

Oxygen fractionation in dense molecular clouds

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ABSTRACT

We have developed the first gas-grain chemical model for oxygen fractionation (also including sulphur fractionation) in dense molecular clouds, demonstrating that gas-phase chemistry generates variable oxygen fractionation levels, with a particularly strong effect for NO, SO, O₂, and SO₂. This large effect is due to the efficiency of the neutral ¹⁸O + NO, ¹⁸O + SO, and ¹⁸O + O₂ exchange reactions. The modeling results were compared to new and existing observed isotopic ratios in a selection of cold cores. The good agreement between model and observations requires that the gas-phase abundance of neutral oxygen atoms is large in the observed regions. The S¹⁶O/S¹⁸O ratio is predicted to vary substantially over time showing that it can be used as a sensitive chemical proxy for matter evolution in dense molecular clouds.

Keywords: ISM: abundances, ISM: clouds, Physical Data and Processes: astrochemistry

1 INTRODUCTION

To understand the transformation of matter from gas and dust present in the interstellar medium to the formation of planetary systems, a precise understanding of the nature and abundance of the various species present prior to cloud collapse is required. With the exception of CO and minor species in the gas phase and a few species on interstellar ices, the exact chemical composition of molecular clouds is still unknown. This is due, in particular, to the difficulty to detect species without a dipole moment (such as O₂ and N₂). It is unknown, for example, what fraction of elemental oxygen remains in atomic form in the gas-phase compared with the fraction that is contained in oxygen bearing molecules in the gas or in ices (in the form of H₂O, CO, CO₂, H₂CO, and/or CH₃OH). One possible method to address this question is to investigate the isotopic composition of the various molecules present, to determine the relative abundances of the various isotopologues. In dense molecular clouds, photons play a relatively small role and induce very few ¹⁸O fractionation effects as a result of CO self-shielding (Lyons & Young 2005, Smith et al. 2009). In this case, the most efficient fractionation pathways are exothermic barrierless reactions involving major species (C⁺, C, O, CO), with the zero-point energy (ZPE) differences in isotopologues driving the fractionation process. Then, the isotopic fractionations are directly linked to the abundance of the elements in the gas-phase when efficient fractionation reactions exist.

Among the various fractionations, hydrogen (deuterium), nitrogen, and carbon have received the most attention (Terzieva & Herbst 2000, Furuya et al. 2011, Pagani et al. 2011, Pagani et al. 2012, Roueff et al. 2015, Furuya & Aikawa 2018), but oxygen fractionation itself has been less well studied. The previous oxygen isotope studies concern mostly the minor isotopologues of CO, (¹³CO, C¹⁷O, and C¹⁸O) to probe the molecular content of clouds as the emission lines of ¹²C¹⁶O are fully saturated. In addition, ¹³C¹⁸O and ¹²C¹⁸O have also been used to determine the ¹²C/¹³C ratio in CO assuming a given ¹⁶O/¹⁸O ratio (Ikeda et al. 2002). The ¹⁶O/¹⁸O ratio across the Galaxy has been derived from the H₂C¹⁶O/H₂C¹⁸O ratio assuming no fractionation in H₂CO (Wilson 1999). This leads to a local ¹⁶O/¹⁸O ISM value equal to 557 ± 30 (Wilson 1999), close to the Solar System value of 530 for the Solar wind (McKeegan et al. 2011) or 511 ± 10 for the sun's photosphere (Ayres et al. 2013), and around 500 for comets (Bockelée-Morvan et al. 2012, Jehin et al. 2009) and meteorites (Lodders 2003). The ¹⁶O/¹⁸O ratio in diffuse molecular clouds is estimated to be equal to 672 ± 110 from the HC¹⁶O⁺/HC¹⁸O⁺ ratio (Lucas & Liszt 1998). Apart from H₂CO, CO and its protonated form HCO⁺, there are

only a few other scattered detections such as ^{18}OCS , S^{18}O , SO^{18}O observations in Orion KL (Tercero et al. 2010, Esplugues et al. 2013), leading to lower apparent $^{16}\text{O}/^{18}\text{O}$ ratios than the local ISM value. Despite the oxygen isotope anomalies in solar-system materials (McKeegan et al. 2011), the role of H_2CO to determine the $^{16}\text{O}/^{18}\text{O}$ ratio and the anomalous results for ^{18}OCS , S^{18}O and SO^{18}O in Orion KL, no model has been developed to calculate the oxygen fractionation of these molecules. Indeed, the only ^{18}O fractionation model, developed by Langer et al. (1984), considers only a few isotopologues and only one fractionation reaction, namely



To understand the mechanisms leading to oxygen fractionation, we have developed a new gas-grain model for dense molecular clouds (that do not contain efficient photodissociation processes). After an exhaustive search, we have introduced various oxygen fractionation reactions, which induce notable fractionation effects for molecules such as NO , SO , O_2 and SO_2 . We have also determined the observed isotopic ratios for these species in a number of cold core using existing spectral surveys. To interpret these observations, we have also added reactions for the isotopic fraction of sulphur to the network. The chemical model including the various updates and the model predictions are presented in Section 2. In section 3, the new observed isotopic ratios and their comparison with the model predictions are shown. Our conclusions are presented in Section 4.

2 CHEMICAL MODELLING

2.1 Model description

Our chemical model is based on Nautilus in its 3-phase version (Ruaud et al. 2016) using *kida.uva.2014* (Wakelam et al. 2015), with updates from Ruaud et al. (2015), Wakelam et al. (2017), Hincelin et al. (2015) and Loison et al. (2016), Loison et al. (2017), Vidal et al. (2017) for the chemistry. The network used here is limited to a carbon skeleton up to $\text{C}_3\text{H}_x\text{N}_y$ ($x = 0-2$, $y=0-1$) and $\text{C}_3\text{H}_x\text{N}_y^+$ ($x = 0-3$, $y=0-1$) to reduce the number of reactions when considering all the ^{18}O and ^{34}S species. It includes 4440 reactions in the gas phase and 5180 reactions on grains. We have checked that the new network reproduces the abundances of the complete network for the main species studied here. The chemical composition of the gas-phase and the grain surfaces is computed as a function of time. The gas and dust temperatures are equal to 10 K, the H_2 density is equal to $2 \times 10^4 \text{ cm}^{-3}$ (various runs have been performed with the H_2 density varied between $1 \times 10^4 \text{ cm}^{-3}$ and $2 \times 10^5 \text{ cm}^{-3}$). The temperature and the H_2 density is kept constant during chemical cloud evolution. The cosmic-ray ionization rate is equal to $1.3 \times 10^{-17} \text{ s}^{-1}$ and the value

of the total visual extinction is set to 10. All elements are assumed to be initially in atomic form except for hydrogen, which is entirely molecular. Elements with an ionization potential below the maximum energy of ambient UV photons (13.6 eV, the ionization energy of H atoms), C, S and Fe, are initially in a singly ionized state. The initial abundances are reported in Table 1, the C/O elemental ratio being equal to 0.7 while sulphur is depleted by a factor of 10 (Fuente et al. 2016, Vidal et al. 2017, Fuente et al. 2018). Although this represents a simplistic approach to molecular cloud modeling, neglecting the structure and the history of the cloud, the main objective of this study is to demonstrate the importance of the chemistry on oxygen fractionation. Nevertheless, we performed different runs to test some of the approximations on the fractionation. First, we performed a run with an initial abundance of CO equal to 8.5×10^{-5} and an initial abundance of C also equal to 8.5×10^{-5} (in the nominal model the initial abundance of CO is equal to 0 and the initial abundance of C is equal to 1.7×10^{-4}). An initial abundance of CO equal to 8.5×10^{-5} represents 35% of the elemental oxygen abundance. The global results of calculations are similar to the nominal model except if we start with an initial $C^{16}O/C^{18}O$ ratio different from the local ISM $^{16}O/^{18}O$ ratio (for example with an initial $C^{16}O$ equal to 8.5×10^{-5} but without $C^{18}O$, all the ^{18}O being under the atomic form). This may happen if the photodissociation of CO in the first part of cloud evolution (diffuse H I cloud where UV radiation effects are important) leads to complete $C^{18}O$ photodissociation but not for $C^{16}O$ due to self-shielding. Then, the initial $^{16}O/^{18}O$ ratio may be smaller than the local ISM value, with some ^{16}O being locked into $C^{16}O$. However, if 35% of elemental oxygen is initially in the form of $C^{16}O$ with no $C^{18}O$ (then with a ratio $^{16}O/^{18}O$ of 320 for atomic oxygen in the gas-phase instead of 500) we cannot reproduce the strong ^{18}O enrichment of SO if we do not consider the exchange reactions. Moreover, almost all the oxygenated species, apart from CO and methanol, are moderately enriched in ^{18}O . We also performed runs varying the total density. The main effect of increasing the total density is to increase the efficiency of the chemistry because the fluxes of the chemical reactions are proportional to the densities of the reactants. However, variation of the total density leads to only minor effects on the chemistry. It should be noted, however, that $S^{18}O$ fractionation is slightly more efficient with a higher total density.

In our model, there are some photons generated by the relaxation of excited H_2 (produced by electron collisions with H_2) (Prasad & Tarafdar 1983, Gredel et al. 1989). These photons have however only a small effect. Moreover, as we do not consider the photochemical boundary of the molecular cloud, the photodissociation of CO should not play a major role and we do not consider potential self-shielding effects (Lyons & Young 2005, Smith et al. 2009).

Table 1. Elemental abundances with respect to hydrogen nuclei.

Element	Abundance
He	0.09
C	1.7e-4
N	6.2e-5
O (¹⁶ O)	2.4e-4
¹⁸ O	4.81e-7
¹⁶ O/ ¹⁸ O	499
S (³² S)	1.5e-6 (factor 10 of depletion)
³⁴ S	6.67e-7 (factor 10 of depletion)
³² S/ ³⁴ S	22.5
Fe	1.00e-8

2.2 ¹⁸O and ³⁴S exchange reactions

In the interstellar medium, fractionation occurs due to the fact that zero-point energy (ZPE) differences favor the exothermic pathway for barrierless exchange reactions. The rate constants for the fractionation reactions have been studied in detail (Terzieva & Herbst 2000, Roueff et al. 2015). Using the work of Henchman and Paulson (1989), we consider in this work that all reactions involve adduct formation. We also consider only reactions without bimolecular exit channels except for exchange reactions because when there is one, or several exothermic bimolecular exit channels, they are likely to be favored. Then, assuming that the adduct lifetime is long enough to have a statistical energy distribution, we can consider that $k_f + k_r = k_\infty$ (k_∞ is the high-pressure rate constant) (Anderson et al. 1985, Terzieva & Herbst 2000, Roueff et al. 2015).

Then

$$k_f = \alpha \times (T/300)^\beta \times f(B,m) / (f(B,m) + \exp(\Delta E/T)),$$

$$k_r = \alpha \times (T/300)^\beta \times \exp(\Delta E/T) / (f(B,m) + \exp(\Delta E/T))$$

with: k_f is the rate constant for the forward reaction, that is reaction towards the right in Table 2, k_r is the rate constant for the reverse reaction, that is reaction towards the left in Table 2, α is in $\text{cm}^3 \cdot \text{molecule}^{-1} \cdot \text{s}^{-1}$, β is without units. $f(B,m)$, which depends on the rotational constants (B), masses (m) and symmetries of the reactants (Terzieva & Herbst 2000), is close to 1 except when O_2 or S_2 is involved in the reaction. ΔE is the exothermicity of the reaction in Kelvin and is equal to the Zero Point Energy (ZPE) differences. This exothermicity is calculated using vibrational data in the literature when it exists. For some isotopologues, vibrational frequencies are unknown. We then calculated the vibrational frequencies for all isotopologues with Density Functional Theory (DFT) at the M06-2X/AVTZ level using Gaussian 09 software (Frisch et al. 2009) and we scaled the theoretical values to the experimental ones for the main isotopologues.

When no data exist on the association reaction, we use the capture rate constant to determine the value of $k_f + k_r$ for barrierless reactions. It should be noted that this formalism seems to be inappropriate for the $^{18}\text{O} + \text{O}_2$ reaction (Anderson et al. 1985, Wiegell et al. 1997, Fleurat-Lessard et al. 2003, Rajagopala Rao et al. 2015). For this reaction, there are no experimental data at low temperature and the theoretical studies are not in good agreement with experiment in the 150-350 K range. Then the $^{18}\text{O} + \text{O}_2$ exchange rate constant is uncertain at low temperature (up to a factor 10), leading to large uncertainties for O_2 fractionation only.

Among the oxygen fractionation reactions, two of them play critical roles, $^{18}\text{O} + \text{NO}$ and $^{18}\text{O} + \text{SO}$. For the $^{18}\text{O} + \text{NO}$ reaction there are direct measurements of isotope exchange (Fernando & Smith 1979, Fernando & Smith 1981, Anderson et al. 1985, Cobos & Troe 1985, W. M. Smith 1997), where the rate of exchange is in good agreement with the high pressure rate constant considering an indirect mechanism (Hippler et al. 1975, Fernando & Smith 1979, Baulch et al. 2005). For the $^{18}\text{O} + \text{SO}$ reaction there are no direct measurements of the isotope exchange reaction but as the association reaction, $\text{O} + \text{SO} \rightarrow \text{SO}_2$ is very exothermic, the lifetime of the excited SO_2^{**} formed should be long enough to apply statistical theory and we use $k_f + k_r = k_\infty$ with k_∞ given by experimental studies (Lu et al. 2003, Cobos et al. 1985). Then for the $^{18}\text{O} + \text{SO} \rightarrow \text{O} + \text{S}^{18}\text{O}$ rate constant we use the experimental high-pressure value, with SO_2 production being negligible at the pressure of dense molecular clouds. The uncertainty of the rate coefficient for the $^{18}\text{O} + \text{NO}$ and $^{18}\text{O} + \text{SO}$ exchange reactions should be close to 30% at room temperature and can be as high as a factor 2 at low temperature.

For sulphur fractionation, the $\text{S}^+ + \text{SO}$ and $\text{S} + \text{SO}$ reactions may play a role in ^{34}S fractionation. For $\text{S}^+ + \text{SO}$ we neglect the exchange reaction (exothermic by 8.7 K) as there are exothermic bimolecular exit channels, namely the slightly exothermic $\text{S}_2^+ + \text{O}$ channel (exothermic by 153 K) and the charge transfer reaction (exothermic by 766 K). When we perform a test considering that only the exchange reaction occurs, we observe no effect on SO fractionation. For $\text{S} + \text{SO}$ we performed various ab-initio and DFT calculations, namely MRCI(+Q)-F12/AVDZ using Molpro 2012 software (Werner et al. 2012), and RCCSD(T)-F12/AVTZ and M06-2X/AVTZ using Gaussian 09 software, the CCSD(T) and DFT methods being likely only poorly adapted due to the highly multiconfigurational aspect of the $\text{S}(^3\text{P}) + \text{SO}(^3\Sigma^-)$ potential energy surface. At the MRCI level we found no barrier for SSO formation on the ground singlet surface (highly exothermic by 295 kJ/mol) but a barrier equal to 6 kJ/mol for SOS formation (exothermic by only 32 kJ/mol) and a barrier equal to 16 kJ/mol for cyclic- SOS formation (exothermic by 154 kJ/mol). Moreover, we found a barrier for the isomerizations

SSO \rightarrow OSS and SSO \rightarrow cyc-SOS, so the exchange reaction is unlikely. However, the surface around the transition states for isomerization is particularly complex, and may also involve the triplet surface, so we cannot completely exclude the possibility of some isomerization. We then performed some runs varying the rate constant for the $^{34}\text{S} + \text{SO} \rightarrow \text{S} + ^{34}\text{SO}$ reaction between zero and the capture rate value. Even for a large rate constant, the effect on ^{34}SO fractionation is low due to the low abundance of sulphur atoms in the gas-phase associated with the fact that the exothermicity of the ^{34}S exchange process is lower than the thermal energy in dense molecular clouds. As a result, there is little doubt that ^{34}SO will show very low enrichment levels.

It should be noted that exchange reactions are efficient only in the gas-phase because on ices we always favor the addition channel (for example $^{18}\text{O} + \text{O}_2 \rightarrow ^{18}\text{OOO}$ only). However, diffusion and tunneling are mass dependent and are then not strictly equivalent for the various isotopologues, these effects being included in our model but having only a small effect on ^{18}O fractionation.

For O_2 and SO_2 there are two possibilities to have one ^{18}O . Then the elemental $^{16}\text{O}^{16}\text{O}/^{16}\text{O}^{18}\text{O}$ and $\text{S}^{16}\text{O}^{16}\text{O}/\text{S}^{16}\text{O}^{18}\text{O}$ ratios are equal to 250 instead of 500.

Table 2. Review of isotopic exchange reactions.

$k_f = \alpha \times (T/300)^\beta \times f(\text{B},\text{m}) / (f(\text{B},\text{m}) + \exp(\Delta E/T))$ (forward reaction, $\text{C}^{18}\text{O} + \text{HCO}^+ \rightarrow \text{HC}^{18}\text{O}^+ + \text{CO}$)

$k_r = \alpha \times (T/300)^\beta \times \exp(\Delta E/kT) / (f(\text{B},\text{m}) + \exp(\Delta E/T))$ (reverse reaction, $\text{HC}^{18}\text{O}^+ + \text{CO} \rightarrow \text{C}^{18}\text{O} + \text{HCO}^+$)

	Reaction	α	β	ΔE	f(B,m)	reference
1.	$\text{C}^{18}\text{O} + \text{HCO}^+ \rightarrow \text{HC}^{18}\text{O}^+ + \text{CO}$	2.6e-10	-0.4	-6.3	1	(Smith & Adams 1980, Mladenovic & Roueff 2014)
2.	$\text{H}_3\text{O}^+ + \text{H}_2^{18}\text{O} \rightarrow \text{H}_3^{18}\text{O}^+ + \text{H}_2\text{O}$	1.5e-9	-0.5	-14.5		Proton transfer rate constant similar to the $\text{H}_2\text{DO}^+ + \text{H}_2\text{O}$ one's (Anicich 2003)
3.	$^{18}\text{O}^+ + \text{CO} \rightarrow \text{C}^{18}\text{O} + \text{O}^+$	4.4e-10	0	-38.0	1	(Fehsenfeld et al. 1974)
4.	$^{18}\text{O} + \text{CO} \rightarrow \text{C}^{18}\text{O} + \text{O}$	"0"		-38.0		This reaction has a barrier and a negligible rate at low temperature (Inn 1974, Toby et al. 1984, Talbi et al. 2006, Goumans & Andersson 2010)
5.	$^{18}\text{O} + \text{SO}^+ \rightarrow \text{O} + \text{S}^{18}\text{O}^+$	3.0e-10	0	-37.3	1	We assume no barrier for this reaction (SO^+ has a reactive doublet ground state and reacts quickly with N atoms (Fehsenfeld & Ferguson 2012)) and a rate constant close to capture rate value. The $\text{S}^+ + \text{O}_2$ exit channel is slightly endothermic and may play a role (Dotan et al. 1979, Tichý et al. 1979, Smith et al. 1981)
6.	$^{18}\text{O} + \text{NO} \rightarrow \text{N}^{18}\text{O} + \text{O}$	7.0e-11	0	-36.3	1	(Fernando & Smith 1979, Fernando & Smith 1981, Anderson et al. 1985, Cobos & Troe 1985, W. M. Smith 1997)
7.	$^{18}\text{O} + \text{SO} \rightarrow \text{S}^{18}\text{O} + \text{O}$	5.3e-11	0	-31.5	1	(Lu et al. 2003, Cobos et al. 1985). We neglect here the radiative association reaction estimated equal to $7.0e^{-16}$ at room temperature (Rolfes et al. 1965, Singleton & Cvetanović 1988)
8.	$^{18}\text{O} + \text{O}_2 \rightarrow \text{O} + \text{O}^{18}\text{O}$	3.4e-12	-0.6	-32.3	2	(Anderson et al. 1985, Wiegell et al. 1997, Fleurat-Lessard et al. 2003, Rajagopala Rao et al. 2015). The experimental studies cover only the 143 K – 353 K range and are difficult to extrapolate at 10K. The theoretical studies are not in very good agreement with the experimental ones.
9.	$^{18}\text{O} + \text{SO}_2 \rightarrow \text{O} + \text{OS}^{18}\text{O}$	"0"				There is a barrier equal to 850 K for this reaction (Naidoo et al. 2005) leading to negligible value at low temperature.

0.	$^{34}\text{S}^+ + \text{CS} \rightarrow \text{S}^+ + \text{C}^{34}\text{S}$	$2.0\text{e-}9$	-0.4	-7.4	1	We assume no barrier for this reaction by comparison with $\text{O}^+ + \text{CO}$, with a rate constant close to capture rate value by comparison with similar S^+ reactions (Anicich 2003)
1.	$^{34}\text{S}^+ + \text{S}_2 \rightarrow \text{S}^+ + \text{S}^{34}\text{S}$	"0"		-8.7		We neglect the exchange reaction favoring the much more exothermic charge transfer (-11650 K).
2.	$^{34}\text{S}^+ + \text{SO} \rightarrow \text{S}^+ + ^{34}\text{SO}$	"0"		-8.6		We neglect the exchange reaction favoring the slightly exothermic $\text{S}_2^+ + \text{O}$ channel (-153 K) and the charge transfer reaction (-766 K) (see text).
3.	$^{34}\text{S} + \text{NS} \rightarrow \text{S} + \text{N}^{34}\text{S}$	$7.0\text{e-}11$	0	-8.9	1	Same high pressure rate constant than $\text{O} + \text{NO}$
4.	$^{34}\text{S} + \text{S}_2 \rightarrow \text{S} + \text{S}^{34}\text{S}$	$3.0\text{e-}11$	0	-8.7	2	We assume no dynamical effect such as for $\text{O} + \text{O}_2$ with a rate constant close to capture.
5.	$^{34}\text{S} + \text{SO} \rightarrow ^{34}\text{SO} + \text{S}$	"0"		-8.6		See text

2.3 Modeling results

The CO, HCO^+ , OH, O_2 , OCS, H_2CO , CH_3OH , NO, SO, and SO_2 abundances relative to H_2 calculated by our model are shown in Figure 1.

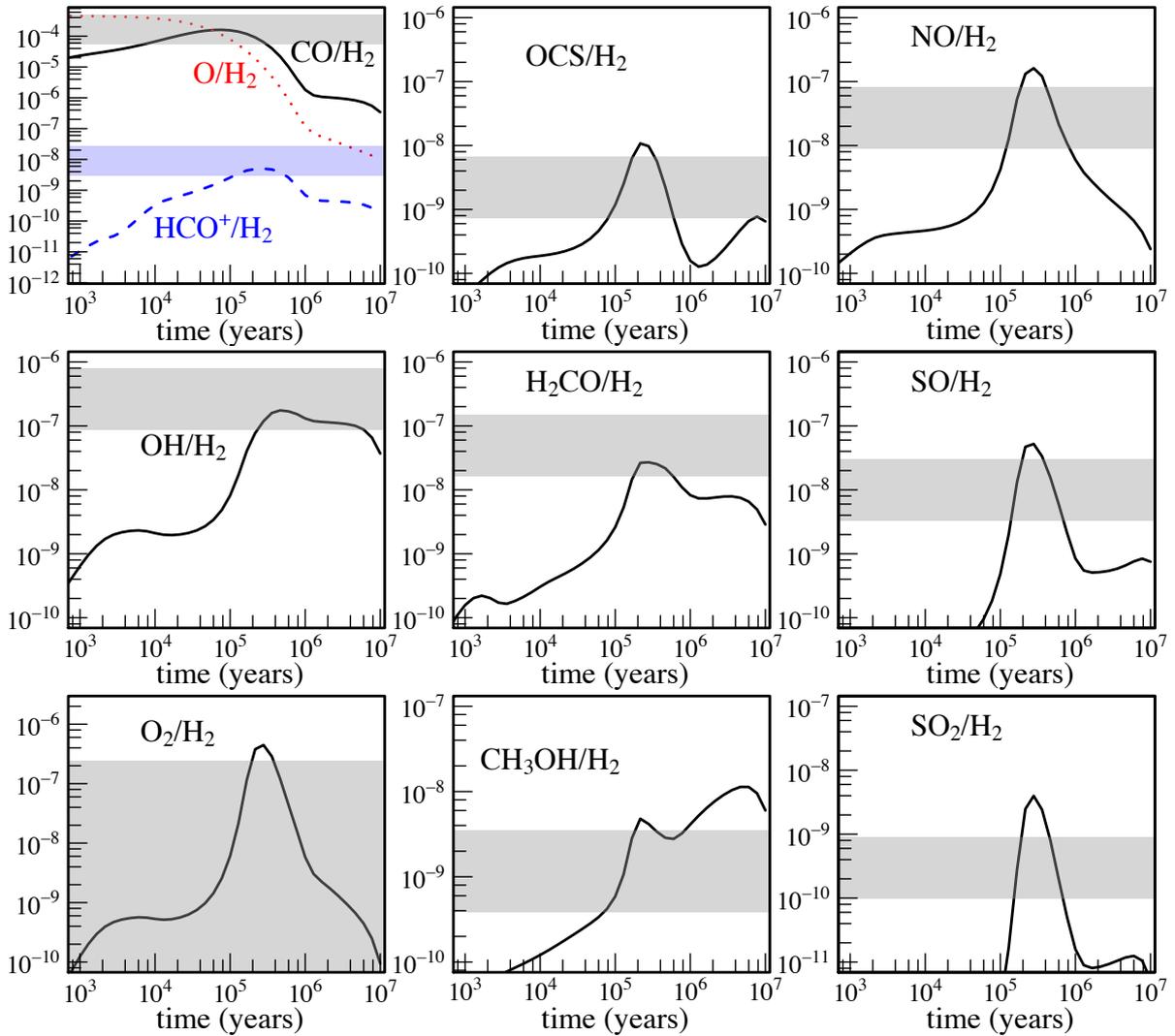


Figure 1: Calculated gas-phase abundance ratios, relative to H_2 , of CO, HCO^+ , OH, O_2 , OCS, H_2CO , CH_3OH , NO, SO and SO_2 studied in this work as a function of time predicted by our model for $\text{N}(\text{H}_2) = 2 \times 10^4 \text{ cm}^{-3}$ and $T = 10\text{K}$. The horizontal grey rectangles represent the abundances observed in the cold core TMC-1 (CP),(Gratier et al. 2016, Lique et al. 2006)

including an arbitrary factor 3 for the uncertainties. In this figure, sulphur is depleted by a factor of 10, the S/H₂ ratio being equal to 1.5×10⁻⁶.

The calculated ¹⁶O/¹⁸O ratios for the same species are shown in Figure 2 assuming an elemental ¹⁶O/¹⁸O ratio of 500.

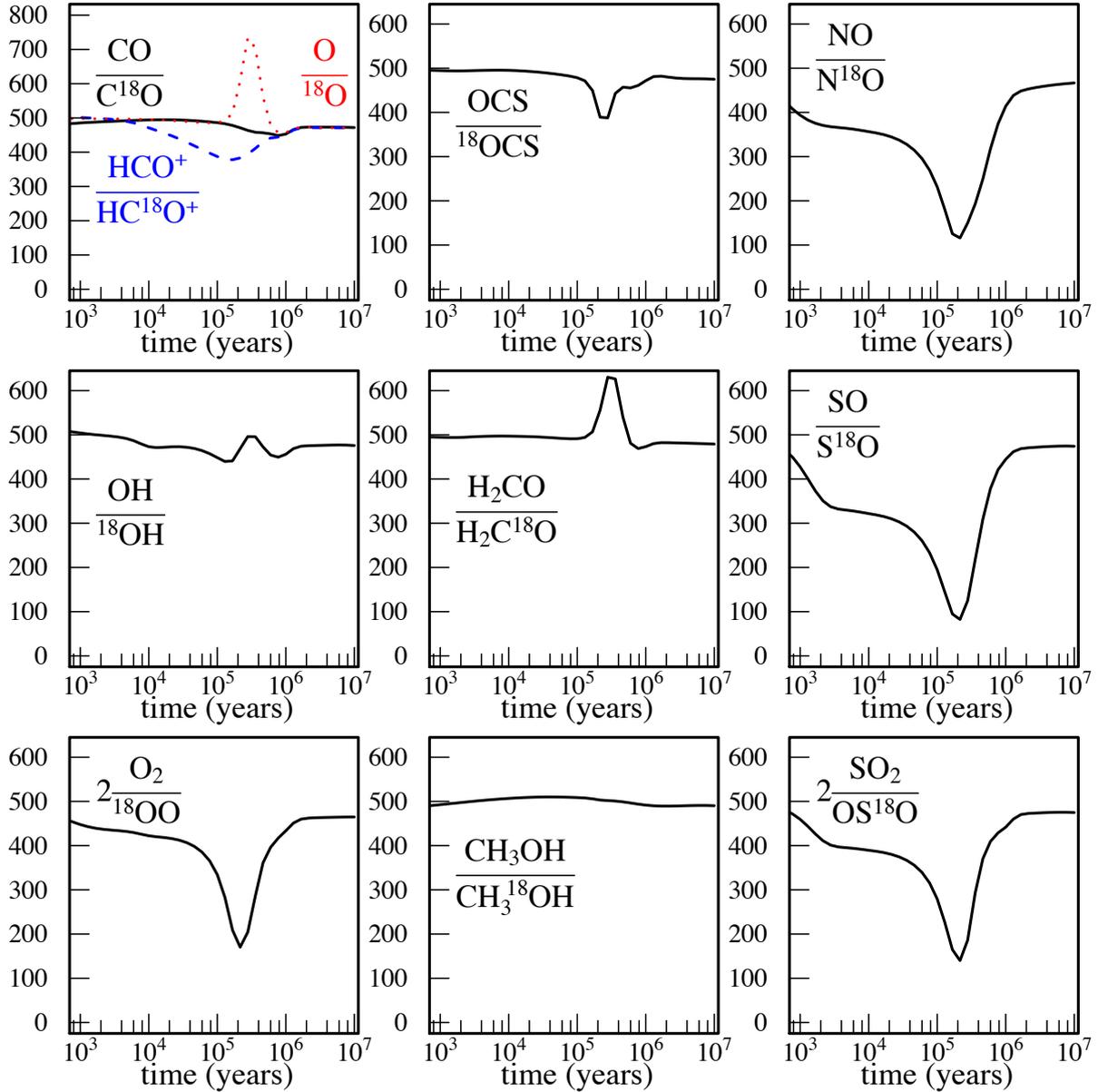


Figure 2: Calculated ¹⁶O/¹⁸O ratio for the main oxygen species in the gas-phase as a function of time predicted by our model (N(H₂) = 2×10⁴ cm⁻³, T = 10K). The ¹⁶O/¹⁸O elemental ratio is taken equal to 500.

The results of our model show variable oxygen fractionation levels with time, some of them being significant. The fractionation for HCO⁺ induced by reaction (1) is low but non-negligible. As electronic Dissociative Recombination (DR) of HCO⁺ leads to CO formation, there is some oxygen fractionation in CO too. However, as the DR of HCO⁺ is not the main

source of CO (the main CO sources are the O + CH, O + CH₂, O + C₂H, O + CN, ... reactions), fractionation is less important in CO than in HCO⁺. The fractionation of methanol is low and similar to the CO one as methanol is essentially produced through CO hydrogenation on ice, where the surface CO, s-CO, comes from depletion of gas-phase CO onto the ice. ¹⁸O enrichment is particularly large for NO, SO, SO₂ and O₂. This result demonstrates that gas-phase isotopic exchange reactions have a significant effect on the oxygen fractionation in dense interstellar clouds. This effect is important for NO and SO because the fractionation reactions:



are efficient as the rate constant is close to the capture rate limiting value (see Table 2) and the available exit channels producing N + O₂ and S + O₂ are endothermic. There is also the equivalent reaction:



which is barrierless but for which the rate constant at low temperature is uncertain due to dynamical effects (see the chemical description above). There is also some fractionation for SO₂ and OCS which is brought about by the fractionation of SO, as SO₂ is mainly formed through the SO + OH reaction. The fractionation effect on OCS is lower because OCS is mainly formed through the OH + CS reaction (Loison et al. 2012). However, when SO reaches a large abundance, the CH + SO reaction produces large quantities of OCS (Loison et al. 2012), which then partially reflects the SO fractionation level.

The amount of ¹⁸O trapped in CO, SO, NO, O₂ and SO₂ is large enough around a few 10⁵ years to strongly deplete gas-phase ¹⁸O. Then, H₂CO becomes depleted in ¹⁸O because H₂CO is mainly produced through the O + CH₃ reaction at this time and atomic oxygen is depleted in ¹⁸O in the gas-phase. At longer times, non-thermal desorption of H₂CO produced on ice through CO hydrogenation becomes competitive and H₂C¹⁸O depletion vanishes. Thus, the use of H₂CO to determine the O/¹⁸O ratio across the galaxy (Wilson 1999) may be not the most pertinent choice.

A remarkable point in the predicted ¹⁸O enrichment of SO and NO is its time dependency. Indeed, there is a large variation of the oxygen fractionation as a function of time, with a maximum around 2×10⁵ years for a constant density of N(H₂) = 2×10⁴ molecules.cm⁻³. After this time, the amount of oxygen (¹⁶O and ¹⁸O) in the gas-phase strongly decreases where it is either transformed into CO or depleted onto dust grains. Then the ¹⁸O + NO and ¹⁸O + SO

reactions are not efficient enough to induce a large fractionation. In contrast to N¹⁸O, S¹⁸O is often detected in interstellar media with good sensitivity.

3 COMPARISONS WITH OBSERVATIONS

In order to test the results of our chemical model, we analyzed observations from existing surveys obtained with the IRAM 30m telescope in five different cold cores: B1-b, TMC-1, L483, L1689B, and the Horsehead cold dense core. Details on the analysis source by source as well as comparison with our model predictions are given in this section.

3.1 Observations

All the observations have been performed with the IRAM 30m telescope. The data were reduced using the CLASS/GILDAS software package, i.e. the individual spectra were co-added, folded to de-convolve from the frequency switching procedure, and a baseline consisting of a low-order polynomial (typically 3 or 5) was withdrawn. The observed lines are presented in Table 3.

Table 3: Observed line parameters of SO, ³⁴SO and S¹⁸O in B1-b, TMC-1, L483, L1689B and Horsehead cold dense core.

Molecule	Transition	Frequency (MHz)	E _{up} (K)	A _{ul} (s ⁻¹)	VLSR (km.s ⁻¹)	D _v (km.s ⁻¹)	$\int T_A^* dv$ (K.km.s ⁻¹)	τ
B1-b								
SO	2 2 - 1 1	86093.958	19.3	5.25E-6	6.53(2)	0.74(2)	1.3714(30)	
					7.10(2)	0.59(2)	0.2158(30)	
SO	2 3 - 1 2	99299.886	9.2	1.12E-5	4.90(12)	0.63(18)	0.0230(50)	
					6.42(2)	0.85(2)	3.6951(10)	
					7.14(2)	0.75(2)	1.5493(10)	
SO	5 4 - 4 4	100029.550	38.6	1.08E-6	6.55(2)	0.63(2)	0.0409(10)	
SO	3 2 - 2 1	109252.181	21.1	1.08E-5	6.43(4)	0.58(4)	0.9196(20)	
					6.84(4)	0.59(4)	0.5749(20)	
					7.35(13)	0.68(8)	0.0774(20)	
³⁴ SO	2 2 - 1 1	84410.685	19.2	4.95E-6	6.57(1)	0.75(2)	0.0734(20)	
³⁴ SO	2 3 - 1 2	97715.405	9.1	1.07E-5	6.47(3)	0.57(5)	0.5285(50)	
					6.89(10)	0.65(5)	0.3482(50)	
³⁴ SO	3 2 - 2 1	106743.363	20.9	1.01E-5	6.54(2)	0.60(2)	0.0779(20)	
					7.01(2)	0.31(6)	0.0079(20)	
S ¹⁸ O	2 3 - 1 2	93267.376	8.7	9.34E-6	6.59(3)	0.68(2)	0.1643(20)	
S ¹⁸ O	3 2 - 2 1	99803.664	20.5	8.22E-6	6.59(3)	0.55(8)	0.0106(10)	
					7.10(7)	0.24(10)	0.0015(10)	
TMC-1								
SO	2 2 - 1 1	86093.958	19.3	5.25E-6	5.692(5)	0.24(5)	0.0048(10)	
					6.07(1)	0.35(2)	0.0146(60)	
SO	2 3 - 1 2	99299.886	9.2	1.12E-5	5.668(4)	0.357(8)	0.2237(50)	
					6.082(2)	0.365(4)	0.3809(50)	
SO	3 2 - 2 1	109252.181	21.1	1.08E-5	5.67(7)	0.47(14)	0.0077(20)	

					6.13(3)	0.34(6)	0.0093(20)	
³⁴ SO	2 3 - 1 2	97715.405	9.1	1.07E-5	5.69(2)	0.29(5)	0.0110(20)	
					6.11(2)	0.35(4)	0.0219(20)	
S ¹⁸ O	2 3 - 1 2	93267.376	8.7	9.34E-6	5.78(8)	0.16(16)	0.0006(10)	
					6.11(3)	0.38(9)	0.0051(10)	
L483								
SO	2 2 - 1 1	86093.958	19.3	5.25E-6			0.254(25)	
SO	2 3 - 1 2	99299.886	9.2	1.12E-5			1.61(16)	
SO	5 4 - 4 4	100029.550	38.6	1.08E-6	5.59(3)	0.92(10)	0.007(1)	
SO	3 2 - 2 1	109252.181	21.1	1.08E-5			0.226(22)	
³⁴ SO	2 2 - 1 1	84410.685	19.2	4.95E-6	5.29(3)	0.42(4)	0.0073(7)	
³⁴ SO	2 3 - 1 2	97715.405	9.1	1.07E-5	5.04(3)	0.42(3)	0.173(17)	
³⁴ SO	3 2 - 2 1	106743.363	20.9	1.01E-5	4.92(7)	0.48(5)	0.008(1)	
S ¹⁸ O	2 3 - 1 2	93267.376	8.7	9.34E-6	4.95(3)	0.43(3)	0.035(3)	
L1689B								
SO	2 2 - 1 1	86093.958	19.3	5.25E-6	3.56(0)	0.50(0)	0.780(67)	0.86
SO	2 3 - 1 2	99299.886	9.2	1.12E-5	3.55(0)	0.65(0)	2.889(244)	
SO	5 4 - 4 4	100029.550	38.6	1.08E-6	3.81(2)	0.41(5)	0.009(1)	0.009
SO	3 2 - 2 1	109252.181	21.1	1.08E-5	3.66(0)	0.49(0)	0.758(63)	0.91
SO	3 3 - 2 2	129138.923	25.5	2.25E-5	3.60(0)	0.45(0)	0.671(81)	1.03
SO	3 4 - 2 3	138178.600	15.9	3.17E-5	3.47(0)	0.61(0)	2.156(257)	
SO	4 3 - 3 2	158971.811	28.7	4.23E-5	3.54(0)	0.46(0)	0.541(62)	0.82
SO	4 4 - 3 3	172181.403	33.8	5.83E-5	3.53(0)	0.43(0)	0.376(42)	0.56
SO	5 6 - 4 5	219949.442	35.0	1.34E-4	3.61(1)	0.51(1)	0.739(95)	0.99
SO	1 1 - 0 1	286340.152	15.2	1.40E-5	3.51(1)	0.33(2)	0.271(37)	1.20
³⁴ SO	2 2 - 1 1	84410.685	19.2	4.95E-6	3.56(1)	0.49(2)	0.026(3)	0.03
³⁴ SO	2 3 - 1 2	97715.405	9.1	1.07E-5	3.29(0)	0.49(0)	0.477(48)	0.64
³⁴ SO	3 2 - 2 1	106743.363	20.9	1.01E-5	3.19(1)	0.46(2)	0.033(4)	0.04
³⁴ SO	3 3 - 2 2	126613.93	25.3	2.12E-5	3.23(3)	0.47(7)	0.030(6)	0.04
³⁴ SO	4 3 - 3 2	155506.795	28.4	3.96E-5	3.50(2)	0.33(5)	0.017(3)	0.04
³⁴ SO	4 4 - 3 3	168815.135	33.4	5.50E-5	3.55(2)	0.31(4)	0.011(2)	0.03
S ¹⁸ O	2 3 - 1 2	93267.270	8.7	9.34E-6	3.22(0)	0.47(0)	0.171(17)	0.18
S ¹⁸ O	3 4 - 2 3	129066.190	14.9	2.58E-5	3.54(0)	0.47(1)	0.108(2)	0.12
S ¹⁸ O	4 3 - 3 2	145874.490	27.5	3.27E-5	3.60(3)	0.42(6)	0.007(1)	0.009
Horsehead								
SO	2 2 - 1 1	86093.958	19.3	5.25E-6	10.55(4)	0.57(1)	0.30(1)	0.18
SO	2 3 - 1 2	99299.886	9.2	1.12E-5	10.55(4)	0.57(1)	3.18(1)	1.39
SO	3 2 - 2 1	109252.222	21.1	1.08E-5	10.55(4)	0.57(1)	0.43(1)	0.21
SO	3 3 - 2 2	129138.923	25.5	2.25E-5	10.55(4)	0.57(1)	0.02(1)	0.28
SO	3 4 - 2 3	138178.56	15.9	3.17E-5	10.55(4)	0.57(1)	2.79(1)	1.37
SO	4 3 - 3 2	158971.811	26.7	4.23E-5	10.55(4)	0.57(1)	0.49(3)	0.27
SO	3 3 - 3 4	201162.805	25.5	2.75E-5	10.55(4)	0.57(1)	0.00(1)	0.00
SO	2 2 - 2 3	210202.256	19.3	2.84E-5	10.55(4)	0.57(1)	0.01(2)	0.00
SO	2 1 - 1 2	236452.293	15.8	1.42E-6	10.55(4)	0.57(1)	0.04(1)	0.01
SO	3 2 - 2 3	246404.588	21.1	1.00E-6	10.55(4)	0.57(1)	0.00(1)	0.01
SO	4 3 - 3 4	267197.756	28.7	7.11E-7	10.55(4)	0.57(1)	0.08(2)	0.00
³⁴ SO	2 2 - 1 1	84410.685	19.3	4.95E-6	10.55(4)	0.57(1)	0.02(1)	0.01
³⁴ SO	2 3 - 1 2	97715.405	9.1	1.07E-5	10.55(4)	0.57(1)	0.18(1)	0.05
³⁴ SO	3 2 - 2 1	106743.363	20.9	1.01E-5	10.55(4)	0.57(1)	0.03(1)	0.01
³⁴ SO	3 4 - 2 3	135775.728	15.6	3.00E-5	10.55(4)	0.57(1)	0.18(1)	0.05
³⁴ SO	4 3 - 3 2	155506.795	28.4	3.96E-5	10.55(4)	0.57(1)	0.00(2)	0.01
³⁴ SO	3 3 - 3 4	202116.596	25.3	2.78E-8	10.55(4)	0.57(1)	0.00(2)	0.00
³⁴ SO	2 1 - 1 2	237107.767	15.8	1.41E-6	10.55(4)	0.57(1)	0.03(1)	0.00
³⁴ SO	3 2 - 2 3	246135.724	20.9	1.01E-6	10.55(4)	0.57(1)	0.00(1)	0.00
³⁴ SO	4 3 - 3 4	265866.874	28.4	7.13E-7	10.55(4)	0.57(1)	0.00(1)	0.00
S ¹⁸ O	2 3 - 1 2	93267.376	8.7	9.34E-6	10.55(4)	0.57(1)	0.03(1)	0.01
S ¹⁸ O	3 2 - 2 1	99803.664	20.5	8.22E-6	10.55(4)	0.57(1)	0.01(1)	0.00
S ¹⁸ O	3 4 - 2 3	129066.19	14.9	2.58E-5	10.55(4)	0.57(1)	0.02(1)	0.01

S ¹⁸ O	4 3 – 3 2	145874.49	27.5	3.27E-5	10.55(4)	0.57(1)	0.00(1)	0.00
S ¹⁸ O	2 1 – 1 2	239102.492	15.7	1.37E-6	10.55(4)	0.57(1)	0.00(1)	0.00
S ¹⁸ O	3 2 – 2 3	245638.781	20.5	1.00E-6	10.55(4)	0.57(1)	0.01(1)	0.00
S ¹⁸ O	4 3 – 3 4	262447.093	27.5	7.13E-7	10.55(4)	0.57(1)	0.00(2)	0.00

L483:

L483 is a cold dense cloud around a Class 0 source, with a column density of H₂ of 3×10^{22} cm⁻² (Tafalla et al. 2000). The volume density and kinetic temperature derived by Jorgensen et al. (2002) are 3.4×10^4 cm⁻³ and 10 K. The observations of L483 were carried out using the IRAM 30m telescope in the framework of molecular line survey in the 3 mm band. Details on these observations can be found in Agúndez et al. (2018b), Agúndez et al. (2018a) and Marcelino et al. (2018) while a thorough description of the observations and the complete survey will be presented by Agúndez et al. (in preparation). Briefly, observations were performed in several sessions from August 2016 to April 2018, with the telescope pointed toward the position of the infrared source IRAS 18148-0440. The main beam of the IRAM 30m telescope at the frequencies observed is in the range 30-21 arcsec. The receiver EMIR E090 was used connected to the FTS backend, which provides a spectral resolution of 50 kHz (0.14-0.18 km s⁻¹ at the observed frequencies, which is good enough to resolve lines in L483, which have typical widths of ≈ 0.5 km s⁻¹). The frequency-switching technique was used to maximize the telescope time. We detect four lines of SO (see Table 3), although only two are taken into account to derive the column density. The line at 99299 MHz is optically thick while that lying at 100029 MHz is only marginally detected. For ³⁴SO we detect three lines, which allow to constrain the rotational temperature to 4.5 +/- 0.5 K, value that is assumed to hold for all SO isotopologues. Finally, for S¹⁸O we only detect one line, although with a very good signal-to-noise ratio.

B1b and TMC-1:

Barnard 1 (B1) is a dense core with a steep density gradient where $N(\text{H}_2)$ is between 7.6×10^{22} cm⁻² (Daniel et al. 2013) and 1.3×10^{23} cm⁻² (Hirano et al. 1999). The column density of H₂ molecules at the position of the cyanopolyne peak in TMC-1 has been estimated equal to 10^{22} cm⁻² (Cernicharo & Guélin 1987). The B1b and TMC-1 data are part of a 3mm line survey using the IRAM 30-m telescope (see (Cernicharo et al. 2012) and references within). Observations were performed between January and May 2012 towards the positions $\alpha_{J2000}=03^{\text{h}}33^{\text{m}}20.8^{\text{s}}$, $\delta_{J2000}=31^{\circ}07'34''$ in B1-b, and the cyanopolyne peak in TMC-1 $\alpha_{J2000}=04^{\text{h}}41^{\text{m}}41.88^{\text{s}}$, $\delta_{J2000}=25^{\circ}41'27''$. The EMIR receivers were used connected to the fast

Fourier Transform Spectrometers (FTS) providing a spectral resolution of 50 kHz and covering the 3mm band between 82.5 and 117.5 GHz. At the observed frequencies the velocity resolution ranges from 0.18 km s⁻¹ to 0.12 km s⁻¹, which is good enough for the typical line widths (~ 0.5 km s⁻¹ in TMC-1, and ~ 1 km s⁻¹ in B1b), and allows us to resolve the two velocity components in both sources (~ 5.7 and 6.0 km s⁻¹ in TMC-1, ~ 6.5 and 7.0 km s⁻¹ in B1b, see Table 3). All the observations were performed using Frequency Switching (FSw) mode. Each spectral setup was observed for 2 hrs, resulting in an average rms of 4-6 mK (up to 10-20 mK at the high frequencies close to the end of the band) for both sources. In B1b we detect 4 lines of SO, but the emission is optically thick and we did not compute column densities. We used the 3 lines of ³⁴SO to perform rotational diagrams and obtain a rotational temperature of 6.5 +/- 0.7 K, a value close to the 8.2 K obtained by Fuente et al. (2016). This temperature was used to compute the column density of S¹⁸O (only 2 lines observed). SO lines in TMC-1 are optically thin and we obtained a rotational temperature of 3.9 +/- 0.1 K, which was used to obtain column densities for ³⁴SO and S¹⁸O since only one line was detected for these isotopologues (see Table 3).

L1689B:

The L1689B dense core is located in the ρ-Ophiuchi star forming complex and has a column density equal to $N(\text{H}_2)$ is $1.4 \times 10^{23} \text{ cm}^{-2}$ (Steinacker et al. 2016). The data presented here were observed during various campaigns spanning 2011-2017 at the IRAM 30-m telescope. The coordinates of the integration position were $\alpha_{\text{J2000}}=16^{\text{h}}34^{\text{m}}48.3^{\text{s}}$, $\delta_{\text{J2000}}=-24^{\circ}38'04''$. The data were taken in frequency switching mode using the EMIR receivers connected to the fast Fourier transform spectrometer (FTS) with a spectral resolution of 50 kHz (at the observed frequencies the velocity resolution is lower than 0.17 km s⁻¹, which is good enough to resolve lines in L1689B, which have typical widths of 0.45-0.5 km s⁻¹). The average rms reached ranged between 2-4 mK at frequencies below 115 GHz to around 10 mK at 2 mm and 50 mK at 1 mm. The line integrated intensities were converted to the main beam temperature scale. To derive the molecular column, we assumed the same excitation temperatures for all transitions, albeit possibly different to the kinetic temperature. Under this assumption, we calculated the line integrated intensities for a grid of values in excitation temperature and molecular column densities. We then minimized the χ^2 between the modelled line integrated intensities and the observed ones to derive the molecular column densities. One-sigma error bars were determined using the column density interval defined by $\chi^2_{\text{min}} + 2.3$, as described in Bacmann and Faure (2016). For the main SO isotopologue, the lines at 99299.886 MHz and at 138178.6 MHz are

optically thick with optical depths around 8-15. We have not considered these lines in our analysis.

Horsehead:

The dense core of the Horsehead nebula (the shielded core characterized by a large DCO⁺ abundance J2000 05h 40m 55.73s, $-02^{\circ} 27' 38''$) has total column density estimated to be $N(\text{H}_2) = 3.0 \times 10^{22} \text{ cm}^{-2}$ (Gerin et al. 2009). The data is part of the Horsehead WHISPER survey and was observed using position switching at the 30m IRAM telescope. It covers the full 3, 2 and 1mm atmospheric bands with a spectral resolution of 50kHz at 2 and 3mm and 195kHz at 1mm. This corresponds to a velocity resolution between 0.17 km/s and 0.05 km/s depending on frequency, sufficient to well resolve the lines in this source (linewidth of typically 0.45 km/s). The median noises are 8.1 mK, 18.5 mK, and 8.3 mK respectively for the 3, 2 and 1mm bands. Details about the data reduction can be found in Pety et al. (2012). Radiative transfer calculations were carried out using the LTE approximation as implemented in the Weeds package (Maret et al. 2011). All lines of SO, S¹⁸O and ³⁴SO with frequencies inside the observed bands and with upper level energies lower than 30K were selected. A 2.5MHz frequency range was selected around each of these lines and a Bayesian method was used to recover the radiative transfer model parameters. The method is presented in details in Andron et al. (2018). The observed spectra are presented in Figure A1 in the appendix. And the 1D and 2D histogram of the posterior probability distribution function and the comparison of the observations are presented in Figure A2.

In Table 4, we present the observed $^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$, $^{32}\text{S}^{16}\text{O}/^{34}\text{S}^{16}\text{O}$ and $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratios computed in the five cold cores. More details on the observations are given in the appendix. In addition, we report the values observed in the pre-stellar core L1544 by Vastel et al. (2018). Local ISM and Solar system values are also given for comparison.

Table 4: Observed $^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$, $^{32}\text{S}^{16}\text{O}/^{34}\text{S}^{16}\text{O}$ and $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ column density ratios.

	$N(\text{H}_2)$ in cm^{-2}	$^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$	$^{32}\text{S}^{16}\text{O}/^{34}\text{S}^{16}\text{O}$	$^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$
TMC1 (this work)	1.0×10^{22}	115 ± 13	19.5 ± 2.2	5.9 ± 1.4
L483 (this work)	3.0×10^{22}	158 ± 47	31 ± 9	5.1 ± 1.5
B1-b (this work)	7.6×10^{22}	-	-	5.2 ± 1.4
L1689B (this work)	1.4×10^{23}	70 ± 20	23 ± 7	3.3 ± 1.1
Horsehead nebula (dense cloud) (this work)	3.0×10^{22}	170 ± 20	27.3 ± 1.2	6.1 ± 0.7

L1544 (Vastel et al. 2018)	4.5×10^{22}	-	-	4.7 ± 1.0
		$^{16}\text{O}/^{18}\text{O}$	$^{32}\text{S}/^{34}\text{S}$	$(^{16}\text{O} \times ^{34}\text{S}) / (^{18}\text{O} \times ^{32}\text{S})$
Local ISM (Wilson 1999)		557 ± 30	≈ 22	25
Solar system (Lodders 2003)		500	22.5	22.2

3.2 Comparison with the model predictions

In TMC-1, the core region of the Horsehead, L1689B and L483, some SO lines are optically thin allowing a direct determination of the $^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratio, showing large discrepancies with the elemental ratio. As the $^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratio predicted by the model is highly dependent on time (see Figures 2 and 3), the observed ratios may then provide strong constraints on the chemical evolution of the cores. We emphasize here that, for simplicity, the physical structure of the cloud remains constant in our simulations. One result, however, remains valid in that for ^{18}O fractionation to be efficient, a high gas-phase abundance of ^{18}O is required. The agreement between the predicted and the observed $^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratio in dense molecular clouds requires an atomic oxygen abundance in the gas phase above 1×10^{-5} relative to H_2 corresponding to a relatively small time period. Such large gas-phase abundances of neutral oxygen atoms indicate only partial depletion onto ices. There are several approximations in our model (no structure, no description of the first part of cloud evolution where UV radiation is important) that can affect the conclusions. However, considering the large reactive fluxes involved in the exchange reactions, the very good agreement between observations and calculations (for the $\text{S}^{18}\text{O}/\text{SO}$ ratio in addition to the abundances of most of the species detected in these molecular clouds) is very unlikely to be coincidental. For all the cold molecular clouds observed in this study, the large ^{18}O enrichment factors in SO clearly show that a significant fraction of oxygen is still in the gas-phase, at least for the part of the cloud probed by SO and S^{18}O . One another important result of our study is the fact that the similar global molecular abundances and S^{18}O enhancement levels means that the cold molecular clouds observed here are probably at similar stages of chemical evolution with a non-negligible oxygen atom abundance remaining in the gas-phase.

When the observed S^{16}O lines are optically thick, an alternative way to determine the oxygen fractionation level is to analyze the $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratios. To study ^{18}O and ^{34}S fractionation, we compare the various observed $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratios with our model predictions including oxygen and sulphur fractionation. As shown in Table 4, the observed $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$

ratios are much smaller (around factor of 5) than the local ISM isotope abundance ratios (25). This effect is mainly due to oxygen fractionation as we obtain very low sulphur fractionation as shown in Figure 3.

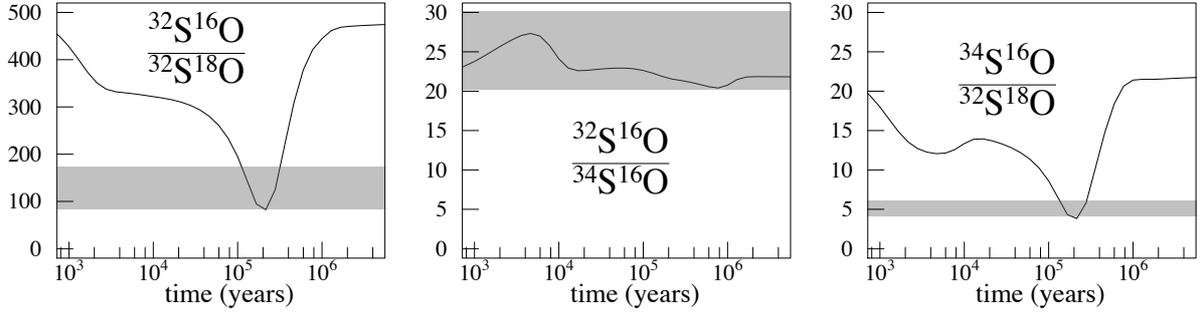


Figure 3: Calculated $\text{SO}/\text{S}^{18}\text{O}$, $^{32}\text{SO}/^{34}\text{SO}$ and $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratios as a function of time predicted by our model for $n(\text{H}) = 2 \times 10^4 \text{ cm}^{-3}$, $T = 10\text{K}$. The horizontal grey rectangle represents the average of dense core observations listed in Table 4.

Indeed, sulphur fractionation is observed to be very small in SO in the molecular clouds presented here, with a $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{16}\text{O}$ ratio close to the local ISM $^{34}\text{S}/^{32}\text{S}$ ratio, and also close to the $^{34}\text{S}/^{32}\text{S}$ ratio measured in diffuse molecular clouds (Lucas & Liszt 1998) and in the solar system (Lodders 2003). Then ^{34}S isotopologues are good proxies to derive abundances when the main ^{32}S species is optically thick. The agreement between the observed and calculated $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratio leads to the same level of chemical evolution as the one derived using the $^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ ratio, indicating that a relatively large gas-phase abundance of neutral oxygen atoms must remain to reproduce the observations.

4 CONCLUSIONS

In this work, we have presented a gas-grain model for oxygen (and sulphur) isotopic fractionation in cold cores. We also computed observed $^{32}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$, $^{32}\text{S}^{16}\text{O}/^{34}\text{S}^{16}\text{O}$ and $^{34}\text{S}^{16}\text{O}/^{32}\text{S}^{18}\text{O}$ isotopic ratios in five cold cores (B1-b, TMC-1, L483, L1689B, and the Horsehead cold dense core) using existing spectral surveys. Our main result is that the large observed $^{16}\text{O}/^{18}\text{O}$ ratio in SO is indicative of large amounts of ^{18}O in the gas-phase (reactive through neutral-neutral reactions), i.e. moderate depletion of ^{18}O on grains.

We have also shown that sulphur fractionation is very small in SO and in all species containing sulphur. Consequently, ^{34}S isotopologues are good proxies to derive abundances when the main ^{32}S species is optically thick.

The ^{18}O fractionation levels in SO indicate that this molecule might be a good proxy for leftover material from dense molecular clouds that could be inherited by comets. Indeed, if SO

in cometary ices originates from SO formed in the dense core leading to solar system formation, it may show ^{18}O fractionation. In contrast, if SO is mainly formed from ice photolysis, all ^{18}O fractionation should disappear as the main reservoir of oxygen on ice, H_2O , does not show any ^{18}O fractionation (Bockelée-Morvan et al. 2012, Mandt et al. 2015). As isotope fractionation is as sensitive probe of the evolution of matter, the chemistry described in this work could eventually be used as the basis for a more complex model including photodissociation and self-shielding effects, allowing us to simulate the evolution of isotopic composition in other environments such as diffuse molecular clouds and planetary systems.

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Appendix:

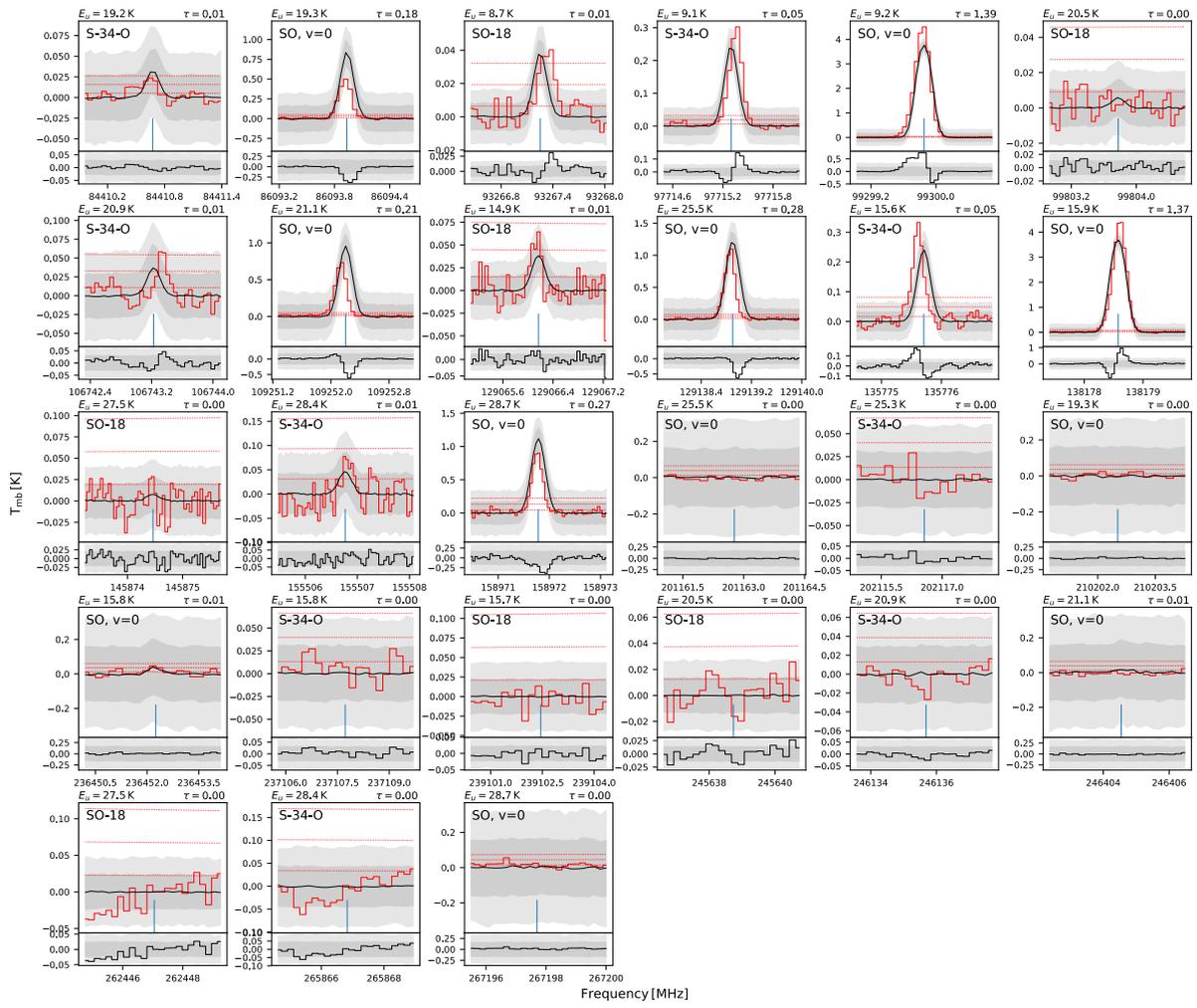


Figure A1: Observed spectra (red line) of various SO, ^{34}SO and S^{18}O lines at the dense core peak of the Horsehead dense core. The black spectrum is the LTE model for a 8.7 K excitation temperature and a column density of $5.64(0.23) \times 10^{13} \text{ cm}^{-2}$ for SO, $2.07(0.10) \times 10^{12} \text{ cm}^{-2}$ for ^{34}SO and $3.38(0.37) \times 10^{11} \text{ cm}^{-2}$ for S^{18}O . The uncertainties given by the global fitting are shown on grey spectra (68% (1σ) and 95% (2σ) probability).

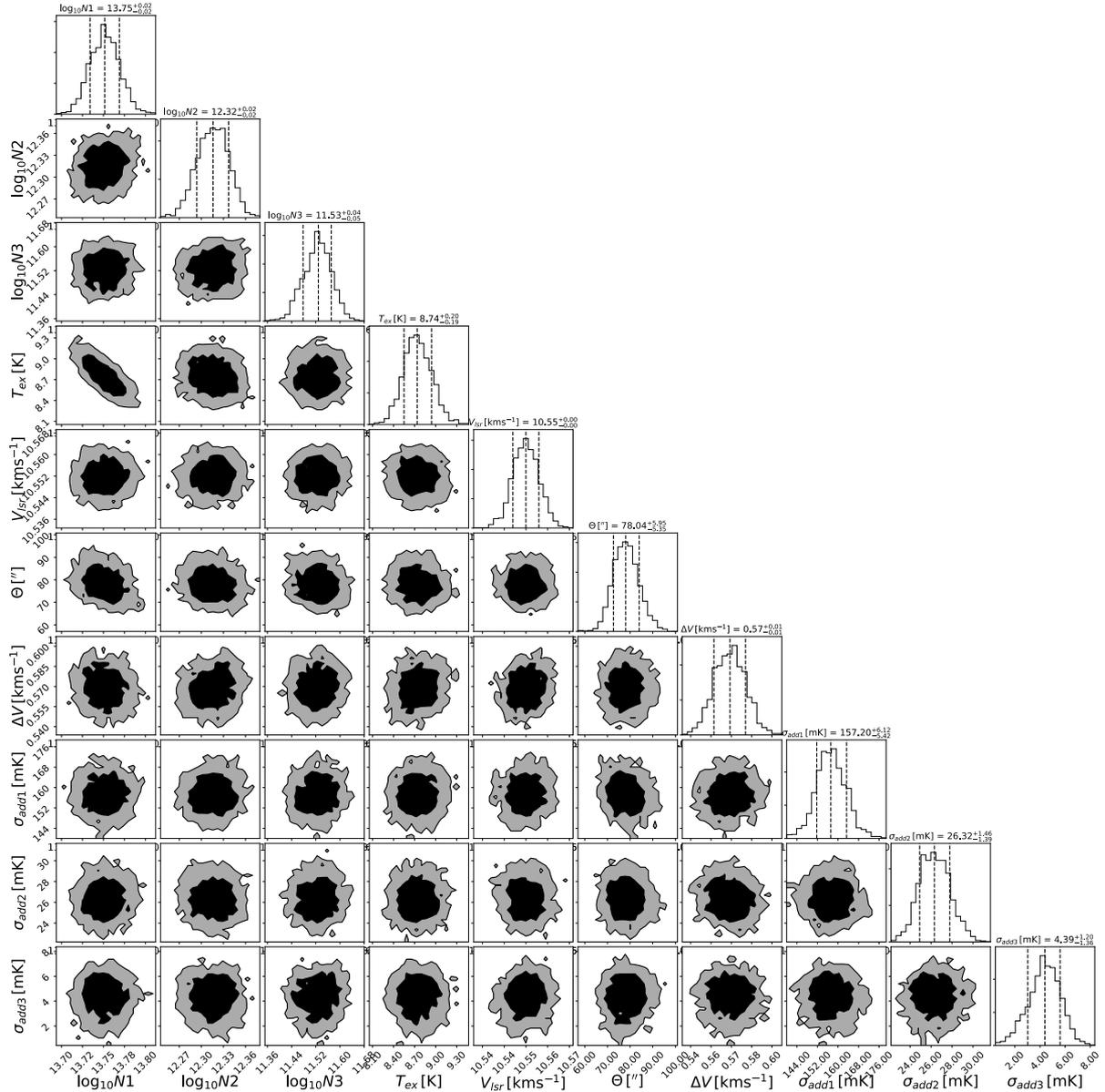


Figure A2: Distributions of the posterior probability for SO, ^{34}SO and S^{18}O column densities ($X1$, $X2$ and $X3$), kinetic temperature (T_{ex}) (assumed to be equal for all the transition and all the SO isotopologues), V_{lsr} is the systemic velocity assumed to be common to all the species, Θ is the source size assuming a gaussian source shape centered in the telescope beam, ΔV is the FWHM of the underlying opacity profile assumed to be common to all the transitions, $\sigma_{\text{add}1,2,3}$ is the additional noise added to each species spectra, it is used to take into account possible model discrepancies by increasing the uncertainties on the other parameters in the Horsehead dense core. Along the diagonal, the one-dimensional probability distribution functions are integrations of the two-dimension probability distribution functions displayed below. The color coding of the two-dimensional histograms runs from 0% (white) to 100% of the peak value (black). The grey contour corresponds to 68% (1σ) of cumulated posterior probability. The Fourier Transform Spectrometer was used with spectral resolutions of 195.3kHz at 1mm and 48.8kHz at 2 and 3mm yielding velocity resolution no higher than 0.17km/s for the lines detected with a peak intensity more than 3 times the noise level. This value is more than 3 times smaller than the estimated linewidth ensuring minimal instrumental broadening.

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