

Unconventional Ferroelectric Switching via Local Domain Wall Motion in Multiferroic ε -Fe₂O₃ Films

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Deterministic polarization reversal in ferroelectric and multiferroic films is critical for their exploitation in nanoelectronic devices. While ferroelectricity has been studied for nearly a century, major discrepancies in the reported values of coercive fields and saturation polarization persist in literature for many materials. This raises questions about the atomic-scale mechanisms behind polarization reversal. Unconventional ferroelectric switching in ε -Fe₂O₃ films, a material that combines ferrimagnetism and ferroelectricity at room temperature, is reported. High-resolution in situ scanning transmission electron microscopy experiments and first-principles calculations demonstrate that polarization reversal in \mathcal{E} -Fe₂O₃ occurs around pre-existing domain walls only, triggering local domain wall motion in moderate electric fields of 250-500 kV cm⁻¹. Calculations indicate that the activation barrier for switching at domain walls is nearly a quarter of that corresponding to the most likely transition paths inside *E*-Fe₂O₃ domains. Moreover, domain walls provide symmetry lowering of the polar structure near the domain boundary, which is shown to be necessary for ferroelectric switching in E-Fe₂O₃. Local polarization reversal in \mathcal{E} -Fe₂O₃ limits the macroscopic ferroelectric response and offers important hints on how to tailor ferroelectric properties by domain structure design in other relevant ferroelectric materials.

symmetry (provided it belongs to the socalled polar classes),^[1] its switchability is a far more intricate matter. Indeed, polar materials which cannot be switched, like tourmaline, were already known as pyroelectrics in ancient times because, when heated or cooled, their temperaturedependent spontaneous electric dipole moments give rise to phenomena of electrostatic attraction. In contrast, ferroelectricity was not discovered until 1920,^[2] being belated by an essential feature of ferroelectrics; the existence of domains with opposite polarizations, which in asprepared crystals results in a zero net polarization.^[3] The response of ferroelectric domains under applied electric fields determines the characteristics of the polarization versus electric field hysteresis loops which are the quintessence of ferroelectrics and what makes them appealing for most applications. Despite intensive research efforts, we do not have, and might never have, a theory of polarization switching which encompasses all ferroelectrics. Since electric dipoles arise from

1. Introduction

A spontaneous polarization which can be switched by applying an electric field is a hallmark of ferroelectrics. While the spontaneous polarization of a crystal is bestowed by its point group

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the relative displacements of positive and negative ions in a crystal and changing their orientation involves a costly deformation of the crystal lattice in terms of elastic energy, the specific structural details can strongly affect the switching mechanism. For instance, many polarization reversal studies have focused

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on perovskites such as BaTiO₃. In this tetragonal structure, the reversal is easily explained by displacements of Ti⁴⁺ ions above or below the center of its coordination octahedra. However, in BiFeO₃, another perovskite with a rhombohedral distortion that has received much attention during the last decade, the polarization switching follows a non-obvious two-step path.^[4] To rev complicate matters further, ferroelectric switching can proceed wh through the growth of existing domains or with the nucleation of new domains and is strongly affected by the

domain geometry or the microstructure of the material. In this context, it is not surprising that the development path of new ferroelectric oxides beyond the prototypical perovskite family is often not a smooth one. This is particularly true in the case of ferroelectrics for which the energy cost of polarization switching is substantially larger compared to the perovskites, with coercive fields (E_c) in the order of MV cm⁻¹ instead of tens to hundreds of kV cm⁻¹. This is the case for LiNbO₃, which was thought to be non-switchable^[5] until its ferroelectricity was demonstrated on very thin specimens,^[6] and, more recently, doped hafnia.^[7] Another example is GaFeO₃, for a long time considered non-ferroelectric until it was prepared in the form of thin films and switched. The fact that GaFeO3 exhibits a Pna21 polar structure up to high temperatures (above 1350 K)^[8] indicates its high stability from which large coercive fields are to be expected. However, most ferroelectricity studies on GaFeO₃-type films^[9–17] report small to moderate E_c not larger than 500 kV cm⁻¹ with a significant dispersion in the values of remanent polarization (P_r) ranging from 0.2 μ C cm^{-2[13]} to 8 μC cm⁻².^[16] In contrast, Song et al. measured much larger E_c of 1.4 MV cm⁻¹ and P_r of 26 μ C cm⁻²,^[18] in good agreement with theoretical predictions.^[18-22]

Multiferroic ε -Fe₂O₃ is isostructural to GaFeO₃ and has attracted interest in recent years because it combines robust ferrimagnetism and ferroelectricity at room temperature.^[23,24] While experiments have demonstrated reversible ferroelectric switching in ε -Fe₂O₃ films at room temperature,^[24] the atomic-scale mechanism behind polarization reversal is still unclear. Moreover, as in the case of GaFeO₃, there are large discrepancies in the reported values of E_{c_1} which are as low as



60 kV cm $^{-1}$ (PUND method)^[24] and as large as 800 kV cm $^{-1}$ (piezoelectric force microscopy).^[16] Here, we provide an alternative explanation for the low P_r values reported on GaFeO₃-type ferroelectric films by using in situ scanning transmission electron microscopy (STEM) on ε -Fe₂O₃ films. Our measurements reveal partial switching of the domains at small electric fields which is only localized around pre-existing domain walls. We propose a mechanism of polarization reversal from first-principles calculations. This mechanism highlights the importance of the initial domain structure for the ferroelectric response of GaFeO3-type films and indicates the potential of domain structure design as a tool to lower the polarization reversal barrier or enhance the saturation polarization. In particular, our results can be important to the understanding of relevant ferroelectrics characterized by large coercive electric fields such as LiNbO3 or hafnia.

2. In Situ STEM Experiments

We performed in situ STEM experiments on 50 nm thick ε -Fe₂O₃ films. The films were grown by pulsed laser deposition (PLD) on an isostructural 8 nm thick AlFeO3 (AFO) buffer layer and a conducting (111)-oriented Nb-doped SrTiO₃ (STO) substrate (see Experimental Section for details). We mainly utilized STEM with a high-angle annular dark-field (HAADF) detector. This imaging mode allows recording of incoherent Z-contrast images, in which the intensity of an atomic column is approximately proportional to the square of the average atomic number (Z).^[25] Hence, Fe ions are resolved clearly. Figure 1 shows HAADF-STEM cross-sectional images and a selected area electron diffraction (SAED) pattern of an *ɛ*-Fe₂O₃ film on our in situ specimen holder with a piezo-controlled metallic tip. The ε -Fe₂O₃ and AFO films are epitaxial and their out-of-plane orientation relation with the STO substrate corresponds to $(001)_{\epsilon-Fe_2O_3}//(001)_{AFO}//(111)_{STO}$ (Figure 1b). The polar c axis of the ε -Fe₂O₃ Pna2₁ structure is thus oriented perpendicular to the film plane. The splitting of the film and substrate diffraction spots, as illustrated by the dashed yellow

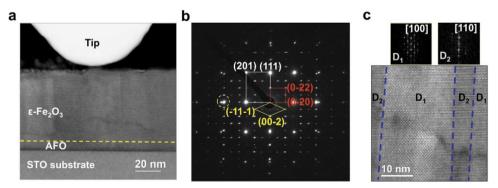


Figure 1. In situ STEM measurement geometry and structural characterization. a) Low magnification cross-sectional HAADF-STEM image of a 50 nm ε -Fe₂O₃/8 nm AFO/Nb-doped STO(111) specimen after establishing contact with a Pt/Ir tip of the piezo-controlled probing holder. The dashed yellow line marks the interface between the ε -Fe₂O₃ and AFO films. During in situ measurements, the Pt/Ir tip is grounded and voltage pulses are applied to the conducting STO substrate. b) SAED pattern of the sample. The pattern is indexed by considering a superposition of diffraction peaks along the zone axis [$\overline{112}$] of the STO substrate (white rectangle) and [100] and [110] of the ε -Fe₂O₃ film (red rectangle and yellow diamond). Splitting of the ε -Fe₂O₃ and STO diffraction spots (see dashed yellow circle) confirms relaxation of the ε -Fe₂O₃ film. c) Enlarged area of the ε -Fe₂O₃ thin film showing the presence of alternating D₁ and D₂ structural domains. The panels above the image show corresponding FFT patterns.

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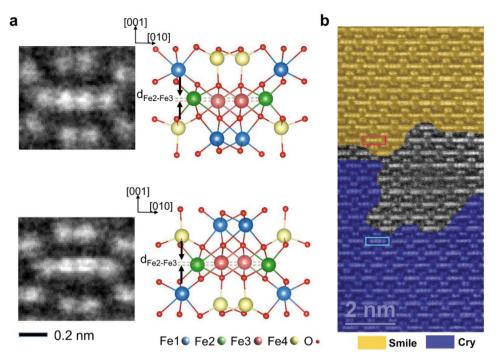


Figure 2. Ferroelectric domain structure. a) High-resolution HAADF-STEM images along the [100] zone axis of the ε -Fe₂O₃ film showing a smile (upper panel) and cry (lower panel) alignment of the Fe2 and Fe3 ions. The corresponding structural models are shown on the right. b) HAADF-STEM image of two polar domains in the ε -Fe₂O₃ film (yellow and blue areas) separated by a non-polar boundary (grey area). The red and cyan rectangles mark Fe ions whose relative positions are monitored during the application of electric field pulses (see Figure 3 for results).

circle in Figure 1b, indicates relaxation of the ε -Fe₂O₃ lattice with respect to the STO substrate. The microstructure of the ε -Fe₂O₃ film consists of alternating columnar domains with a width ranging from a few to tens of nanometers (Figure 1c). Fast Fourier transform (FFT) patterns and electron diffraction simulations (Figure S1, Supporting Information) indicate that the domains are oriented along the ε -Fe₂O₃ [100] and [110] crystal axes. Diffraction spots of these domains, which we label D₁ and D₂, are marked by a yellow diamond and red square in the SAED pattern of Figure 1b. The formation of structural domains with approximately equal probability is anticipated because of the pseudo sixfold symmetry in the (001) planes of AFO and ε -Fe₂O₃.^[24,26]

The unit cell of the ε -Fe₂O₃ Pna2₁ structure consists of four non-equivalent Fe³⁺ sites, as schematically illustrated in Figure 2a for a projection along the [100] crystal axis (D₁ domain). The ions labeled Fe1 and Fe2 exhibit a distorted octahedral coordination, while Fe4 ions are tetrahedral. Fe3 ions with regular octahedral coordination are located in the same plane as Fe2 ions, with slightly different coordinates along [001]. Because of this alignment in the [100] projection, it is possible to measure vertical displacements between Fe2 ions and Fe3 ions with high precision. For this reason, we focus our attention on the row with two Fe3 ions in the center and two Fe2 ions at the edges. In the polar *Pna2*₁ phase, the Fe2 ions are positioned either slightly above or below the Fe3 ions, depending on the direction of ferroelectric polarization (see structural models and HAADF-STEM images in Figure 2a). We refer to these two ionic configurations as "smile" and "cry", respectively. Figure 2b shows a high-resolution HAADF-STEM image of a D₁ domain

in the ε -Fe₂O₃ film. In the upper part of the image, the Fe2 and Fe3 ions form a smile structure, whereas cry configurations are measured in the lower part. For clarity, we colored the two polar domains yellow and blue (an uncolored image is shown in Figure S2, Supporting Information). In the middle of the image (grey area), the Fe2 and Fe3 ions are positioned on the same horizontal line within measurement error. This alignment suggests that the ε -Fe₂O₃ *Pna*2₁ unit cell has transformed into a centrosymmetric structure. Hence, we identify the grey area as a non-polar domain wall. To derive the vertical position of the Fe2 ions with respect to the Fe3 ions inside the polar domains, we used a 2D Gaussian fitting procedure. Averaging over ten unit cells, we find d_{Fe2-Fe3} = 6.1 ± 2.9 pm for the domain with smiles. A similar value but with opposite polarity is derived for the domain with cries (d_{Fe2-Fe3} = -8.5 ± 3.5 pm).

In order to image vertical displacements between Fe2 and Fe3 ions under an electric field, we contacted the ϵ -Fe₂O₃ film by the piezo-controlled metallic tip of our in situ probing holder (Figure 1a). In the in situ measurements, we grounded the tip and applied triangular voltage pulses with a duration of 0.1 s to a contact on the Nb-doped STO substrate (see Experimental Section for details). The pulse amplitude was swept and high-resolution images were recorded after applying voltages with opposite polarity. From a careful analysis of the HAADF-STEM images, we conclude that the Fe2 and Fe3 ions do not measurably shift inside the domains, that is, away from the domain wall, up to a pulse amplitude of 5 V. In the immediate vicinity of the wall, however, we observe reversible transpositions of Fe ions, turning smiles into cries and vice versa. **Figure 3**a shows snapshots from this experiment (full





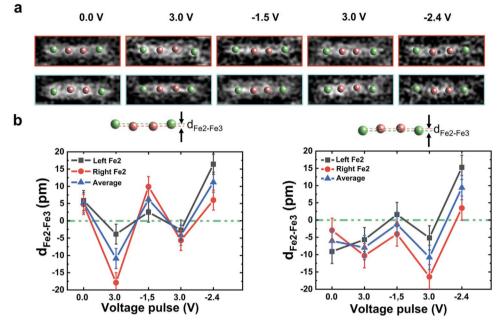


Figure 3. Electric-field-driven ion displacements. a) High-resolution HAADF-STEM images from selected areas in Figure 2b obtained after application of alternating positive and negative voltage pulses to the Nb-doped STO substrate. The positions of the Fe2 and Fe3 ions are determined by a Gaussian fitting procedure and marked by green and red dots, respectively. b) Summary of the relative vertical positions of the left Fe2 ion (grey data) and right Fe2 ion (red data) with respect to the average vertical position of the Fe3 ions after the application of positive and negative voltage pulses. The average d_{Fe2-Fe3} displacement is shown in blue. The left and right graphs show results for the red and cyan rectangles in Figure 2b. Positive values of d_{Fe2-Fe3} correspond to a smile, while negative values resemble a cry.

images are shown in Figure S3, Supporting Information). We focus on one unit cell above and another below the domain wall (marked by red and cyan rectangles in Figure 2b) and plot the relative positions of the two Fe2 ions with respect to the mean position of the two Fe3 ions (i.e., $d_{Fe2-Fe3}$). Applying a +3 V pulse turns the initial smile into a cry, while the initial cry remains practically unaltered. In contrast, negative voltage pulses turn cries into smiles. Since positive (negative) pulses move the positively charged Fe³⁺ ions up (down), our in situ results imply that the Fe3 ions move more than the Fe2 ions in an applied electric field. Moreover, from the bias polarity we derive that the ferroelectric polarization points up in the cry domain and down in the smile domain. The relative vertical displacement of the Fe2 and Fe3 ions near the domain boundary is consistent with the magnitude of smiles and cries inside the domains. This observation suggests that applying 1.5-3.0 V, corresponding to an electric field of 250-500 kV cm⁻¹, is sufficient to saturate the local polarization, in agreement with the polarization versus electric field hysteresis loop previously reported for this film.^[24]

At higher bias voltages, local polarization reversal leads to lateral motion of the domain wall. We illustrate this effect in **Figure 4**. The depicted HAADF-STEM images show how the cry domain with upward polarization grows at the expense of the smile domain when we apply positive voltage pulses of increasing amplitude to the Nb-doped STO substrate. This behavior, driven by local polarization reversal at the domain wall, produces a macroscopic ferroelectric response. Since ferroelectric switching does not encompass the entire sample (Figure S4, Supporting Information), we expect the magnitude of the macroscopic signal to be small compared to predictions based on published first-principles calculations. The restriction of polarization reversal to the vicinity of pre-existing domain walls might explain existing discrepancies between theory and experiments on ε -Fe₂O₃ and possibly GaFeO₃ in literature.

3. First-Principles Calculations

3.1. Ferroelectric Switching without Pre-Existing Domain Walls

A ferroelectric phase transition, be it of the displacive or of the order-disorder type, is typically characterized by small deviations of atomic positions in the polar structure from the corresponding sites in the centrosymmetric structure, which is considered as a reference. In both cases, the symmetry of the ferroelectric state is lower than the corresponding paraelectric one. For a typical ferroelectric, the polar state exists only below a certain critical temperature, above which the spontaneous polarization disappears. If the ferroelectric phase transition occurs at a temperature that is within measurement reach, the structure of the polar and non-polar states can be determined experimentally. This is very helpful in obtaining the transition coordinates and building the corresponding phenomenological and/or ab-initio models of the phase transition. Unfortunately, in the case of GaFeO₃ and ε -Fe₂O₃ the reference paraelectric phase is not known from experiments, leading to an ambiguity in the choice of the high-symmetry structure and in the corresponding calculated properties such as the value of the spontaneous polarization.





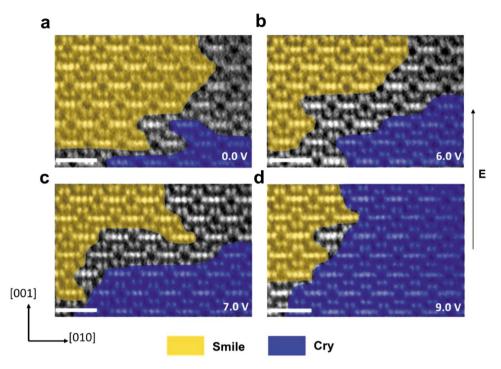


Figure 4. In situ STEM observation of the motion of a ferroelectric domain boundary. a–d) HAADF-STEM images showing the evolution of two polar domains during application of positive voltage pulses to the Nb-doped STO substrate. In the area with cries (blue) the polarization points up and in the area with smiles (yellow) it points down. Local polarization reversal near the non-polar boundary leads to domain wall motion. The scale bar corresponds to 1 nm.

Recent studies on ferroelectric switching in isostructural GaFeO3 considered the Pnna phase as the non-polar reference structure, yielding high energy barriers for ionic displacements.^[18-22] The choice for the Pnna structure was made by symmetry arguments, as a nearest centrosymmetric supergroup of the polar *Pna2*₁ one, achievable by small atomic displacements.^[19] Our in situ STEM experiments on *ɛ*-Fe₂O₃ films, however, indicate that ferroelectric switching occurs near domain walls at moderate electric fields. In order to understand this low-energy switching behavior we performed an ab initio-based search for alternative transition paths using an evolutionary algorithm, as implemented in USPEX code.^[27-30] Based on this analysis, we found a low-energy metastable centrosymmetric phase with monoclinic P2/c symmetry (Table 1). The P2/c phase is an elastically relaxed extension of the Pbcn structure (the latter was recently obtained by K. Xu et al. using a stochastic surface walking method^[31]) with frozen distortions according to the Γ_4^+ irreducible representation of *Pbcn* (Figure 5a-d). We estimate the potential barrier for ferroelectric switching via the Pbcn reference structure at 86 meV per f.u. (similar to 85 meV per f.u. obtained in ref. [31]), whereas ferroelectric switching inside a & Fe₂O₃ domain via the elastically relaxed P2/c structure results in a significantly lower energy barrier of 59 meV per f.u. (Figure 5e).

An examination of the Γ -point phonon structure reveals a dynamic instability in the *Pbcn* phase, with one polar phonon of imaginary frequency. Figures 5f,g show the eigendisplacements of Fe ions for the unstable phonon mode in *Pbcn*. Clearly, the eigendisplacements produce smile features similar to those in the STEM images of Figures 2–4, with Fe3 ions shifting down and Fe2 ions shifting up along the [001] direction. Freezing of

the unstable polar mode lowers the symmetry of the reference structure from non-polar *Pbcn* to polar *Pna2*₁. A decomposition

Table 1. Structural parameters of non-polar monoclinic P2/c andorthorhombic *Pbcn* reference structures.

Space group	Lattice constant, [Å]	Wyckoff position	X	Ŷ	Ζ
Ρ2/c	a = 9.60108	Fel 4g	0.21776	0.09929	0.28643
		Fe2 2f	0.5	0.27769	0.25
		Fe3 2f	0.5	-0.08640	0.25
	b = 8.71696	Fe4 4g	0.29853	0.39862	0.70943
		Fe5 2e	0.0	0.78847	0.25
	c = 5.04469	Fe6 2e	0.0	0.40230	0.25
	$\beta=96.32^\circ$				
		O1 4g	0.61657	-0.08336	-0.06784
		O2 4g	0.89069	0.58735	0.39074
		O3 4g	0.62095	0.76342	0.46437
		O4 4g	0.88562	0.74948	-0.09903
		O5 4g	0.86415	0.08207	0.88130
		O6 4g	0.62675	0.41975	0.43261
Pbcn	a = 9.59875	Fel 4c	0.0	0.09203	0.25
	b = 8.72242	Fe2 8d	0.21110	0.39648	0.24759
	c = 5.00751	Fe3 4c	0.0	0.71392	0.25
		O1 8d	0.61160	0.58726	0.58818
		O2 8d	0.61792	0.74270	0.06735
		O3 8d	0.86843	0.42188	0.59656





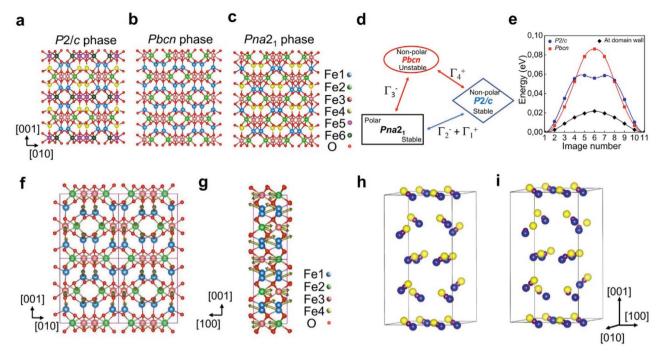


Figure 5. Fercelectric switching inside ε -Fe₂O₃ domains. a–c) Structural models of the *P2/c*, *Pbcn*, and *Pna*2₁ phases of ε -Fe₂O₃. d) Relations between the polar ground state and non-polar transition states of ε -Fe₂O₃. e) Calculated migration barriers for switching via *P2/c* and *Pbcn* reference structures inside a ε -Fe₂O₃ domain, as well as in the presence of a domain wall. Image numbers indicate intermediate images on the transition path between the initial and final states. f,g) Eigendisplacements of Fe ions (indicated by arrows) in the imaginary soft-mode of the non-polar *Pbcn* structure. The eigendisplacements of Fe ions in the low-energy phonon mode of the elastically relaxed *P2/c* structure are comparable to those shown here. Schemes of ferroelectric switching via h) *Pbcn* and i) *P2/c*. The view is along the [010] axis and, for clarity, only Fe ions are shown. The images depict two states with opposite polarization directions with blue and yellow spheres indicating ion positions in the states corresponding to the cry and smile features, respectively. The purple spheres represent the positions of ions in the transition state. The calculations show that all Fe ions move equivalently if switching proceeds though the *Pbcn* phase. In this case, the ions shift by ≈ 0.8 Å. For switching via the *P2/c* path in (i), the transposition of Fe ions is clearly asymmetric. Ions in the transition scorresponding to the cry features (blue spheres) in the uper half of the unit cell, whereas they are close to the positions corresponding to the smile features (yellow spheres) in its lower half. This means that only a part of the Fe ions displace during the first half of the transition and the remaining ions finalize the transition during the second half. The absolute displacement of Fe ions during switching via the *P2/c* path is similar to the *Pbcn* case, that is, ≈ 0.8 Å.

of real ion displacements during these structural conversions reveals the main contribution of the low energy Γ_3^- phonon, that is, its eigenvector completely defines the transition path for polarization switching. Although the phonon develops some polarization along the [001] direction in the reference non-polar structures (Figure 5f), ions mainly displace along the [100] direction, producing large antipolar components in neighboring chains (running along [001]) of Fe ions (Figure 5g). Consequently, polarization switching along [001] is accompanied by significant antipolar displacements of a large number of ions along [100] (Figure 5h). Since the displacements of Fe ions along the in-plane directions are not stabilized against thermal fluctuations by a perpendicular electric field, this fact could explain why switching within the ε -Fe₂O₃ domains is not observed in our in situ STEM experiments.

In contrast to *Pbcn*, all Γ -phonons are real in the *P2/c* structure. The eigenvector of the low-energy polar phonon mode in the *P2/c* phase exhibits all the main features of the imaginary mode vector of *Pbcn*. Consequently, the eigendisplacements of Fe ions are comparable for both structures. Decomposition of the real polar displacements in terms of eigendisplacements of the non-polar reference structure reveals the principal contribution of the polar Γ_2^- mode together with the

full-symmetry Γ_1^+ mode (Figure 5d). Coupling of these two modes produces a triple-well potential (Figure 5e), similar to the one in monoclinic Sn₂P₂S₆ uniaxial ferroelectrics.^[32] In the P2/c structure, the Fe1 sublattice of the Pbcn structure with tetrahedral coordination splits into two sublattices, one being tetrahedrally and the other octahedrally coordinated by oxygen ions (Figure 5a). Transformation to a polar phase from P2/c is therefore simpler than from Pbcn because it involves asymmetric ion displacements in only one half of the unit cell. To develop a smile feature starting from the P2/c structure (indicated by yellow spheres in Figure 5i), the largest displacements are performed by Fe ions with positions $z \ge$ 0.5 (compare distances between purple and yellow spheres), whereas Fe ions with $z \le 0.5$ displace most during the formation of a cry feature (compare distances between purple and blue spheres). This displacement pattern is consistent with the eigendisplacements of the phonon mode with lowest energy. As a result, the non-polar P2/c structure transforms to the polar Pc structure. However, because elastic relaxations decrease the monoclinic angle to zero, the system finally settles in the Pna21 orthorhombic polar phase. Therefore, in order to switch the polarization via the P2/c reference structure one has to break the symmetry in such a way that the

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Table 2. Calculated piezoelectric tensor (in 10^{-12} C/N) of $\epsilon\text{-}Fe_2O_3$ in $\textit{Pna2}_1$ crystallographic setting.

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dij	1	2	3	4	5	6
1					7.84	
2				1.31		
3	-0.178	-3.18	4.23			

angle between the *a* and *c* axes of $Pna2_1$ becomes monoclinic, which requires an ε_5 shear strain component.

In summary, one can formulate several reasons why ferroelectric switching inside *ɛ*-Fe₂O₃ domains is not observed in electric fields of up to 2 MV cm⁻¹ (maximum electric field in our in situ STEM experiments): i) The low-energy path for switching goes via the non-polar P2/c state. Since this transition state has lower symmetry than the initial *Pna2*₁ polar phase, the symmetry of Pna21 needs to be lowered during switching. In particular, this requires breaking of the glide plane symmetry orthogonal to [100]. This could be achieved by an elastic deformation ε_5 via the piezoelectric tensor component d_{51} , which we found to be significant in *ɛ*-Fe₂O₃ (see Table 2). However, in this scenario the electric field should have a [100] in-plane component, which is not the case for the out-of-plane geometry used in our experiment. ii) One can consider Pbcn as a virtual centrosymmetric reference structure with a higher transition barrier than P2/c, but also in this scenario the main component of the phonon mode that drives the transition lies along [100], that is, perpendicular to the applied electric field. The out-ofphase ion displacements along [100] are fully symmetric due to glide plane symmetry. Hence, one can consider ferroelectric switching in ε -Fe₂O₃ as a side-product of antiferroelectric ion displacements along the [100] axis. Reversal of the displacements along [100] will reverse also the net polarization along [001]. The estimated ratio of Fe ion displacements along [100] and [001] is about ≈3.5 for Fe1 and Fe4, ≈4.2 for Fe3, and ≈8.7 for Fe2 ions. For oxygen ions the corresponding ratio varies from \approx 2.4 to \approx 23. These numbers suggest that only a very high out-of-plane electric field component would produce the corresponding in-plane displacements, which could be well beyond dielectric breakdown of the material. Again, also here an inplane electric field component along the [100] direction would assist in ferroelectric switching.

3.2. Ferroelectric Switching with Pre-Existing Domain Walls

Next, we discuss the role of domain walls in ferroelectric switching. The metastable non-polar P2/c structure could exist as an extended phase or appear as a non-polar domain wall between ferroelectric domains with opposite polarizations. As can be seen from the triple-well potential for switching via the P2/c path (Figure 5e), the barrier from the non-polar to the polar phase is very small (\approx 1 meV per f.u.). Hence, the P2/c state is not stable in its free-standing form. However, the structure could be realized between head-to-head or tail-to-tail domains, as observed experimentally in the STEM image of Figure 2b (domain stacking along the [001] direction). Because of its significant monoclinic distortion (Table 1), it is unlikely

that the P2/c phase separates orthorhombic domains that are stacked along the [010] direction and polarized along [001]. In this geometry, which we observe also in experiments (Figure 4), we expect the domain wall to have an orthorhombic structure, probably with lower symmetry than *Pbcn*.

To analyze the effect of domain walls on ferroelectric switching, we consider a vertical wall separating two polar *Pna2*¹ domains wherein the polarization points down (smiles) and up (cries), respectively (Figure 6a). In contrast to switching via Pbcn and P2/c structures inside a ε -Fe₂O₃ domain where Fe1 and Fe4 ions occupy octahedral and tetrahedral sites in the initial Pna21 phase, respectively (Figure 5c), the unit cell of the modeled domain wall is altered by cross-substituting one tetrahedrally coordinated Fe4 ion with an octahedral Fe ion and one octahedrally coordinated Fe1 ion with a tetrahedral Fe ion (see green-shaded areas in the "wall" region as well as the lightorange and dark-blue triangles in Figure 6a). These substitutions break the glide plane symmetry orthogonal to the [100] axis, symmetrize the hexagon formed by the Fe2-Fe4-Fe2-Fe1-Fe1 ions (see thin black lines in Figure 6a,b), and align the Fe2 and Fe3 ions along the [001] directions within the domain wall. HAADF-STEM simulations of this domain wall configuration shown in Figure S5, Supporting Information indicate that smile and cry features are indeed not expected to appear in the domain wall, in agreement with the STEM images of Figures 2 and 4. By moving the domain as a whole unit along the [010] direction, we estimate an energy barrier of ≈22 meV per f.u., which is significantly lower than that estimated for ferroelectric switching inside a ε -Fe₂O₃ domain (Figure 5e). Detailed analysis of the calculations shows that one of the octahedral Fe1 ions swaps to a tetrahedral surrounding and one of the tetrahedral Fe4 ions swaps to an octahedral surrounding during the lateral domain wall translation (see the green-shaded and light-orange areas in Figure 6a,b). Next, the second Fe1 and Fe4 ions undergo the same coordination modification. Coincidently, the cry feature transforms into a smile feature via an intermediate phase by vertical transpositions of Fe2 and Fe3 ions if the domain wall moves from left to right. This observation is in excellent agreement with our in situ STEM measurements of voltage-induced motion of non-polar domain walls (Figure 4). Figure 6c shows the displacements of Fe ions along the [100] direction across a domain wall. The Fe2 and Fe3 ions displace gradually in the vicinity of the wall, undergoing only small transpositions upon domain wall motion. From the eight Fe ions taking part in ferroelectric switching via lateral wall motion, the ions on the Fe1 and Fe4 sites displace most. Their displacement is ≈0.4 Å, which is only half compared to switching inside a ε -Fe₂O₃ domain. Consequently, the energy barrier of domain wall assisted switching is significantly smaller than that of switching inside *ɛ*-Fe₂O₃ domains if the walls pre-exist. If the domain walls need to form first, an extra price has to be paid. For a discussion on the influence of lattice deformations on the energy barrier of ferroelectric switching, we refer to Figures S6 and S7, Supporting Information.

In addition to the vertical domain wall, we considered an inclined domain wall (Figure S8, Supporting Information), which is also visible in the STEM images (Figure 4). As in the vertical wall, the domains are stacked along the [010] direction, but the inclined wall is not orthogonal to [010]. We find that





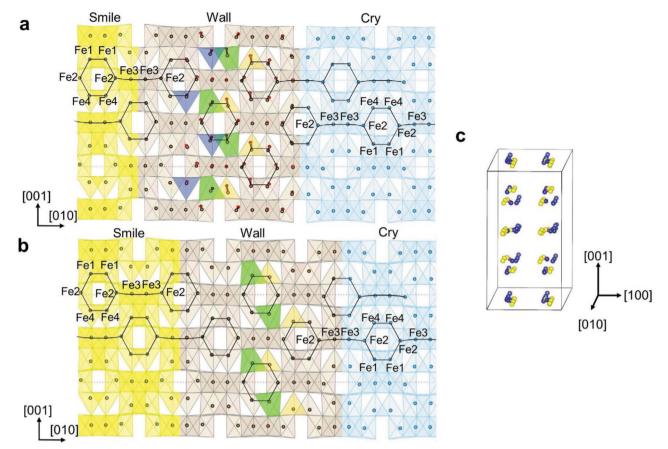


Figure 6. Model of a 180° domain wall separating two polar $Pna2_1$ domains (Figure 5c) with opposite polarization. The domains are stacked along the [010] direction. For clarity, only Fe ions are depicted. a,b) View of the domain wall along the [100] direction. Thin grey lines represent the oxygen polyhedra. The yellow and blue areas mark smile and cry domains. Thin black lines are a guide to the eye, connecting Fe ions to highlight the smiles and cries, as well as the hexagon arrangements of Fe1-Fe2-Fe4 ions. The domain wall is shaded grey. In the middle of the domain wall, selected Fe ions (green-shaded) exhibit octahedral coordination, as in the P2/c phase (Figure 5a). Ions with tetrahedral coordination on both sides of the hexagon, as in the *Pbcn* phase (Figure 5b), are marked by light-orange and dark-blue triangles. Feroelectric switching involves the swapping of the Fe1 (in octahedral coordination) and Fe4 (in tetrahedral coordination) sublattices, which is achieved by lateral motion of the non-polar domain wall along the [010] direction. When the domain wall moves to the right (panel b shows the final position of the translated domain wall), the Fe4 ions in the light-orange triangles displace most. Motion to the left, displaces the Fe4 ions in the dark-blue triangles most (not shown). Smaller relative displacements of the Fe2 and Fe3 ions produce the smile and cry features. The red arrows depict the displacement of all Fe ions. The arrow size is proportional to the ion displacement from the initial (a) to final (b) state during domain wall assisted feroelectric switching. Ion positions in the cry, smile, and transition states are indicated by blue, yellow, and purple colored spheres, respectively. The maximum Fe ion displacement during switching is ≈ 0.4 Å. The ions displace most along the [100] direction, that is, in the direction perpendicular to the applied electric field, highlighting the unconventional nature of ferroelectric switching in ϵ -Fe₂O₃.

in contrast to the vertical domain wall, the inclined domain wall preserves the orthogonal to [100] glide plane symmetry. Therefore, taking into account the above mentioned arguments, we do not expect that this wall plays a role in polarization switching. Unfortunately, the estimated formation energy of the inclined wall is significantly smaller than that of the vertical wall, $E_{\rm f}^{\rm inclined} = 234$ mJ m⁻² versus $E_{\rm f}^{\rm vertical} = 370$ mJ m⁻². This could lead to a transformation of vertical walls into inclined walls during switching, which would result in the disappearance of the ferroelectric response. In both cases, the formation energy is much higher than in the conventional ferroelectrics (e.g., ≈ 10 mJ m⁻² in BaTiO₃^[33]). It is even higher than the most energy expensive 180° domain wall in PbTiO₃ (≈ 169 mJ m^{-2[33]}). This makes the nucleation of domains with opposite polarization very difficult and explains the lack of

ferroelectric switching inside ε -Fe₂O₃ domains. To generate a ferroelectric response in ε -Fe₂O₃, one has to grow thin films with pre-engineered domain walls.

4. Conclusions

We combined in situ STEM experiments and first-principles calculations to elucidate the origin of ferroelectric switching in multiferroic ε -Fe₂O₃ films. We find that ferroelectric switching proceeds locally via the motion of non-polar boundaries. During switching, the polar state of the *Pna*2₁ structure transforms via an intermediate non-polar *P2/c* or *Pbcn* structure. The centrosymmetric *P2/c* transition state has lower symmetry than the polar *Pna*2₁ structure. Therefore,



the phase transition in ε -Fe₂O₃ differs from that in conventional ferroelectrics, like, for example, BaTiO₃, where the lowsymmetry polar structure is described by a subgroup of the high-symmetry paraelectric reference phase. To enable ferroelectric switching in ε -Fe₂O₃ via the P2/c reference structure, one first has to lower the symmetry of the polar starting point. This can be achieved with an electric field in the [100] direction via the d₅₁ piezoelectric component assisting the switching process or at domain walls that lower the symmetry. Since the presence of domain boundaries also significantly reduces the energy barrier of this phase transition, we experimentally measure a local ferroelectric response at moderate electric fields of 250-500 kV cm⁻² in samples with pre-existing domains. There are several reasons why ferroelectric switching by a perpendicular electric field inside ε -Fe₂O₃ domains does not occur; the activation barrier for switching is almost four times higher in domains than at pre-existing domain walls, switching involves significant antipolar ionic displacements within the film plane, that is, perpendicular to the [001] polar axis and external electric field, and the formation energy of domain walls in ε -Fe₂O₃ is much higher than that for conventional ferroelectrics. The unconventional, local nature of polarization reversal provides a viable explanation for discrepancies in the reported values of coercive field and saturation polarization for ε -Fe₂O₃ and isostructural GaFeO₃. We argue that similar atomic-scale mechanisms may also be at play in other relevant ferroelectric materials, especially those with large activation barriers.

5. Experimental Section

Film Growth: ε -AlFeO₃/ ε -Fe₂O₃ films were grown by PLD using a KrF excimer laser (248 nm wavelength, 25 ns pulse duration) at 5 Hz repetition rate on Nb-doped (0.5%) (111)-oriented SrTiO₃ (STO) single crystals at 825 °C, as described in more detail in ref. [24]. For the present study, the film on which the ferroelectric characterization reported in ref. [24] was previously studied was employed.

In Situ STEM Experiments: High-resolution in situ imaging of ion displacements in ε -Fe₂O₃ thin films was carried out on an aberrationcorrected JEOL 2200FS TEM using a piezo-controlled in situ biasing holder (HE150 electrical probing holder with double-tilt capability from Nanofactory AB). Wedge-shaped TEM specimens were prepared by a mechanical polishing process and argon ion milling (for details see ref. [34]). Silver paste was used for making good electrical contacts to the Nb-doped STO substrate after gluing the specimen to a half Cu TEM grid. As top electrode, The piezo-controlled Pt/Ir tip of the probing holder was exploited (Figure 1a). This tip contacted the sample over a length of about 30 nm. During in situ STEM measurements, the tip was grounded and triangular voltage pulses were applied to the Nb-doped STO substrate. The duration of the voltage pulses was set to 0.1 s and their magnitude was continuously swept in 0.1 V steps.

First-Principles Calculations: For structural predictions, the USPEX code was employed,^[27–30] which is based on an evolutionary algorithm. The USPEX method searches for the global ground state structure, but produces a series of metastable states as by-product, being therefore suited also for searching all possible metastable polymorphs. This method was applied to search for the low-energy metastable centrosymmetric structure of ε -Fe₂O₃. A 40-atoms unit cell of ε -Fe₂O₃ was considered. Each individual structure was relaxed by means of the Vienna ab-initio simulation package,^[35–37] with projector augmented wave pseudopotentials.^[38] The following valence-electron configurations $3p^{6}3d^{7}4s^{1}$ for Fe and $2s^{2}2p^{4}$ for oxygen were considered. Ground-state



properties were obtained using the generalized gradient approximation (PBEsol) adopted for solids. $^{\left[39\right] }$

To correctly account for strong electron correlation effects on the d shell of Fe atoms, a DFT+U scheme was used.^[40] On-site Coulomb parameter U = 4.0 eV and Hund's exchange J = 0.89 eV were used. The kinetic energy cutoff was set to 600 eV. For Brillouin zone sampling, uniform Γ -centered meshes with a reciprocal-space resolution of $2\pi \times 0.05$ Å⁻¹ were used. All energies were converged to within 10^{-6} eV per cell. The stopping criterion for structural relaxation was a change in (free) energy smaller than 1 meV.

Searches for metastable structures with the USPEX code were made by assuming ferromagnetic ordering on all Fe atoms in order to make energy comparisons of different structures independent of possible magnetic configurations. Total energy for the resulting low-energy structures as well as phonon calculations were performed with proper antiferromagnetic alignments of the spins.

For phonon calculations, the obtained structures were optimized with residual forces below 0.002 eV Å⁻¹. The Brillouin zone was sampled with 4 × 4 × 4 Monkhorst-Pack Γ -centered special k-point grids for *P2/c* and *Pbcn* structures. Calculations of dynamical properties were performed using the force-constant method.^[41] Eigenvalues and eigenvectors of the long-wavelength phonons were calculated at the Γ -point of the Brillouin zone and, therefore, no supercells were used. The Hellman-Feynman forces were calculated for displacements of atoms of up to 0.04 Å. The dynamical matrix was constructed by Fourier transforming the force constant calculated at the Γ -point. The phonon-mode frequencies and eigenvectors of the dynamical matrix.

Domain wall movements were simulated in a 320 atom supercell, which consisted of two equivalent domains with opposite direction of polarization. Ferromagnetic ordering on all Fe atoms was imposed for initial and final states as well as for all images along the transition path to avoid possible uncontrolled flips of spins on individual atoms during nudged elastic band calculations.

Transition energy barriers were calculated with a variable cell nudged elastic band as implemented in USPEX code.^[42] Crystallographic codes AMPLIMODE^[43] and FINDSYM^[44] were used for symmetry analysis of the obtained phases and their relations, as well as VESTA code^[45] for visualization of obtained results.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Keywords

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