Magnetic properties engineering of nanopatterned cobalt antidot arrays

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Abstract

We report on the study of arrays of 60 nm wide cobalt antidots,
nanopatterned using focused ion beam milling. Square and hexago-

nal symmetry arrays have been studied, with varying antidot densities and lattice constant from 150 up to 300 nm. We find a strong increase of the arrays' magnetic coercivity with respect to the unpatterned film, which is monotonic as the antidot density increases. Additionally, there is a strong influence of the array symmetry to the in-plane magnetic anisotropy: square arrays exhibit fourfold symmetry and hexagonal arrays exhibit sixfold symmetry. The above findings are corroborated by magnetic imaging and micromagnetic modeling, which show the magnetic structure of the arrays to depend strongly on the array morphology.

Keywords: Co antidot arrays, focused ion beam, MOKE magnetometry, AFM, MFM, micromagnetic modeling

1 Introduction

Magnetic antidot arrays are groups of ordered holes created on a continuous magnetic film. They are being intensively investigated as candidates for high-density storage media [1, 2], magnonic crystals with potential application in microwave devices [3, 4], magnetically-active plasmonics [5], and lately for magnetic biosensing applications [6].

The main non-material-dependent parameters that influence the array magnetic properties are its symmetry and lattice constant and the antidot shape and size. Antidot arrays studies have been mainly focused on square or hexagonal symmetry arrays of circular antidots [7–9], although there are as well studies of other symmetries, like e.g. tetragonal [10] or honeycomb [7] and of square-shaped antidots [11].

Most of the antidot array studies concern μm - and sub- μm -scale antidots, fabricated by patterning methods like e-beam lithography [2, 11, 12] and UV lithography [13]. On the other hand, the principal means for attaining nm-scale antidot arrays are various self-assembly techniques employing porous anodic alumina [8, 14], colloidal lithography [15], block copolymer templates [16], or nanochannel glass [17]. However, there are significant inherent drawbacks in all of the self-assembly fabrication methods, mainly regarding the limitations of the array symmetry and/or size and the extent of

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the symmetric domains, which is on the order of some μm . Only recently advanced fabrication techniques have been introduced for the study of nm-scale antidot arrays, as for example the use of focused ion beam (FIB) patterning [18], which allow for obtaining antidot arrays of any symmetry extending over areas of several tens of μm or even mm.

In this article, we present our work on nm-scale antidot arrays fabricated using FIB nanopatterning. Magneto-optical Kerr effect (MOKE) magnetometry has been used to characterize the magnetic properties of the arrays. We find an intense increase of the magnetic coercivity (H_C) of the film after patterning, while there is also a monotonic increase of H_c as the density of nanoholes increases. Additionally, the in-plane anisotropy axes of the patterned film depend strongly on the array symmetry, with alternating hard and easy axes following the fourfold symmetry of the square arrays, or the sixfold symmetry of the hexagonal arrays. Finally, high-resolution magnetic imaging and micromagnetic modeling have been employed and we find the arrays magnetic structure to be commensurate to the array morphology.

2 Methods

For sample fabrication, first a continuous Ti(2 nm)/Co(10 nm)/Au(10 nm) stack was sputter-deposited in an ultra-high vacuum chamber (base pressure $1 \cdot 10^{-10}$ Torr) on a monocrystalline (0001) sapphire substrate from MaTecK GmbH. The substrate was rotated around its normal axis during the deposition in order to avoid the formation of a strong magnetic anisotropy during the growth of the film. The Ti underlayer promotes adhesion of the stack, while the Au capping layer protects Co from oxidation.

Antidot arrays were directly etched on the continuous stack using an IonLine FIB machine, with 30 keV Ga ions and 6.9 pA ion current. For each lattice position of the array, the stack was exposed to the focused beam for 0.17 seconds, thus etching each one of the antidots. The exposure time corresponds to a dose of 1.2 pC, that was enough to etch the sample at a depth of 42 nm, 20 nm more than the whole metallic stack thickness.

Atomic/Magnetic Force Microscopy (AFM/MFM) measurements have been performed using a Bruker Dimension Icon microscope and commer-

cial AFM/MFM probes (Bruker MESP). MFM images were obtained using the phase imaging double-pass tapping-mode: surface topography is recorded during the first pass and then the tip is lifted at a certain height and the magnetic contrast is recorded. As the MFM tip is magnetized along the axis vertical to the sample, the observed contrast originates from magnetic charges on the sample surface. All microscopy images were processed using the WSxM software [19].

Longitudinal MOKE hysteresis loops of the arrays were obtained using a Nanomake 2.0 (Durham Magneto-optics Ltd.) setup, using 635 nm laser wavelength. The laser spot was focused to a 3 μm diameter. The spot was placed into each antidot array using the robotic motion stage which allows the movement of the sample with a precision of 1 μm . In order to check that the laser spot is placed in the right position, the longitudinal reflectivity was measured. Besides, the focused laser spot and the sample surface can be viewed together. The sample was rotated using a rotation stage and the laser spot was reallocated using the same procedure above mentioned. Magnetic field was applied along the 0°, 45°, and 90° direction when measuring the square arrays and along 0°, 30°, 60° and 90° direction when measuring the hexagonal arrays (see figure 1).

Micromagnetic modeling has been performed using the GP Magnet program¹ software that allows us to simulate three-dimensional systems of large volume using graphic processing units. Under this frame, the ferromagnetic system is divided into cubic cells with a uniform magnetization inside each cell. For the calculations we have considered a circular sample (diameter 8 μm) of Co antidots defined by a thickness of 8 nm and a pore diameter of 55 nm, which are arranged in a square array with a lattice constant of 300 nm. In order to obtain an adequate description for the Co sample, the size of the cubic cell has to be smaller than the exchange length of the material, defined by [20] $\Delta_d = \sqrt{2A/\mu_0 M_S^2} = 4.7$ nm, where $A = 30 \times 10^{-12}$ J/m is the exchange stiffness constant and $M_S = 1400 \times 10^3$ A/m is the saturation magnetization. Thus, we have chosen a cell size of 4 x 4 x 4 nm³, which implies that the micromagnetic simulations involve 8 million cells and 1108 antidot elements. Additionally, we included a small uniaxial anisotropy of

¹GoParallel S.L., <http://www.goparallel.net/index.php/gp>

2400 J/m³ in 90° direction, which was obtained from the experimental measurements (see discussion related to figure 6 (a)). In all cases the damping constant was $\alpha = 0.5$.

3 Results and discussion

3.1 Sample morphology

AFM imaging (see figure 1) reveals that the surface morphology of the initial film has very low roughness (root mean square roughness is 0.1 nm), which is desirable for the ulterior FIB nanopatterning.

Figure 1: Typical morphology of the arrays obtained by AFM. (a) Design and global view of the arrays: B is 15 μm and C is 20 μm . The color scale (from dark to bright) is from 0 to 45 nm. Typical images of square (b) and hexagonal (c) arrays. The color scale is from 0 to 15 nm. (d) Typical antidot morphology obtained at image (c). The color scale is from 0 to 12 nm. Straight lines indicate directions where line profiles are obtained and shown in (e). All the samples share the same coordinates, as-defined in this figure.

After patterning each antidot array has the shape of a disk (diameter 15 μm), for avoiding any shape anisotropy, surrounded by a circular trench that magnetically decouples the array from the rest of the layer (see figure 1

(a)). The trench was etched using a 21 mC/cm² ion beam dose for obtaining a depth equal to the one of the antidots. Moreover, for the sake of comparison, regions confined by a trench but without any patterning were also prepared, i.e. defining Co disks with 20 μ m diameter.

The studied symmetries are square and hexagonal (see figures 1 (b) and 1 (c)). From a magnetic viewpoint each nanohole may be considered as a defect, since they act as pinning centers for the domain-wall (DW) motion during magnetization reversal [21]. If a is the lattice constant (nearest neighbor centre-to-centre distance) and d the hole diameter, the defect volume density (DVD), which is the ratio of the surface covered by holes to the total surface, is given by $\frac{\pi}{4}(\frac{d}{a})^2$ for the square arrays and by $\frac{\pi}{2\sqrt{3}}(\frac{d}{a})^2$ for the hexagonal ones.

The diameter of the antidots is determined at figure 1 (e) as the full-width at half maximum of the hole, at the level of the Co layer, and it is measured to be 60 nm. The antidot appears to have a “tapered” geometry, however, this is due to the convolution with the AFM tip, which has a pyramid geometry with 25° slope. Four different arrays were etched for each symmetry, having lattice constant equal to 150, 200, 250, and 300 nm. The DVD is 0.126, 0.071, 0.045 and 0.031 for the square arrays and 0.145, 0.082, 0.052 and 0.036 for the hexagonal ones, respectively.

A striking characteristic of sample morphology is the apparent “rim” around the antidots: this appears as a 2.5 nm depression when approaching the antidot center, followed by a 1 nm elevation, while its average width is 18 nm. This pattern is consistently repeated around every antidot studied. It is interesting to note that a similar effect has been previously reported on FIB etched antidots and shown to be a local film alteration due to the tail of the Gaussian-like section of the ion beam [18].

3.2 Hysteresis curves

Figure 2 (a) shows MOKE loops obtained at an unpatterned Co disk along the 0° and 90° directions. It is clear that the unpatterned film has a small uniaxial in-plane magnetic anisotropy; the easy axis (EA) is along 90°, with $H_C=21$ Oe and an almost square loop: the remanence magnetization to sat-

Figure 2: Representative MOKE loops obtained along various magnetic field directions. (a) Unpatterned area confined by a circular trench. (b) Square array. (c) Hexagonal array. In both cases the lattice constant is 250 nm, resulting in respective defect volume density values of 0.071 and 0.082. Please note the smaller magnetic field axis scale used in (a).

uration magnetization (M_R/M_S) value is 0.95. The 0° direction is the hard axis (HA), as H_C is 14 Oe and M_R/M_S is 0.82. However, significant hysteresis is observed, in conjunction to the non-epitaxial polycrystalline structure of the films; in the past it has been shown that vacuum deposited polycrystalline Co films have hcp crystallites, not completely randomly oriented, that induce an in-plane uniaxial anisotropy [22]. In our case, the mono-crystalline sapphire substrate should be additionally taken into account, as it probably induces a preferred crystallites texture, in spite of the fact that it was rotating during deposition.

Figure 2 (b) shows representative square array MOKE loops (lattice constant is 250 nm and DVD is 0.071). The increase of H_C with respect to the unpatterned film is pronounced. Small steps appear at low field, i.e. of the same magnitude as the H_C values of the unpatterned film. This suggests a facile DW motion between antidots (at the unpatterned regions of the array) and strong DW pinning at antidots, indicating a combined effect of the uniaxial magnetocrystalline anisotropy of the unpatterned film and antidot array symmetry.

The 45° direction (second-nearest-neighbor) is the magnetic anisotropy EA (H_C is 186 Oe and M_R/M_S is 0.95). The 0° direction (nearest-neighbor) is a HA (H_C is 120 Oe and M_R/M_S is 0.78) and it coincides with the unpat-

terned film HA. However, although the 90° direction is also along nearest-neighbors, H_C is smaller (100 Oe) but M_R/M_S is higher (0.88). This could be attributed to a convolution effect with the unpatterned film EA, which lies along the 90° direction; in the past it has been shown that a small in-plane uniaxial anisotropy may greatly influence magnetization reversal [23]. It should be noted that similar results are obtained for the rest of the square symmetry arrays. Finally, a similar behavior has been also reported in the past for square symmetry Co antidot arrays [9], although it concerned μm -scale antidots and only one antidot density was studied.

Figure 2 (c) shows representative hexagonal array MOKE loops (lattice constant is 250 nm and DVD is 0.082). There is also a multi-fold increase of H_C with respect to the unpatterned film. The lowest H_C is obtained at 0° (66 Oe), a nearest-neighbor direction, whereas the highest at 30° (129 Oe), a second-nearest neighbor direction. Intermediate H_C values are obtained at 60° (85 Oe) and at 90° (98 Oe).

From MOKE loops, the H_C and M_R/M_S values are determined for all samples and shown in figure 3 as a function of the applied magnetic field direction. In most cases there is a clear dependence of H_C and M_R/M_S on direction and the same trend is usually maintained for a given array symmetry. For square arrays, the maximum H_C and M_R/M_S values are obtained along the 45° direction (second-nearest-neighbors), indicating that this is a magnetic anisotropy EA. The only exception is the array with the lowest DVD (0.031), where a monotonic decrease of H_C and increase of M_R/M_S is observed, suggesting that for the lowest DVD the array magnetic anisotropy is dominated by the unpatterned film uniaxial anisotropy.

For hexagonal arrays, it is generally observed that H_C and M_R/M_S have an opposite variation trend making the interpretation of data challenging. The maximum H_C values are along 30° and 90° directions (second-nearest-neighbors), except for the array with maximum DVD (0.145) where the inverse trend is observed. On the contrary, M_R/M_S values have local maxima along 0° and 60° directions (nearest-neighbors). The only exception is the array with minimum DVD (0.036) where a monotonic increase is observed, again indicating that the array magnetic anisotropy is dominated by the unpatterned film uniaxial anisotropy.

Figure 3: H_C values as a function of magnetic field direction for (a) square and (b) hexagonal symmetry arrays. M_R/M_S values for (a) square and (b) hexagonal symmetry arrays. Data for various defect volume density (DVD) values are shown. Brown stars indicate the values obtained at an unpatterned area confined by a circular trench.

It is worth pinpointing that the remanent magnetization barely depends on DVD, whereas the coercivity strongly depends on it. This behavior indicates that the separation between holes does not affect the type of domain walls that are formed, but it strongly alters their pinning during reversal. In fact, the MFM experiments that will be discussed later showed the same type of domain walls for all the arrays with the same symmetry.

In order to highlight the importance of DVD on the strength of the pinning, figure 4 shows all the H_C data obtained as a function of DVD. For both array symmetries, there is a monotonic increase of H_C as DVD increases. The above are in accordance with previous studies which predict an increase of H_C as the density of domain-wall pinning centers (in this case the antidots) increases [21]. The maximum H_C value for both symmetries is obtained at the maximum DVD value and it is 318 Oe for the square symmetry arrays

at 45° and 268 Oe for the hexagonal symmetry at 60°.

Figure 4: Variation of H_C with respect to defect volume density. Square arrays: field direction along first neighbors (filled squares) and second neighbors (open squares). Hexagonal arrays: field direction along first neighbors (filled triangles) and second neighbors (open triangles). Unpatterned area confined by trench: field direction along 0° (filled circle) and 90° (open circle).

The arrays with the lowest DVD exhibit small H_C dispersion, indicating that at low DVD values antidot density prevails over antidot symmetry in tailoring film magnetic properties. However, as DVD increases, the array symmetry becomes more important: H_C values are more dispersed and the maximum value is always at the second-nearest-neighbor direction, for both symmetries.

The only exception to the above-mentioned tendency appears at the hexagonal array with the highest DVD, which exhibits opposite behavior: the 60° direction has the highest H_C , while at 0° H_C is almost equal to 90°. This could be attributed to the onset of a “crossover” from antidot (continuous magnetic film with an array of holes) to dot (an array of magnetically isolated nanostructures) magnetic behavior previously reported [18]; it has been shown that for square symmetry array and DVD values higher than 0.130, despite the fact that the film is still magnetically continuous, emerges an intermediate regime between antidot and dot, due to the close proximity

of neighboring regions affected by the tail of the Gaussian-like section of the ion beam. It should be noted that although we try to interpret the behavior of hexagonal symmetry arrays based on findings concerning square symmetry arrays, the study presented in reference [18] takes into account only DVD, without considering the effect of symmetry or applied field direction. Thus, it could be assumed that this “crossover” effect is more pronounced along second-nearest-neighbor directions at hexagonal arrays (30° and 90°), resulting in the observed behavior.

3.3 Magnetic imaging and micromagnetic modeling

MFM imaging has been performed for obtaining microscopic insight of the arrays magnetic structure. All images show the magnetic structure of the arrays in remanence state: first a 15 kOe magnetic field is applied along a given direction in order to magnetically saturate the sample and then the field is reduced to zero before imaging.

Figure 5 (a) shows the typical magnetic structure of an unpatterned Co layer confined by circular trench. Magnetic domains have random structure and sizes from several tens to hundreds of nm, much larger than the average grain size, indicating strong magnetic coupling between grains. Arrows indicate abrupt signal changes, which correspond to DW drag effects because of the magnetic stray field of the MFM tip, which is in coherence with the low H_C value of the unpatterned film.

Figure 5 (b) shows the typical magnetic structure of a 200 nm hexagonal array at remanence state, after applying magnetic field along the 30° direction. It is immediately clear that the magnetic structure is commensurate to the morphology of the array. Dark contrast stripes correspond to super-DWs [12] and they are aligned along the 0° and 120° (equivalent to 60°) directions. As before, there is significant DW dragging due to the MFM tip stray field, although H_C is 113 Oe, much higher than the unpatterned film. It should be noted that similar magnetic structure is observed for the rest of the arrays and applied field directions, suggesting that this is the equilibrium magnetic structure of the hexagonal arrays. This absence of discrepancy between directions is attributed to the non-perfect alignment of

Figure 5: MFM images of the samples' magnetic structure. (a) Unpatterned Co layer confined by circular trench. (b) Hexagonal array (200 nm period), magnetic field along 30°, and (c) the corresponding AFM image. Square array (300 nm period): (d) magnetic field along 90° and (e) magnetic field along 45° (the square frame indicates the simulated area shown in figure 6), and (f) the corresponding AFM image. The scale bar is 1 μm and all figures have the same area. The color scale at the MFM images is from 0 to 0.9° and at the AFM images is from 0 to 25 nm. Lift height during MFM imaging was always 40 nm.

the sample during the magnetization process before MFM imaging and the subtle variation between alternating EAs and HAs.

Figure 5 (c) shows the magnetic structure of the 300 nm square symmetry array, after applying magnetic field along the 90° direction. In this case only vertical super-DWs are apparent, which are commensurate to the square symmetry of the array. As before, there are several DW-drag events, although H_C is 72 Oe. Figure 5 (d) shows the magnetic structure of the 300 nm square symmetry array, after applying magnetic field along the 45° direction. Apparently there is some distinction from the 90° case: the image has mixed dark and bright contrast aligned along the 45° directions, with only a few

vertical super-DWs. The overall contrast is mainly bright, in accordance to the high remanence magnetization obtained from the MOKE loops for magnetic field applied along the 45° direction. The most striking difference is the total absence of DW-drag: although H_C is 79 Oe, only slightly higher than the 90° direction and much lower than the hexagonal symmetry array imaged in figure 5 (c), the stray field from the MFM tip does not affects the array magnetic structure.

In order to understand more deeply the magnetic structure of the arrays and the formation of super-DWs, micromagnetic simulations were performed [24]. Simulations consider an external magnetic field applied at 45° , from saturation (10 kOe) to -30 Oe, passing through the remnant state (0 Oe).

When a 10 kOe field is applied, all magnetic moments are pointing in the same direction as the external field (45°). Thus, it can be said that the sample is saturated (see figure 6 (b)). Then, when the external magnetic field is set to 0 Oe (figure 6 (c)), most of the magnetic moments relax to the direction along the easy magnetization axis (90°) defined by the small magnetic anisotropy measured experimentally. However, those magnetic moments closest to the edge of the sample remain pinned at 45° because of the edge effect (the edge tries to align magnetic moments in 0° , while the magnetocrystalline anisotropy favors the direction of 90°). Thus, on average, the magnetic moments will remain pinned at 45° . Once a field of -10 Oe is applied at 45° , the magnetic moments closest to the surface remain pinned at 45° while the inner magnetic moments reverse their magnetization, thereby forming a soft U-shaped magnetization (figure 6 (d)). If the field is further reduced to -20 Oe, there is simply an increase of the angle at which the magnetic moments face each other in the U-shaped magnetization (figure 6 (e)). Finally, at a field of -30 Oe, the magnetic moments generate 180° super-DWs (figure 6 (f)), corresponding to the magnetic contrast observed in the MFM images. Thus, micromagnetic simulations intend to give a qualitative explanation of how patterning a thin film affects the formation of magnetic domains on its surface. From these simulations we can conclude that an antidot pattern created on a thin film induces linear magnetic domains.

Figure 6: Simulated magnetic structure of the array samples. a) Circular sample of $8 \times 8 \mu\text{m}^2$ of Co antidots defined by a thickness of 8 nm and a pore diameter of 55 nm, which are arranged in a square array with a lattice constant of 300 nm. The axes show the directions according to the experimental results. The inset white square corresponds to the area shown in the following figures. The external magnetic field is applied at 45° with an intensity of b) 10 kOe, c) 0 Oe, d) -10 Oe, e) -20 Oe and f) -30 Oe, in order to reproduce the formation of super-DWs in the remnant state. The color scale (red-white-blue) corresponds to divergence from -0.02 to 0.02.

4 Conclusions

FIB has allowed for fabricating antidot arrays with 60 nm hole diameter and long-range order, following two symmetries: square and hexagonal. Various antidot-to-antidot distances have been studied for each symmetry. We have shown the important effects of antidot array symmetry and defect volume density on the coercivity and anisotropy of magnetic thin films: coercivity increases with the density of antidots and magnetic anisotropy axes strongly depend on array symmetry. MFM images show the magnetic structure of the arrays to be commensurate to their morphology, while micromagnetic

simulations indicate the mechanisms of super-DW creation in magnetic antidot arrays. The above findings provide further insight for fine tuning the magnetic properties of thin films employing arrays of antidots.

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