Electron effective mass and mobility in heavily doped n -GaAsN probed by Raman scattering

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We investigate inelastic light scattering by longitudinal optic phonon-plasmon coupled modes (LOPCMs) in a series of heavily Se-doped, n -type $\text{GaAs}_{1-x}\text{N}_x$ epilayers with $x < 0.4\%$. We perform a line shape analysis of the LOPCM spectra to estimate the optical effective mass, m_{opt}^* , and the scattering time of the conduction electrons in GaAsN. We use these results to evaluate an effective carrier mobility for our samples. The values thus obtained, which we compare with measured electron Hall mobilities, indicate that the x -dependence of the mobility in $\text{GaAs}_{1-x}\text{N}_x$ is dominated by the scattering time, rather than by the variation of the electron effective mass. The Raman analysis yields m_{opt}^* values that are lower than those obtained from the band anticrossing model.

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I. INTRODUCTION

Dilute nitride compounds, in particular GaAsN and GaInAsN, have attracted much interest over the last decade because of their remarkable physical properties and their potential for device applications in long-wavelength optoelectronics.¹ It has been established that the incorporation of a few atomic percent of N into the Ga(In)As alloy system leads to a substantial band-gap reduction, as well as to the splitting of the conduction band of the III-V matrix into two highly nonparabolic subbands, E_+ and E_- .²⁻⁵ The simple two-level band anticrossing (BAC) model² provides a reasonably accurate description of the dependence on N content of the energies of E_+ and E_- . Also, it predicts a substantial increase in the effective mass (m_e^*) for the lower energy subband E_- relative to the III-V matrix.^{6,7} However, a complete description of the band structure of dilute nitrides requires detailed calculations of the localized electronic states introduced by N and their interaction with the extended conduction states of the host matrix.^{4,5} While magneto-tunneling measurements have revealed the admixed character of the N-induced states and the anticrossing behavior of the E_- and E_+ subbands in $\text{GaAs}_{1-x}\text{N}_x$ quantum wells,^{8,9} optical and transport techniques have confirmed the increase of m_e^* of conduction electrons in both GaAsN and GaInAsN.^{6,7,10-13}

Most of the optical experiments to determine m_e^* in dilute Ga(In)AsN were performed on undoped material. As a consequence, the m_e^* values obtained in those experiments correspond to the bottom of the E_- conduction subband (m_{e0}^*). In order to use optical techniques to investigate the conduction band (CB) dispersion of Ga(In)AsN and determine m_e^* far above the zone-center minimum of E_- , heavily

doped n -type samples are required. Studies on highly doped material tend to confirm the validity of the BAC model as a description of the energy-wave vector dispersion, $E(k)$, in the case of the GaInAsN quaternary alloy.^{6,7} In contrast, magnetophotoluminescence measurements on undoped $\text{GaAs}_{1-x}\text{N}_x$ suggest that the BAC model underestimates m_{e0}^* for $x \geq 0.1\%$,¹² while experimental studies probing m_e^* in this compound at energies above the CB minimum are presently lacking. Additional experiments are therefore necessary to determine how $E(k)$ and $m_e^*(k)$ depend on N content both in GaAsN and GaInAsN.

Raman scattering by longitudinal optical (LO) phonon-plasmon coupled modes (LOPCMs) has been widely reported in the literature as a method for determining the free-carrier concentration in polar semiconductors.¹⁴⁻¹⁹ Conversely, the investigation of LOPCMs can also be used to optically probe the CB dispersion of the compound under study if the carrier concentration, N_e , is known from independent measurements, since the frequency of the LOPCMs strongly depends on m_e^* . It should be recalled that optical experiments probe the optical effective mass of the carriers, m_{opt}^* , which exhibits a marked N_e -dependence in nonparabolic bands.^{20,21}

In the present work, we use Raman scattering to investigate the LOPCMs in a series of heavily doped n -type $\text{GaAs}_{1-x}\text{N}_x$ epilayers ($0\% < x < 0.4\%$). From the line shape analysis of the LOPCM spectra, we estimate m_{opt}^* and the scattering time, τ , of conduction electrons in our samples. We use the values of m_{opt}^* and τ to obtain an effective electron mobility which we compare with the Hall effect mobility. We find that the values of m_{opt}^* are lower than those predicted by the BAC model. Our analysis suggests that the

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TABLE I. List of n -type Se-doped GaAs_{1-x}N_x epilayers studied in this work.

Sample	x	N_e (cm ⁻³)	μ_{Hall} (cm ² /Vs)	m_{opt}^*/m_e	Γ_e (cm ⁻¹)	μ_{Raman} (cm ² /Vs)
A	0%	1.0×10^{19}	406	0.09	270	384
B	0.10%	5.3×10^{18}	101	0.09	688	151
C	0.20%	7.6×10^{18}	114	0.13	563	127
D	0.23%	7.8×10^{18}	61	0.12	1009	77
E	0.30%	1.5×10^{19}	46	0.13	1346	53
F	0.36%	1.5×10^{19}	51	0.11	1555	55

x -dependence of the mobility in n -GaAs_{1-x}N_x with $x < 0.4\%$ is controlled by the carrier lifetime rather than by the variation of m_e^* .

II. EXPERIMENT

Six Se-doped, n -type GaAs_{1-x}N_x epilayers ($0\% < x < 0.4\%$) were grown on (001) semi-insulating GaAs substrates by metal-organic molecular beam epitaxy. The growth conditions can be found elsewhere.^{22,23} Se was used as the n -type dopant instead of Si because Si and N passivate each other in Si-doped GaAsN due to the formation of Si-N complexes.²⁴ The N concentrations of the films (samples A–F), as determined by high-resolution x-ray diffraction (HRXRD) measurements,²⁵ are given in Table I. The thickness of the epilayers is in the 120–220 nm range, as obtained from the analysis of the HRXRD scans. Hall measurements at different temperatures were carried out in order to determine N_e and the Hall mobility (μ_{Hall}) of the layers. The third and fourth columns of Table I display N_e and μ_{Hall} as obtained at 100 K. Owing to the high N_e values measured ($N_e > 5 \times 10^{18}$ cm⁻³), it can be assumed that the free carriers are degenerate in all the samples studied.

Raman measurements were performed at 80 K in a back-scattering geometry on the (001) face. The spectra were obtained with the 514.5 nm line of an Ar⁺ laser as excitation. Given that the penetration depth of the 514.5 nm light is appreciably smaller than the thickness of the GaAsN epilayers, the contribution of the GaAs substrate to the Raman signal is negligible. A Jobin-Yvon T64000 spectrometer equipped with a charge-coupled device detector was used to record the Raman measurements. The spectra were acquired with the high-resolution triple additive configuration of the spectrometer, with 100 μm slits.

III. RESULTS AND DISCUSSION

Figure 1 shows $z(xy)\bar{z}$ Raman spectra of our Se-doped GaAsN layers (samples B–F). Three main features can be observed in all the spectra. The most intense peak is located at ~ 294 cm⁻¹ and corresponds to the GaAs-like LO phonon of GaAsN.^{26,27} In the case of n -type material, the LO peaks arise from the surface depletion region of the samples.¹⁴ The broad band centered at ~ 268 cm⁻¹ can be assigned to the GaAs-like TO mode of GaAsN.^{26,27} An additional broad feature that is not observed in undoped GaAsN and whose frequency and width change from sample to sample emerges between the TO and LO GaAs-like phonons. We assign this feature to a heavily damped LOPCM. Similar heavily

damped LOPCM bands have been observed in p -GaAs,²⁸ and in n -type InGaAs lattice matched to InP.¹⁹ While the LOPCMs in p -GaAs are heavily damped due to the very low hole mobility, Landau damping effects associated with the low electron effective mass of InGaAs are responsible for the low LOPCM lifetimes in this compound. In the case of n -type GaAsN, the observation of heavily damped LOPCMs instead of the well-known L^- and L^+ coupled modes¹⁴ might be at first sight surprising. Note that, as expected, we observe both the L^+ and L^- bands in the Raman spectra of our n -GaAs sample (inset of Fig. 1), while no L^+ band is observed for any of the n -GaAsN epilayers.

To confirm that the features observed in the spectra of Fig. 1 correspond to a heavily damped LOPCM, we show in Fig. 2 the calculated LOPCM frequency versus N_e for n -GaAs in the high damping regime (solid curve). This curve was obtained by calculating Raman line shapes at different N_e values by using the fluctuation-dissipation formalism of Hon and Faust and the hydrodynamical (HD) model (see Refs. 16 and 29 for details), taking the maxima of the calculated LOPCM curves. For the sake of simplicity, we used for the calculations a constant value of $m_{\text{opt}}^* = 0.09m_e$, which is the value found in heavily doped n -GaAs for $N_e \sim 1$

FIG. 1. Raman spectra acquired at 80 K of the n -GaAsN epilayers studied in this work (samples B–F). The inset shows the Raman spectrum of the n -GaAs epilayer (sample A).

FIG. 2. Calculated N_e -dependence of the frequency of the heavily damped LOPCM in low mobility n -GaAs. The solid curve was calculated with $m_{\text{opt}}^* = 0.09m_e$ and the dashed curve with $m_{\text{opt}}^* = 0.13m_e$. Inset: LOPCM line shape fit (solid line) to the Raman spectrum of sample F (dots).

$\times 10^{19} \text{ cm}^{-3}$.²⁰ A phenomenological electronic damping parameter $\Gamma_e = 1000 \text{ cm}^{-1}$, consistent with the low electron mobilities measured in our heavily doped samples (see Table I and Ref. 30), was used. The resulting curve confirms that, as for the case of p -GaAs,²⁸ in n -GaAs with low electron mobility only a single LOPCM is expected between the TO and LO phonon modes of GaAs. In the case of GaAsN, the low (high) μ_{Hall} (Γ_e) values are a consequence of the N-related disorder.^{31,32} With regard to this, we would like to note that both N_e and μ_{Hall} exhibited a weak temperature dependence in our samples. This suggests that the contribution of N-related alloy scattering to τ in these layers is much stronger than the contribution of other relaxation mechanisms such as inelastic phonon scattering.

The L^+ mode observed in n -GaAs is particularly sensitive to variations in N_e and in m_{opt}^* . However, the heavily damped LOPCM does not display such high sensitivity. We therefore need to evaluate the effect of m_{opt}^* on the LOPCM frequency in order to determine whether the Raman spectra are sufficiently sensitive to effective mass variations, in which case valuable information about m_{opt}^* can be obtained from the LOPCM spectra. Thus, we repeated the calculation of the frequency of the heavily damped LOPCM in n -GaAs as a function of N_e by using a higher value of $m_{\text{opt}}^* = 0.13m_e$. This is close to the values measured by Masia *et al.* in undoped $\text{GaAs}_{1-x}\text{N}_x$ samples with N contents similar to those of our samples¹² and also to the value obtained from magnetophonon resonance measurements in moderately doped $\text{GaAs}_{1-x}\text{N}_x$ with $x = 0.1\%$.¹³

The resulting curve, plotted in Fig. 2 (dashed curve), shows that the frequency of the heavily damped LOPCM is higher (i.e., closer to the uncoupled LO mode) when m_{opt}^* is increased. This result demonstrates that a change in m_{opt}^* has measurable effects on the LOPCM frequency, and hence that the analysis of the Raman spectra can provide useful information about m_e^* in dilute n -GaAsN.

To determine m_{opt}^* in our samples, we have carried out a line shape analysis of the Raman spectra based on the HD mode in the degenerate limit (see Refs. 16 and 29). The calculated line shapes are fitted to the experimental Raman spectra using the N_e values obtained from Hall measure-

FIG. 3. Optical effective mass values, m_{opt}^* , extracted from the analysis of the Raman measurements (dots) and values predicted by the two-level BAC model for the N composition and N_e of the studied samples (open squares). The solid (dashed) line is intended only as a guide to the eye to show the increasing trend of m_{opt}^* with N content in our samples, as derived from the Raman spectra (BAC model).

ments (Table I) and leaving m_{opt}^* and Γ_e as free parameters. Note that the lifetime τ of the LOPCMs, and hence the scattering time of the free carriers, is related to Γ_e through the energy-time uncertainty relation $\tau^{-1} = 2\pi c\Gamma_e$. To avoid possible ambiguities in the fitting procedure, since different combinations of the fitting parameters may lead to satisfactory fits (see for instance Ref. 17 for the case of p -GaAs), we restrict m_{opt}^* and Γ_e to vary within meaningful ranges, compatible with our measured Hall-effect carrier mobilities and with the m_e^* values reported in the literature.^{12,13}

We plot in the inset of Fig. 2 (solid line) the resulting line shape fit to the Raman spectrum of one of the analyzed n -GaAsN films (sample F). Note that prior to the fits the Raman peaks from the TO and LO phonon modes of GaAsN were fitted by Lorentzian line shapes and subtracted from the Raman spectra. Values of $m_{\text{opt}}^* = 0.11m_e$ and $\Gamma_e = 1555 \text{ cm}^{-1}$ were extracted from this fit. As can be seen in the figure, the HD model provides good fits to the heavily damped LOPCM line shapes. We show in the fifth and sixth columns of Table I the m_{opt}^* and Γ_e values obtained from the fits. In the particular case of the n -GaAs epilayer (sample A), m_{opt}^* and Γ_e were obtained from a fit to the L^+ band. The last column of the table shows the mobility of the samples as estimated from $\tau = 1/(2\pi c\Gamma_e)$ and m_{opt}^* with the expression $\mu_{\text{Raman}} = e\tau/m_{\text{opt}}^*$. As can be seen in the table, both μ_{Hall} and μ_{Raman} tend to decrease with increasing x . Interestingly, a quite good agreement between the transport and the Raman mobilities is found, which provides support for the reliability of the Raman analysis.

In Fig. 3, we plot as a function of x the m_{opt}^* values extracted from the fits for all the samples studied in this work (dots). Error bars have been drawn in the figure to take into account possible uncertainties in the determination by Hall-effect measurements of N_e . These uncertainties also lead to significant relative errors in Γ_e , which we estimate to be around 10–20%. For comparison, we also plot in Fig. 3 the

m_{opt}^* values predicted by the two-level BAC model for the N composition and N_e of our samples (open squares). We use the analytical expressions for the effective mass given in Refs. 6 and 7, where the Fermi wave vector k_F is evaluated in the degenerate limit as $k_F = (3\pi^2 N_e)^{1/3}$. To obtain the parameters that enter the BAC model at 80 K, we extrapolate the values given in Ref. 33. As can be seen in Fig. 3, the m_{opt}^* values obtained with the BAC model increase as expected with increasing x . Note that the large m_{opt}^* values obtained with the BAC model for the samples with the highest N content (samples E and F, with $x=0.30$ and 0.36% , respectively) are due to the high free-electron density of these two epilayers (see Table I). For such high doping levels, the BAC model predicts a large CB nonparabolicity, i.e., increased m_{opt}^* values. As can be seen from the figure, however, for the N concentrations of the samples studied in this work, the m_{opt}^* values extracted from the LOPCM spectra are appreciably lower than those predicted by the two-level BAC model.

Although the discrepancy between the Raman data and the predictions of the two-level BAC model could be a consequence of intrinsic uncertainties in the analysis of the LOPCM spectra, it is quite likely that the BAC model offers a too simplistic description of the electron effective mass in GaAsN. The BAC model seems to correctly predict the large N-induced increase of m_e^* for $x > 1\%$ in n -type $\text{In}_y\text{Ga}_{1-y}\text{As}_{1-x}\text{N}_x$.⁶ However, in the case of undoped GaAsN, magnetophotoluminescence measurements have revealed that m_{e0}^* is sizably higher than that predicted by the BAC model for the composition range of the samples studied here. These experimental results can be understood in terms of a description based on a linear combination of isolated nitrogen states,⁵ which shows that for the particular case of $0.1\% < x < 0.2\%$ the CB-edge electronic states of $\text{GaAs}_{1-x}\text{N}_x$ are strongly hybridized with N cluster states. Such a strong hybridization is responsible for the large m_{e0}^* values measured in this composition range.¹² However, for heavily doped n -GaAs $_{1-x}$ N $_x$ and the N compositions of the samples studied here, the Fermi energy lies well above the N cluster states (i.e., hundreds of meV depending on x and N_e), and therefore only a weak interaction exists between the extended electronic states around the Fermi surface and the N-related localized cluster states. As a consequence, the enhancement of the electron effective mass due to the hybridization with N cluster states should play a much weaker role in our samples. These arguments can explain why, unlike the m_{e0}^* values measured by magnetophotoluminescence in undoped GaAsN, the m_{opt}^* values extracted from the LOPCM spectra are not larger than the values predicted by the two-level BAC model. However, the fact that the Raman data are below the predictions of the BAC model (Fig. 3) remains unexplained. Further work is necessary to confirm these results and to ascertain how m_e^* is affected by N_e .

Interestingly, the fact that m_{opt}^* is lower than predicted by the BAC model has important implications for the mechanisms responsible for the low electron mobility of heavily doped GaAsN. The m_{opt}^* values derived from our analysis, together with the x -dependence of μ_{Hall} and μ_{Raman} , indicate that the electron mobility in GaAsN is limited more by the decrease of the electron scattering time with increasing N

content as a consequence of N-related disorder than by changes of m_{opt}^* with increasing N-content and/or carrier concentration.

IV. CONCLUSION

We have found that N-related disorder in n -GaAs $_{1-x}$ N $_x$ gives rise to a single heavily damped LOPCM even for N contents as low as 0.1% . Despite the lower sensitivity to N_e or m_e^* variations of the heavily damped LOPCM in comparison to the L^+ coupled-mode branch observed in n -GaAs, a careful analysis of the Raman spectra provides a means of estimating the optical effective mass of the free electrons, m_{opt}^* , in the n -GaAs $_{1-x}$ N $_x$ epilayers. We find that the m_{opt}^* values obtained from the fits are lower than those predicted by the BAC model in heavily doped n -GaAsN. These results suggest that the x -dependence of the measured electron mobility is mainly determined by the scattering time.

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