{+0.039}_{-0.039}$	$0.801^{+0.037}_{-0.035}$	$0.796^{+0.040}_{-0.040}$

FIG. 1. 68% and 95% C.L. allowed contours and one-dimensional posterior probability distributions within the minimal IDE model in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations. Only a subset of cosmological parameters are shown.

dark energy ($w_x = -1.27^{+0.14}_{-0.17}$ at 99% C.L.). Adding the Pantheon and CC measurements to the CMB (see the fifth column of Table II) leads to constraints that are very similar to the CMB + BAO case. The combination CMB + BAO + Pantheon + CC (see the sixth column of Table II) only diminishes the error bars when compared to the previous case. Finally, the data combination of CMB + R19 + Pantheon + CC (see the last column of Table II) is completely driven by the discrepancies between the CMB + Pantheon + CC data combination and the R19 measurements. Therefore, the Hubble constant shifts slightly towards higher values, reducing the tension with R19 at 2.3σ and leading to evidence for a phantom dark energy component $w_x < -1$ at a high significance.

2. IDE + M_ν : Nine parameters

The results for an IDE + M_ν scenario, based on nine parameters, with a dark energy equation of state $w_x < -1$ are shown in Table III and Fig. 2.

In this scenario—extended to include the total neutrino mass M_ν —independently of the data combination chosen, all of the constraints on the six cosmological parameters of the Λ CDM model as well as on the dark energy equation of state w_x and all the derived parameters (H_0 , Ω_{m0} , σ_8 , and

S_8) are very similar to those in the minimal IDE scenario of the previous section (see Table II). Therefore, the addition of the total neutrino mass does not introduce new correlations between the previous cosmological parameters, as we can see in Fig. 2. The well-known correlations between M_ν and the dark energy equation of state w_x , the matter density Ω_{m0} , and the clustering parameter σ_8 are present in this model, and are especially visible for the CMB + BAO and CMB + R19 data combinations. However, the also very well-known degeneracy between H_0 and M_ν disappears completely in this scenario. For this reason, the M_ν and $\Omega_\nu h^2$ upper limits are identical in the CMB and CMB + R19 cases, instead of being improved when R19 measurements are added to CMB observations (as it happens in the Λ CDM + M_ν model). Comparing the constraints obtained in this extended IDE scenario with those obtained within a Λ CDM scenario for the same combination of data sets, one can notice that the upper limits on M_ν are slightly relaxed in this case, because of the phantom behavior of the dark energy equation of state and the $M_\nu - w_x$ correlation. Cosmological neutrino mass bounds are softened if the dark energy equation of state is taken as a free parameter. If w_x is allowed to vary, the matter energy density takes very high values, and this can

TABLE III. 95% C.L. constraints within the IDE + M_ν model in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	$0.133^{+0.018}_{-0.015}$	$0.136^{+0.015}_{-0.016}$	$0.135^{+0.017}_{-0.015}$	$0.135^{+0.014}_{-0.014}$	$0.135^{+0.015}_{-0.015}$	$0.134^{+0.016}_{-0.015}$
$\Omega_b h^2$	$0.02237^{+0.00030}_{-0.00031}$	$0.02238^{+0.00028}_{-0.00028}$	$0.02236^{+0.00031}_{-0.00031}$	$0.02235^{+0.00030}_{-0.00029}$	$0.02240^{+0.00028}_{-0.00027}$	$0.02243^{+0.00029}_{-0.00029}$
$100\theta_{MC}$	$1.0402^{+0.0010}_{-0.0011}$	$1.0401^{+0.0010}_{-0.0010}$	$1.0401^{+0.0010}_{-0.0010}$	$1.0401^{+0.0010}_{-0.0010}$	$1.0401^{+0.0010}_{-0.0010}$	$1.0402^{+0.0011}_{-0.0011}$
τ	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.055^{+0.017}_{-0.015}$
n_s	$0.9650^{+0.0088}_{-0.0088}$	$0.9654^{+0.0080}_{-0.0078}$	$0.9646^{+0.0087}_{-0.0091}$	$0.9645^{+0.0086}_{-0.0086}$	$0.9660^{+0.0080}_{-0.0079}$	$0.9663^{+0.0085}_{-0.0085}$
$\ln(10^{10}A_s)$	$3.043^{+0.033}_{-0.031}$	$3.045^{+0.034}_{-0.031}$	$3.044^{+0.033}_{-0.032}$	$3.045^{+0.032}_{-0.031}$	$3.045^{+0.033}_{-0.031}$	$3.045^{+0.035}_{-0.031}$
w_x	$-1.60^{+0.52}_{-0.46}$	> -1.22	$-1.29^{+0.15}_{-0.16}$	$-1.092^{+0.090}_{-0.086}$	> -1.15	$-1.136^{+0.082}_{-0.087}$
ξ	> -0.086	> -0.101	> -0.098	> -0.102	> -0.101	> -0.100
Ω_{m0}	$0.23^{+0.11}_{-0.09}$	$0.337^{+0.045}_{-0.043}$	$0.288^{+0.039}_{-0.037}$	$0.342^{+0.042}_{-0.042}$	$0.339^{+0.037}_{-0.037}$	$0.318^{+0.039}_{-0.038}$
σ_8	$0.88^{+0.15}_{-0.14}$	$0.758^{+0.076}_{-0.070}$	$0.803^{+0.079}_{-0.076}$	$0.756^{+0.071}_{-0.065}$	$0.756^{+0.070}_{-0.065}$	$0.775^{+0.070}_{-0.069}$
H_0 [km/s/Mpc]	> 68	$68.8^{+2.8}_{-2.7}$	$74.2^{+2.7}_{-2.7}$	$68.2^{+2.1}_{-2.1}$	$68.3^{+1.5}_{-1.5}$	$70.4^{+1.7}_{-1.7}$
M_ν [eV]	< 0.313	< 0.183	< 0.313	< 0.255	< 0.156	< 0.151
$\Omega_\nu h^2$	< 0.0034	< 0.0020	< 0.0034	< 0.0027	< 0.0017	< 0.0016
S_8	$0.754^{+0.069}_{-0.064}$	$0.802^{+0.039}_{-0.037}$	$0.785^{+0.044}_{-0.045}$	$0.806^{+0.042}_{-0.041}$	$0.802^{+0.038}_{-0.037}$	$0.796^{+0.042}_{-0.040}$

be compensated with a larger neutrino mass. Indeed, the authors of Ref. [67] found that a larger neutrino mass would be allowed when a dark coupling is present. The most stringent limit we find on the total neutrino mass is for the

CMB + R19+Pantheon+CC data combination, $M_\nu < 0.151$ eV at 95% C.L. The former bound is very similar to the one obtained for CMB + BAO + Pantheon + CC, $M_\nu < 0.156$ eV at 95% C.L.

FIG. 2. 68% and 95% C.L. allowed contours and one-dimensional posterior probability distributions within the IDE + M_ν model in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations. Only a subset of cosmological parameters are shown.

TABLE IV. 95% C.L. constraints within the IDE + N_{eff} scheme in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	$0.131^{+0.019}_{-0.017}$	$0.133^{+0.017}_{-0.017}$	$0.131^{+0.018}_{-0.016}$	$0.134^{+0.017}_{-0.017}$	$0.135^{+0.017}_{-0.017}$	$0.138^{+0.018}_{-0.017}$
$\Omega_b h^2$	$0.02227^{+0.00042}_{-0.00043}$	$0.02230^{+0.00039}_{-0.00039}$	$0.02226^{+0.00043}_{-0.00043}$	$0.02232^{+0.00038}_{-0.00039}$	$0.02238^{+0.00036}_{-0.00035}$	$0.02255^{+0.00037}_{-0.00036}$
$100\theta_{MC}$	$1.0404^{+0.0012}_{-0.0013}$	$1.0404^{+0.0012}_{-0.0013}$	$1.0404^{+0.0012}_{-0.0013}$	$1.0402^{+0.0012}_{-0.0012}$	$1.0402^{+0.0012}_{-0.0012}$	$1.0399^{+0.0012}_{-0.0012}$
τ	$0.053^{+0.016}_{-0.016}$	$0.054^{+0.016}_{-0.015}$	$0.053^{+0.016}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.056^{+0.017}_{-0.015}$
n_s	$0.960^{+0.017}_{-0.017}$	$0.962^{+0.015}_{-0.015}$	$0.960^{+0.017}_{-0.017}$	$0.963^{+0.015}_{-0.015}$	$0.965^{+0.014}_{-0.014}$	$0.972^{+0.013}_{-0.013}$
$\ln(10^{10}A_s)$	$3.037^{+0.037}_{-0.038}$	$3.039^{+0.036}_{-0.036}$	$3.036^{+0.037}_{-0.037}$	$3.042^{+0.036}_{-0.036}$	$3.043^{+0.036}_{-0.035}$	$3.053^{+0.036}_{-0.034}$
w_x	$-1.61^{+0.54}_{-0.46}$	> -1.22	$-1.31^{+0.14}_{-0.15}$	$-1.090^{+0.087}_{-0.079}$	$-1.082^{+0.081}_{-0.074}$	$-1.122^{+0.084}_{-0.088}$
ξ	> -0.087	> -0.099	> -0.094	> -0.101	> -0.101	> -0.101
Ω_{m0}	$0.22^{+0.12}_{-0.09}$	$0.334^{+0.046}_{-0.042}$	$0.281^{+0.039}_{-0.037}$	$0.340^{+0.040}_{-0.041}$	$0.339^{+0.036}_{-0.036}$	$0.321^{+0.037}_{-0.036}$
σ_8	$0.89^{+0.15}_{-0.16}$	$0.761^{+0.074}_{-0.071}$	$0.814^{+0.072}_{-0.075}$	$0.758^{+0.068}_{-0.064}$	$0.754^{+0.068}_{-0.064}$	$0.773^{+0.070}_{-0.069}$
$H_0[\text{km/s/Mpc}]$	> 67	$68.4^{+3.2}_{-2.9}$	$74.2^{+2.7}_{-2.8}$	$68.0^{+2.6}_{-2.5}$	$68.2^{+2.1}_{-2.1}$	$70.9^{+2.0}_{-2.0}$
N_{eff}	$2.91^{+0.38}_{-0.38}$	$2.94^{+0.36}_{-0.35}$	$2.90^{+0.38}_{-0.36}$	$2.99^{+0.32}_{-0.31}$	$3.02^{+0.32}_{-0.31}$	$3.22^{+0.31}_{-0.29}$
S_8	$0.753^{+0.068}_{-0.065}$	$0.801^{+0.036}_{-0.035}$	$0.785^{+0.041}_{-0.041}$	$0.806^{+0.040}_{-0.040}$	$0.800^{+0.037}_{-0.035}$	$0.798^{+0.041}_{-0.040}$

3. IDE + N_{eff} : Nine parameters

The results for an IDE + N_{eff} scenario, based on nine parameters, with a dark energy equation of state $w_x < -1$ are shown in Table IV and Fig. 3. Notice that in general the

constraints on the cosmological parameters of the Λ CDM model, with the exception of the spectral index n_s , are very similar to those obtained in previous scenarios. Due to the well-known correlation between N_{eff} and n_s , we notice a

FIG. 3. 68% and 95% C.L. allowed contours and one-dimensional posterior probability distributions within the IDE + N_{eff} model in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations. Only a subset of cosmological parameters are shown.

very mild shift in the mean value of the spectral index toward smaller values. The effective number of relativistic degrees of freedom N_{eff} we recover in this modified cosmological scenario is perfectly consistent with its standard value $N_{\text{eff}} = 3.046$ [68,69]. Also in this scenario, the addition of the effective number of neutrino species N_{eff} as a free parameter does not introduce a new direction of correlation between the previous cosmological parameters; see Fig. 3. The well-known correlation between N_{eff} and the Hubble constant H_0 disappears completely in this scenario, since the dark energy equation of state is also an additional free parameter. For this very same reason, the constraints on N_{eff} are the same for the CMB and CMB + R19 cases. When adding Pantheon and CC data to the CMB (see the fifth column of Table IV), the relativistic degrees of freedom shift towards higher values ($N_{\text{eff}} = 2.99 \pm 0.16$ at 68% C.L.) with respect to the CMB-only case (where $N_{\text{eff}} = 2.91 \pm 0.019$ at 68% C.L.). When we further add the R19 measurements, i.e., we consider CMB + R19 + Pantheon + CC (see the last column of Table IV), we obtain our most stringent bound $N_{\text{eff}} = 3.22^{+0.31}_{-0.29}$ at 95% C.L. associated with the highest mean value for N_{eff} .

4. IDE + M_ν + N_{eff} : Ten parameters

The results for an IDE + M_ν + N_{eff} scenario, based on ten parameters, with a dark energy equation of state $w_x < -1$ are shown in Table V and Fig. 4. In this scenario the spectral index n_s is shifted further down and we obtain an indication that w_x is a phantom at a high significance for the CMB + R19 data set combination; see Table V.

The considerations we made in the previous cases about the directions of the correlations between the cosmological parameters are unaltered by the variation of M_ν and N_{eff} at

the same time. While the constraints on the effective number of neutrino species N_{eff} for all data set combinations are identical to the IDE + N_{eff} scenario, the upper limits on the total neutrino mass M_ν are mildly relaxed with respect to the IDE + M_ν model. The most stringent bound on this parameter is now obtained for the combination CMB + BAO + Pantheon + CC (see the sixth column of Table V), and it corresponds to $M_\nu < 0.160$ eV at 95% C.L.

B. IDE with $w_x > -1$

In the following sections we present the constraints for the case of a quintessence-like dark energy equation of state $w_x > -1$.

1. IDE

The results for our baseline IDE scenario, based on eight parameters, with a dark energy equation of state $w_x > -1$ are shown in Table VI and Fig. 5.

Notice that the amount of cold dark matter is much lower than that in the canonical Λ CDM scenario. The reason for this is due to the energy flow from the DM to DE sector and, consequently, the current amount of dark matter energy density decreases as ξ increases; see Fig. 5 and Refs. [58,70]. For this very same reason the CMB + R19 data combination prefers a nonzero value of the coupling ξ at a very high significance.

For the CMB-only case (see the second column of Table VI), the Hubble constant is shifted towards a higher value, mildly alleviating the Hubble constant tension with R19 data at 1.1σ (mainly via the degeneracy between ξ and H_0), as can be seen in Fig. 5. When including the BAO data (see the third column of Table VI), most of the parameters

TABLE V. 95% C.L. constraints within the IDE + M_ν + N_{eff} scheme in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	$0.132^{+0.019}_{-0.017}$	$0.134^{+0.017}_{-0.018}$	$0.132^{+0.018}_{-0.017}$	$0.135^{+0.017}_{-0.017}$	$0.135^{+0.017}_{-0.017}$	$0.139^{+0.018}_{-0.018}$
$\Omega_b h^2$	$0.02223^{+0.00046}_{-0.00045}$	$0.02230^{+0.00042}_{-0.00040}$	$0.02223^{+0.00043}_{-0.00044}$	$0.02232^{+0.00038}_{-0.00038}$	$0.02237^{+0.00036}_{-0.00036}$	$0.02256^{+0.00036}_{-0.00035}$
$100\theta_{MC}$	$1.0404^{+0.0013}_{-0.0013}$	$1.0403^{+0.0013}_{-0.0012}$	$1.0404^{+0.0012}_{-0.0012}$	$1.0402^{+0.0012}_{-0.0012}$	$1.0402^{+0.0012}_{-0.0012}$	$1.0399^{+0.0012}_{-0.0012}$
τ	$0.053^{+0.016}_{-0.016}$	$0.054^{+0.016}_{-0.015}$	$0.053^{+0.017}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.017}_{-0.015}$	$0.056^{+0.017}_{-0.016}$
n_s	$0.959^{+0.017}_{-0.017}$	$0.962^{+0.016}_{-0.015}$	$0.959^{+0.017}_{-0.016}$	$0.963^{+0.015}_{-0.015}$	$0.965^{+0.014}_{-0.014}$	$0.973^{+0.013}_{-0.013}$
$\ln(10^{10} A_s)$	$3.036^{+0.037}_{-0.037}$	$3.040^{+0.037}_{-0.036}$	$3.037^{+0.039}_{-0.037}$	$3.043^{+0.036}_{-0.034}$	$3.043^{+0.037}_{-0.034}$	$3.054^{+0.037}_{-0.035}$
w_x	> -2.13	> -1.23	$-1.34^{+0.19}_{-0.20}$	$-1.097^{+0.091}_{-0.088}$	> -1.158	$-1.123^{+0.089}_{-0.093}$
ξ	> -0.093	> -0.101	> -0.097	> -0.101	> -0.101	> -0.102
Ω_{m0}	$0.23^{+0.13}_{-0.10}$	$0.336^{+0.044}_{-0.042}$	$0.283^{+0.040}_{-0.037}$	$0.342^{+0.041}_{-0.040}$	$0.339^{+0.037}_{-0.037}$	$0.322^{+0.038}_{-0.037}$
σ_8	$0.87^{+0.16}_{-0.16}$	$0.757^{+0.074}_{-0.068}$	$0.805^{+0.079}_{-0.075}$	$0.755^{+0.069}_{-0.064}$	$0.756^{+0.071}_{-0.065}$	$0.772^{+0.075}_{-0.069}$
H_0 [km/s/Mpc]	> 65	$68.4^{+3.1}_{-3.1}$	$74.2^{+2.8}_{-2.7}$	$68.0^{+2.2}_{-2.7}$	$68.2^{+2.2}_{-2.1}$	$70.9^{+1.9}_{-2.0}$
M_ν [eV]	< 0.367	< 0.184	< 0.332	< 0.263	< 0.160	< 0.172
N_{eff}	$2.89^{+0.37}_{-0.37}$	$2.94^{+0.39}_{-0.35}$	$2.88^{+0.37}_{-0.36}$	$3.00^{+0.34}_{-0.33}$	$3.02^{+0.33}_{-0.31}$	$3.22^{+0.29}_{-0.29}$
$\Omega_\nu h^2$	< 0.0037	< 0.0019	< 0.0034	< 0.0028	< 0.0017	< 0.0018
S_8	$0.751^{+0.068}_{-0.067}$	$0.800^{+0.039}_{-0.037}$	$0.779^{+0.044}_{-0.045}$	$0.805^{+0.041}_{-0.040}$	$0.803^{+0.039}_{-0.037}$	$0.798^{+0.042}_{-0.041}$

FIG. 4. 68% and 95% C.L. allowed contours and one-dimensional posterior probability distributions within the IDE + M_ν + N_{eff} model in the phantom-like dark energy scenario ($w_x < -1$) from several data set combinations. Only a subset of cosmological parameters are shown.

are unmodified with respect to the CMB-only case. The tension on H_0 with R19 data is at the 2.9σ level. While the values of σ_8 and S_8 go down with respect to the CMB-only

case, they are still far from those corresponding to the Λ CDM model, even if they are in agreement due to the very large error bars.

TABLE VI. 95% C.L. constraints within the IDE model in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	< 0.115	$0.076^{+0.046}_{-0.058}$	< 0.055	$0.075^{+0.046}_{-0.059}$	$0.077^{+0.044}_{-0.059}$	$0.057^{+0.040}_{-0.051}$
$\Omega_b h^2$	$0.02236^{+0.00029}_{-0.00029}$	$0.02239^{+0.00029}_{-0.00027}$	$0.02238^{+0.00030}_{-0.00030}$	$0.02236^{+0.00029}_{-0.00028}$	$0.02239^{+0.00028}_{-0.00027}$	$0.02241^{+0.00029}_{-0.00029}$
$100\theta_{MC}$	$1.0448^{+0.0050}_{-0.0043}$	$1.0438^{+0.0043}_{-0.0031}$	$1.0476^{+0.0027}_{-0.0029}$	$1.0438^{+0.0044}_{-0.0032}$	$1.0437^{+0.0044}_{-0.0031}$	$1.0450^{+0.0042}_{-0.0032}$
τ	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.017}_{-0.015}$	$0.054^{+0.015}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$
n_s	$0.9650^{+0.0084}_{-0.0084}$	$0.9658^{+0.0082}_{-0.0084}$	$0.9659^{+0.0080}_{-0.0082}$	$0.9648^{+0.0082}_{-0.0085}$	$0.9660^{+0.0079}_{-0.0079}$	$0.9661^{+0.0085}_{-0.0084}$
$\ln(10^{10} A_s)$	$3.045^{+0.031}_{-0.031}$	$3.045^{+0.034}_{-0.032}$	$3.044^{+0.031}_{-0.031}$	$3.045^{+0.032}_{-0.031}$	$3.045^{+0.033}_{-0.031}$	$3.045^{+0.033}_{-0.031}$
w_x	< -0.77	< -0.80	< -0.904	< -0.79	< -0.79	< -0.834
ξ	< 0.27	< 0.24	$0.231^{+0.060}_{-0.071}$	< 0.25	< 0.24	$0.16^{+0.11}_{-0.10}$
Ω_{m0}	$0.18^{+0.16}_{-0.15}$	$0.21^{+0.11}_{-0.13}$	$0.089^{+0.067}_{-0.054}$	$0.21^{+0.11}_{-0.13}$	$0.22^{+0.10}_{-0.13}$	$0.16^{+0.09}_{-0.10}$
σ_8	$1.6^{+2.1}_{-1.2}$	$1.3^{+1.1}_{-0.7}$	$2.6^{+1.8}_{-1.4}$	$1.3^{+1.2}_{-0.7}$	$1.2^{+1.1}_{-0.6}$	$1.6^{+1.5}_{-0.9}$
H_0 [km/s/Mpc]	$69.3^{+6.2}_{-6.5}$	$68.4^{+2.7}_{-2.5}$	$73.3^{+2.3}_{-2.3}$	$68.2^{+1.9}_{-1.9}$	$68.3^{+1.6}_{-1.5}$	$70.2^{+1.7}_{-1.6}$
S_8	$1.07^{+0.52}_{-0.32}$	$0.97^{+0.35}_{-0.21}$	$1.32^{+0.39}_{-0.34}$	$0.98^{+0.36}_{-0.22}$	$0.97^{+0.35}_{-0.20}$	$1.06^{+0.43}_{-0.26}$

FIG. 5. 68% and 95% C.L. allowed contours and one-dimensional posterior probability distributions within the IDE model in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations. Only a subset of cosmological parameters are shown.

When considering the CMB + R19 combination (see the fourth column of Table VI), the Hubble constant value moves in agreement with the R19 measurement within 1σ , leading to a stronger upper limit on the dark energy equation of state w_x and pushing the value towards the cosmological constant case. In particular, we have $w < -0.904$ at 95% C.L. for CMB + R19. As previously stated, we find a mean value of the coupling ξ that is different from zero at many standard deviations, due to the flux of energy from the DM to DE sector. Both σ_8 and S_8 move towards extremely high values with very large error bars, increasing the tension between *Planck* and the cosmic shear data. The addition of Pantheon and CC to CMB measurements (fifth column of Table VI) leads to a Hubble constant disagreement with R19 data at the 3σ level. The data set combination CMB + R19 + Pantheon + CC provides constraints that lie between the CMB + Pantheon + CC and CMB + R19 cases, slightly shifting the Hubble constant towards higher values (and therefore reducing the tension with R19 data down to the 2.4σ level) and setting limits on the coupling ξ that are different from zero at a high significance.

2. IDE + M_ν : Nine parameters

The results for an IDE + M_ν scenario, based on nine parameters, with a dark energy equation of state $w_x > -1$ are shown in Table VII and Fig. 6. The addition of a varying neutrino mass does not change the directions of the correlations between the cosmological parameters we have without M_ν , as can be seen in Fig. 6. The well-known correlation between M_ν and the dark energy equation of state w_x is present also in this model, while the negative degeneracy present between H_0 and M_ν is completely absent in this scenario with $w_x > -1$. With respect to the phantom regime, a very mild correlation between M_ν and ξ appears, especially in the case of the CMB + R19 data set combination, as we can see in Fig. 6. For this reason, the M_ν and $\Omega_\nu h^2$ upper limits improve in the CMB + R19 case, contrary to what happens when $w_x < -1$ (see Table III). Similarly to the phantom model case, the M_ν upper limits are relaxed, and the most stringent limit we find on the total neutrino mass is for the CMB + Pantheon + CC and CMB + R19 + Pantheon + CC data combinations, for which $M_\nu < 0.152$ eV at 95% C.L.

TABLE VII. 95% C.L. constraints within the IDE + M_ν model in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	<0.116	$0.073^{+0.048}_{-0.058}$	<0.056	$0.074^{+0.046}_{-0.057}$	$0.076^{+0.045}_{-0.058}$	$0.059^{+0.041}_{-0.051}$
$\Omega_b h^2$	$0.02233^{+0.00031}_{-0.00032}$	$0.02238^{+0.00028}_{-0.00028}$	$0.02238^{+0.00030}_{-0.00029}$	$0.02234^{+0.00030}_{-0.00031}$	$0.02239^{+0.00028}_{-0.00028}$	$0.02242^{+0.00029}_{-0.00027}$
$100\theta_{MC}$	$1.0448^{+0.0049}_{-0.0043}$	$1.0439^{+0.0044}_{-0.0033}$	$1.0476^{+0.0027}_{-0.0031}$	$1.0438^{+0.0043}_{-0.0032}$	$1.0437^{+0.0043}_{-0.0031}$	$1.0449^{+0.0041}_{-0.0032}$
τ	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.017}_{-0.015}$	$0.054^{+0.016}_{-0.015}$	$0.054^{+0.016}_{-0.016}$	$0.055^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$
n_s	$0.9644^{+0.0089}_{-0.0090}$	$0.9660^{+0.0079}_{-0.0080}$	$0.9657^{+0.0084}_{-0.0085}$	$0.9646^{+0.0085}_{-0.0087}$	$0.9660^{+0.0081}_{-0.0080}$	$0.9665^{+0.0084}_{-0.0083}$
$\ln(10^{10}A_s)$	$3.045^{+0.032}_{-0.031}$	$3.045^{+0.033}_{-0.031}$	$3.044^{+0.033}_{-0.032}$	$3.045^{+0.032}_{-0.031}$	$3.045^{+0.032}_{-0.031}$	$3.045^{+0.033}_{-0.031}$
w_x	< -0.76	< -0.79	< -0.905	< -0.80	< -0.79	< -0.835
ξ	<0.28	<0.25	$0.234^{+0.067}_{-0.081}$	<0.26	<0.24	$0.158^{+0.11}_{-0.10}$
Ω_{m0}	$0.19^{+0.17}_{-0.13-0.15}$	$0.21^{+0.11}_{-0.13}$	$0.089^{+0.069}_{-0.054}$	$0.21^{+0.11}_{-0.13}$	$0.21^{+0.10}_{-0.13}$	$0.17^{+0.09}_{-0.10}$
σ_8	$1.6^{+2.0}_{-1.1}$	$1.3^{+1.2}_{-0.7}$	$2.6^{+1.8}_{-1.5}$	$1.3^{+1.1}_{-0.7}$	$1.2^{+1.1}_{-0.6}$	$1.5^{+1.4}_{-0.8}$
H_0 [km/s/Mpc]	$68.8^{+6.6}_{-7.1}$	$68.5^{+2.8}_{-2.5}$	$73.3^{+2.2}_{-2.4}$	$68.1^{+2.1}_{-2.1}$	$68.3^{+1.6}_{-1.5}$	$70.2^{+1.7}_{-1.6}$
M_ν	<0.318	<0.173	<0.203	<0.263	<0.152	<0.152
$\Omega_\nu h^2$	<0.0034	<0.0019	<0.0022	<0.0028	<0.0016	<0.0016
S_8	$1.08^{+0.51}_{-0.31}$	$0.99^{+0.36}_{-0.22}$	$1.33^{+0.39}_{-0.35}$	$0.98^{+0.33}_{-0.21}$	$0.97^{+0.34}_{-0.20}$	$1.05^{+0.40}_{-0.25}$

3. IDE + N_{eff} : Nine parameters

Table VIII and Fig. 7 depict the results for an IDE + N_{eff} scenario, based on nine parameters. Concerning the

correlation between N_{eff} and n_s , we notice a shift of 1σ of the spectral index towards lower values, followed by a shift of H_0 in the same direction.

FIG. 6. 68% and 95% C.L. allowed contours and one-dimensional posterior probability distributions within the IDE + M_ν model in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations. Only a subset of cosmological parameters are shown.

TABLE VIII. 95% C.L. constraints within the IDE + N_{eff} model in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	< 0.113	$0.074^{+0.046}_{-0.053}$	< 0.065	< 0.112	$0.077^{+0.045}_{-0.057}$	$0.064^{+0.047}_{-0.056}$
$\Omega_b h^2$	$0.02223^{+0.00044}_{-0.00044}$	$0.02231^{+0.00041}_{-0.00040}$	$0.02237^{+0.00040}_{-0.00037}$	$0.02232^{+0.00038}_{-0.00037}$	$0.02237^{+0.00037}_{-0.00036}$	$0.02254^{+0.00037}_{-0.00036}$
$100\theta_{MC}$	$1.0448^{+0.0050}_{-0.0042}$	$1.0439^{+0.0040}_{-0.0033}$	$1.0475^{+0.0031}_{-0.0037}$	$1.0439^{+0.0047}_{-0.0034}$	$1.0437^{+0.0043}_{-0.0032}$	$1.0445^{+0.0045}_{-0.0035}$
τ	$0.053^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.054^{+0.017}_{-0.016}$	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.056^{+0.016}_{-0.015}$
n_s	$0.960^{+0.017}_{-0.018}$	$0.963^{+0.015}_{-0.015}$	$0.965^{+0.015}_{-0.014}$	$0.963^{+0.014}_{-0.014}$	$0.966^{+0.014}_{-0.013}$	$0.973^{+0.013}_{-0.013}$
$\ln(10^{10}A_s)$	$3.038^{+0.037}_{-0.036}$	$3.041^{+0.036}_{-0.035}$	$3.044^{+0.037}_{-0.036}$	$3.042^{+0.035}_{-0.034}$	$3.044^{+0.036}_{-0.035}$	$3.054^{+0.035}_{-0.034}$
w_x	< -0.76	< -0.81	< -0.902	< -0.79	< -0.79	< -0.823
ξ	< 0.27	< 0.24	$0.229^{+0.069}_{-0.090}$	$0.13^{+0.13}_{-0.12}$	< 0.24	$0.15^{+0.12}_{-0.11}$
Ω_{m0}	$0.19^{+0.16}_{-0.16}$	$0.21^{+0.11}_{-0.12}$	$0.092^{+0.082}_{-0.061}$	$0.21^{+0.11}_{-0.13}$	$0.22^{+0.10}_{-0.13}$	$0.17^{+0.10}_{-0.11}$
σ_8	$1.6^{+2.0}_{-1.1}$	$1.24^{+0.99}_{-0.61}$	$2.6^{+1.8}_{-1.5}$	$1.3^{+1.3}_{-0.7}$	$1.2^{+1.0}_{-0.6}$	$1.5^{+1.5}_{-0.8}$
$H_0[\text{km/s/Mpc}]$	$68.1^{+7.3}_{-7.5}$	$68.1^{+3.0}_{-2.9}$	$73.2^{+2.4}_{-2.5}$	$68.0^{+2.6}_{-2.5}$	$68.2^{+2.1}_{-2.1}$	$70.9^{+2.0}_{-1.9}$
N_{eff}	$2.92^{+0.38}_{-0.37}$	$2.97^{+0.35}_{-0.35}$	$3.04^{+0.34}_{-0.31}$	$3.00^{+0.32}_{-0.31}$	$3.03^{+0.32}_{-0.32}$	$3.23^{+0.30}_{-0.29}$
S_8	$1.07^{+0.51}_{-0.31}$	$0.97^{+0.31}_{-0.20}$	$1.31^{+0.40}_{-0.37}$	$0.99^{+0.39}_{-0.22}$	$0.96^{+0.32}_{-0.19}$	$1.04^{+0.43}_{-0.26}$

The effective number of relativistic degrees of freedom N_{eff} is perfectly consistent with its standard value $N_{\text{eff}} = 3.046$ [68,69] for all data set combinations considered here,

with mean values similar to those obtained in the $w_x < -1$ scenario. A freely varying effective number of neutrino species N_{eff} does not affect the directions of the correlations

FIG. 7. 95% C.L. constraints within the IDE + N_{eff} model in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

TABLE IX. 95% C.L. constraints within the IDE + M_ν + N_{eff} model in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

Parameters	CMB	CB	CR19	CPCC	CBPCC	CR19PCC
$\Omega_c h^2$	< 0.113	$0.070^{+0.049}_{-0.058}$	$\ll 0.061$	$0.074^{+0.046}_{-0.055}$	$0.077^{+0.045}_{-0.058}$	$0.064^{+0.046}_{-0.057}$
$\Omega_b h^2$	$0.02222^{+0.00046}_{-0.00045}$	$0.02231^{+0.00040}_{-0.00039}$	$0.02238^{+0.00039}_{-0.00036}$	$0.02232^{+0.00040}_{-0.00038}$	$0.02236^{+0.00036}_{-0.00035}$	$0.02254^{+0.00036}_{-0.00036}$
$100\theta_{MC}$	$1.0448^{+0.0049}_{-0.0042}$	$1.0442^{+0.0045}_{-0.0036}$	$1.0476^{+0.0030}_{-0.0034}$	$1.0439^{+0.0042}_{-0.0032}$	$1.0437^{+0.0044}_{-0.0032}$	$1.0444^{+0.0046}_{-0.0035}$
τ	$0.053^{+0.016}_{-0.016}$	$0.054^{+0.016}_{-0.016}$	$0.054^{+0.017}_{-0.016}$	$0.054^{+0.016}_{-0.015}$	$0.055^{+0.016}_{-0.015}$	$0.056^{+0.016}_{-0.015}$
n_s	$0.959^{+0.017}_{-0.017}$	$0.962^{+0.016}_{-0.015}$	$0.966^{+0.014}_{-0.014}$	$0.963^{+0.015}_{-0.015}$	$0.965^{+0.014}_{-0.013}$	$0.973^{+0.013}_{-0.013}$
$\ln(10^{10}A_s)$	$3.039^{+0.036}_{-0.036}$	$3.041^{+0.037}_{-0.036}$	$3.044^{+0.037}_{-0.037}$	$3.043^{+0.036}_{-0.036}$	$3.044^{+0.035}_{-0.034}$	$3.054^{+0.036}_{-0.034}$
w_x	< -0.75	< -0.80	< -0.90	< -0.80	< -0.79	< -0.818
ξ	< 0.28	< 0.26	$0.231^{+0.068}_{-0.086}$	< 0.25	< 0.24	$0.15^{+0.12}_{-0.11}$
Ω_{m0}	$0.19^{+0.16}_{-0.16}$	$0.20^{+0.12}_{-0.13}$	$0.091^{+0.075}_{-0.056}$	$0.21^{+0.11}_{-0.12}$	$0.22^{+0.10}_{-0.13}$	$0.17^{+0.10}_{-0.11}$
σ_8	$1.6^{+1.9}_{-1.1}$	$1.3^{+1.3}_{-0.7}$	$2.6^{+1.7}_{-1.5}$	$1.3^{+1.0}_{-0.6}$	$1.2^{+1.0}_{-0.6}$	$1.5^{+1.6}_{-0.9}$
H_0	$67.7^{+7.3}_{-7.4}$	$68.1^{+3.3}_{-2.9}$	$73.2^{+2.4}_{-2.4}$	$68.0^{+2.7}_{-2.6}$	$68.2^{+2.2}_{-2.1}$	$70.8^{+2.0}_{-1.9}$
M_ν	< 0.337	< 0.170	< 0.199	< 0.243	< 0.156	< 0.158
N_{eff}	$2.92^{+0.38}_{-0.37}$	$2.96^{+0.37}_{-0.35}$	$3.05^{+0.33}_{-0.32}$	$3.01^{+0.33}_{-0.32}$	$3.02^{+0.33}_{-0.30}$	$3.22^{+0.29}_{-0.29}$
$\Omega_\nu h^2$	< 0.0035	< 0.0018	< 0.0021	< 0.0026	< 0.0017	< 0.0017
S_8	$1.06^{+0.49}_{-0.30}$	$1.00^{+0.39}_{-0.23}$	$1.32^{+0.40}_{-0.38}$	$0.98^{+0.32}_{-0.20}$	$0.96^{+0.33}_{-0.20}$	$1.04^{+0.43}_{-0.26}$

FIG. 8. 95% C.L. constraints within the IDE + M_ν + N_{eff} in the quintessence-like dark energy scenario ($w_x > -1$) from several data set combinations, where CB, CR19, CPCC, CBPCC, and CR19PCC correspond to the combinations CMB + BAO, CMB + R19, CMB + Pantheon + CC, CMB + BAO + Pantheon + CC, and CMB + R19 + Pantheon + CC, respectively.

between the cosmological parameters, as we can see in Fig. 7, while the very strong correlation between N_{eff} and the Hubble constant H_0 present within the Λ CDM model is considerably reduced in this interacting scenario. The N_{eff} values obtained for the CMB + R19, CMB + Pantheon + CC, and CMB + BAO + Pantheon + CC data combinations are very similar and very close to 3. However, if we consider the CMB + R19 + Pantheon + CC data combination (see the last column of Table VIII), we obtain $N_{\text{eff}} = 3.23^{+0.30}_{-0.29}$ at 95% C.L.

4. IDE + M_ν + N_{eff} : Ten parameters

The results for this scenario are shown in Table IX and Fig. 8. In this full scenario, where both the total neutrino mass M_ν and the effective number of relativistic degrees of freedom N_{eff} vary simultaneously, both n_s and H_0 are shifted to lower values when compared to the previous IDE + N_{eff} model shown in Table VIII.

The upper limits on the total neutrino mass M_ν are only mildly relaxed with respect to the IDE + M_ν model shown in Table III for the CMB-only case, while they are slightly stronger for the CMB + Pantheon + CC data set combination. The most stringent upper limit we have on this parameter is obtained for the data set combination CMB + BAO + Pantheon + CC (see the sixth column of Table IX), for which $M_\nu < 0.156$ eV at 95% C.L.

V. SUMMARY

In this paper we have explored possible extensions of interacting dark energy, where the dark energy and dark matter fluids interact with each other. We have focused on the impact of such interactions on the dark radiation sector, allowing the neutrino mass and effective number of neutrino species to vary freely, both individually and simultaneously. The effect of such a dark coupling on the dark radiation sector was analyzed within two different dark energy regimes: a phantom scenario ($w_x < -1$) and a quintessence scenario ($w_x > -1$). We have exploited the most recent publicly available cosmological observations, which include the *Planck* 2018 legacy data, baryon acoustic oscillations, the most recent measurement of the Hubble

constant using Cepheids as calibrators, type Ia supernovae Pantheon data, and measurements of the Hubble parameter from cosmic chronometers. We found, in general, that the constraints on the dark radiation sector physics are quite close to those found within the minimal Λ CDM cosmology. The derived bounds are almost independent of the dark energy regime (phantom versus quintessence), contrary to the case without a dark coupling [71,72]. We found a total neutrino mass $M_\nu < 0.15$ eV and a number of effective relativistic degrees of freedom $N_{\text{eff}} = 3.03^{+0.33}_{-0.33}$, both at 95% C.L., which are indeed not that far from those obtained within the Λ CDM cosmology, $M_\nu < 0.12$ eV and $N_{\text{eff}} = 3.00^{+0.36}_{-0.35}$, for the same data combination. Current cosmological observations are therefore powerful enough to disentangle the physical effects associated with the different dark sector components, i.e., dark energy, dark matter, and dark radiation.

On the other hand, it might be interesting to investigate the mutual interaction scenario in the full dark sector of the Universe (namely, between dark energy, dark matter, and dark radiation) and consider different rates of interaction, and examine how such coupling can affect both the dark and neutrino sectors in light of recent cosmological observations.

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