Sensitivity on Earth Core and Mantle densities using Atmospheric Neutrinos

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Abstract. Neutrino radiography may provide an alternative tool to study the very deep structures of the Earth. Though these measurements are unable to resolve the fine density layer features, nevertheless the information which can be obtained are independent and complementary to the more conventional seismic studies. The aim of this paper is to assess how well the core and mantle averaged densities can be reconstructed through atmospheric neutrino radiography. We find that about a 2% sensitivity for the mantle and 5% for the core could be achieved for a ten year data taking at an underwater km³ Neutrino Telescope. This result does not take into account systematics related to the details of the experimental apparatus.

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1. Introduction

Earth tomography with high-energy cosmic neutrinos is quite an old idea [1]-[8] that seems to provide a viable independent determination of the internal structure of our planet. In particular, cosmic neutrinos with an energy of a few TeV have an interaction length of the order of the Earth radius and thus sample the density profile along the path. Detecting at a km³ Neutrino Telescope the flux of emerging charged leptons (mainly muons) versus the arrival direction can be therefore, a promising approach for measuring at least some of the features of the Earth density radial profile as recently discussed in Ref. [8]. In particular, such a measurement can provide information concerning the core/mantle boundary which determines the geodynamo as well as the feeding mechanism of hotspots at the surface [9]. The standard body-wave and free oscillation studies, even though are much more precise tools than what it can be reasonably obtained by neutrino radiography, are not free of ambiguities related to the local nature of the seismometer arrays and moreover, to the capacity of free-oscillation data to detect one-dimensional structures only.

At the energy of few TeV the neutrino flux crossing the Earth is essentially made of Atmospheric Neutrinos (AN) which are produced in collisions of cosmic rays with nuclei in the Earth's atmosphere. The AN spectrum decreases very steeply with energy, as the flux is proportional to $E^{-\gamma}$ with $\gamma \simeq 3 - 3.7$ [10]. Until energies of the order of 100 TeV the AN are the dominant contribution to the whole neutrino flux and this is compatible with **AMANDA** bound on extragalactic neutrinos [10, 11]. On the other hand, at higher energies a considerable prompt neutrino flux from the decay of heavy mesons is expected, as well as an extragalactic neutrino component. We are limited in our analysis by the transparency of the Earth to the neutrinos of the lowest energies, and by their prompt and yet uncertain extragalactic flux components at the highest energies. So, we use the electron and muon (anti)neutrino fluxes calculated in Ref. [12] by using the “modified DPMJET-III” in the energy range ($10^3 - 10^4$) GeV and extrapolating as a power-law behavior till 10^5 GeV. These fluxes show a zenith angle dependence, as shown in Fig. 1, which should be taken into account since the relative numbers of neutrino induced charged lepton events in the detector in different angular bins are crucial observables for our analysis. We notice that neutrino flavor oscillations can be neglected in the energy range we are interested in, since they are only effective at energies lower than 1 TeV [13, 14].

The detection perspectives of high energy neutrinos have received a great interest in the past few years, in view of several proposals and R&D projects for Neutrino Telescopes (NT's) in the deep water of the Mediterranean sea. In particular, the construction of the **ANTARES** NT [15] was recently completed and it is taking data. **ANTARES** [15], as well as **NEMO** [16] and **NESTOR** [17], are involved in research and development projects which in the future could lead to the construction of a km³ telescope as pursued by the **KM3NeT** project [18]. Furthermore, **IceCube** experimental setup, a cubic-kilometer under-ice neutrino detector [19] is now under construction and already taking data. It

Figure 1. Atmospheric electron and muon (anti)neutrino fluxes for different arrival directions, with θ denoting the zenith angle. We use the results of [12] and extrapolate the power-law behavior above 10^4 GeV.

applies and improves the successful technique of **AMANDA** [20] to a larger volume.

The sensitivity of a NT to the very deep geological structures is provided by the charged lepton event rate as a function of the arrival direction, which shows a remarkable dependence upon the adopted radial matter density profile, as discussed in details in Ref. [8]. In particular, in this work the authors point out the possibility to use the arrival direction distribution of events in ten years of data taking at **IceCube**, to distinguish, at 3σ level, between the Earth matter density profile of the Preliminary Reference Earth Model (PREM) [21] and a homogeneous Earth toy model. However, in Ref. [8] no indication of the real sensitivity of neutrino Earth radiography to PREM parameters is reported. In this paper we present a study of the sensitivity of an underwater NT to Earth interior in the case of the *simplified* PREM (sPREM) shown in Fig. 2, where core and mantle densities are assumed to be constant and hereafter denoted by ρ_c and ρ_m , respectively. To assess how well these two parameters can be reconstructed, we exploit a likelihood analysis where the reference Earth model corresponds to the average values predicted by sPREM, $\rho_c = 11.0 \text{ g cm}^{-3}$ and $\rho_m = 4.48 \text{ g cm}^{-3}$ with the core/mantle boundary fixed at 3450 km from the center of the Earth. We use as physical observable

Figure 2. The Preliminary Reference Earth Model radial density [21] (dashed line). The solid line corresponds to a *simplified* PREM (sPREM), where core and mantle densities are assumed to be constant.

the expected event rate as a function of the arrival direction, which accounts for muon (anti)neutrino induced processes and, only for neutrino conversions inside the NT, for the electron (anti)neutrino contribution as well.

2. The Monte Carlo for neutrino interaction in the Earth

We choose as an example of undersea NT a km^3 detector placed at NEMO site, and generate a large number of tracks crossing the NT fiducial volume (for simplicity a cube of 1 km edge placed at 100 m from seabed) by means of a detailed Digital Elevation Map of the under-water Earth surface, which is available from the Global Relief Data survey (ETOPO2), a grid of altimetry measurements with a vertical resolution of 1 m averaged over cells of 2 minutes of latitude and longitude [22]. Details can be found in [23, 24]. The simulation is performed following tracking particles inside the rock with a maximum of 5 zones of 3 different densities, corresponding to the two regions of sPREM, as well the crust thin layer. This leads to three possible kinds of neutrino tracks inside the Earth: those going i) through the core, ii) through mantle and crust, and iii) through the crust only. We inject a number of electron and muon (anti)neutrinos for a given energy at each angular bin according to the flux of AN given in [12]. We do not consider neutrino tau contribution in this range of energy, since we are neglecting neutrino oscillations.

The detectable events can be classified in two categories: the *track* events where the charged lepton is produced outside the fiducial volume, and the *contained* ones, where neutrino converts inside the NT.

Concerning muon neutrinos, which provide the main contribution to the total amount of events, the Monte Carlo simulates their interaction in the Earth and propagates the outgoing lepton. In this respect, we take into account the phenomenon of neutrino regeneration for a neutral current neutrino interaction. In the case of a charged current neutrino interaction, we consider the muon energy loss in matter due to ionization, bremsstrahlung, e^+e^- pair production and nuclear interaction. An energy threshold of 1 TeV is considered in counting the muons detected in the fiducial volume and the condition of a minimal track length of 300 m in the apparatus defines detectable events. This energy threshold value results to be a good compromise between the need of a sufficiently large statistics, thus a not too high lower energy threshold, and the necessity to reduce the neutrino interaction length in order to increase the sensitivity to Earth density profile. Contained events, which take contributions both from electron and muon neutrinos, are treated separately. To be conservative, in analogy to track ones we assume that they are detected if charged lepton energy is larger than 1 TeV. This, of course, does not take into account the amount of energy released in the hadronic channel accompanying the charged current interaction that for contained events could be in principle detectable. Since the contribution of contained processes is in any case subdominant with respect to the track one, we assume this conservative point of view which has the advantage to make our analysis almost independent of the details of the experimental apparatus. In Fig. 3 we show the angular distribution of the total number of events simulated with our Monte Carlo (at these energies the neutrino and detected charged lepton are collinear) with ϑ the zenith angle of the emerging charged lepton, i.e. upgoing neutrinos correspond to $\cos \vartheta = 1$. Here, from top to bottom, the solid line represents track-muons, the dashed one the contained-muons and finally the dotted line the contained-electrons. The electron neutrino contribution is typically smaller by one order of magnitude than the corresponding muons due to the less abundant ν_e incoming flux (see Fig. 1).

In Fig. 4 we show the total amount of events as a function of both the charged lepton energy and the arrival direction. As expected the main contribution comes from almost horizontal processes just close to the chosen energy threshold.

In Table 1 we report the angular distribution of ν_μ induced events in 10 years of operation of a NT placed at NEMO site as predicted by our analysis for the sPREM, and compare it with the PREM expectation of Ref. [8] obtained for IceCube. The energy threshold for muons has been fixed to 10 TeV since the corresponding values for 1 TeV are absent in Ref. [8]. As a result of this comparison the two predictions can be considered quite in fair agreement if one takes into account the difference in the adopted Earth density profiles and in the level of detail of the simulation approaches. In fact, differently than in Ref. [8] where a complete Monte Carlo of IceCube is exploited, we are not assuming any details of the experimental apparatus, but simply assume a cube with a 1 km³ volume and acceptance only constrained by the requirement that charged leptons should have a track length in the apparatus not smaller than 300 m.

Figure 3. The zenith angle distribution of neutrino induced events in a NT for a charged lepton energy threshold of 1 TeV and the sPREM. The up-going neutrinos correspond to $\cos\vartheta = 1$. From top to bottom, the solid line represents track-muons, the dashed one the contained-muons and finally the dotted line the contained-electrons.

Figure 4. The total amount of events as a function of both the arrival direction and the charged lepton energy. Larger boxes correspond to a larger number of events.

$\cos \vartheta$	sPREM	PREM [8]
[0, 0.17]	2463	1132
[0.17, 0.33]	1196	736
[0.33, 0.50]	714	537
[0.50, 0.67]	513	429
[0.67, 0.83]	306	359
[0.83, 1.0]	210	254

Table 1. The angular distribution of ν_μ induced events in 10 years of operation of a NT placed at NEMO site as predicted by our analysis for the sPREM, and the PREM expectation of Ref. [8] for IceCube. The energy threshold for muons is 10 TeV.

3. Results and Conclusions

In order to carry out a sensitivity study, we vary the mantle and core densities in a grid of 5×4 values: $\rho_m = \{4.00, 4.25, 4.50, 4.75, 5.00\}$ g cm $^{-3}$, $\rho_c = \{9.0, 10.0, 11.0, 12.0\}$ g cm $^{-3}$, and calculate with the Monte Carlo the corresponding number of events in ten years of data taking, $N_i(\rho_m, \rho_c)$, in the five equally spaced angular bins of $\cos \vartheta$ in the interval [0,1]. We assume an Earth radius of 6378 km and a crust with a thickness of 37 km, while the crust density is fixed to be 2.68 g cm $^{-3}$. For each pair of chosen values of ρ_m and ρ_c , the radius of the core/mantle boundary R_c is then constrained by the mass of the Earth.

We then compare the counts $N_i(\rho_m, \rho_c)$ with the expected counts N_i^0 for the benchmark case, $\rho_m = 4.48$ g cm $^{-3}$, $\rho_c = 11.0$ g cm $^{-3}$, $R_c = 3450$ km, by means of a likelihood analysis, in which the likelihood function, $\mathcal{L}'(\rho_m, \rho_c, \xi, \eta) \propto \exp(-\chi(\rho_m, \rho_c, \xi, \eta)^2/2)$, is defined using the following expression for the χ^2 :

$$\chi(\rho_m, \rho_c, \xi, \eta)^2 = \sum_{i=1}^5 \frac{[N_i(\rho_m, \rho_c)(1 + \xi)(1 - \eta \langle \cos \vartheta \rangle_i) - N_i^0]^2}{N_i^0} + \left(\frac{\xi}{\Delta \xi} \right)^2 + \left(\frac{\eta}{\Delta \eta} \right)^2, \quad (1)$$

where ξ takes into account an overall uncertainty of the atmospheric neutrino fluxes and neutrino interaction cross-section ($\Delta \xi = 0.25$), while η encodes the uncertainty between horizontal and vertical events ($\Delta \eta = 0.05$) [8].

We show in Fig. 5 the 68 and 95% C.L. contours of the marginalized function with respect to ξ and η ,

$$\mathcal{L}(\rho_m, \rho_c) = \int \mathcal{L}'(\rho_m, \rho_c, \xi, \eta) d\xi d\eta. \quad (2)$$

By using $\mathcal{L}(\rho_m, \rho_c)$ we can derive the one dimensional likelihoods reported in Figs. 6 and 7 from which one obtains the “measured” values of the densities and the radius of core/mantle boundary at $1\sigma(2\sigma)$:

$$\rho_m = 4.47 \begin{smallmatrix} +0.02 \\ -0.03 \end{smallmatrix} \begin{smallmatrix} (+0.04 \\ -0.06 \end{smallmatrix} \text{ g cm}^{-3} \quad (3)$$

Figure 5. The 68 and 95% C.L. contours of the marginalized likelihood function $\mathcal{L}$ for the measured mantle and core Earth densities, for 10 years of data taking at a NT. The point denoted by M is the sPREM $\equiv (\rho_m = 4.48, \rho_c = 11.0) \text{ g cm}^{-3}$, while $A \equiv (\rho_m = 4.48, \rho_c = 11.5) \text{ g cm}^{-3}$ and $B \equiv (\rho_m = 4.53, \rho_c = 11.0) \text{ g cm}^{-3}$ (see text and Table 2).

Figure 6. One dimensional likelihoods for the Earth densities, ρ_m and ρ_c .

Figure 7. One dimensional likelihood for the radius of core/mantle boundary, R_c .

$$\rho_c = 11.0^{+0.3}_{-0.1} \left({}^{+0.5}_{-0.2} \right) \text{ g cm}^{-3} \quad (4)$$

$$R_c = 3440 \pm 30 \left({}^{+70}_{-50} \right) \text{ km} \quad (5)$$

Our analysis hence suggests that a 2% and 5% uncertainties (at 2σ level) on the averaged mantle and core densities respectively, can be reached in a neutrino radiography campaign with a ten years of data taking at a typical km^3 NT, placed in the **NEMO** site.

In order to understand how different values of ρ_m and ρ_c can affect the angular distribution of events, we report in Table 2 the number of expected ν_μ induced events in 10 years of operation of a NT placed at **NEMO** site in the five bins considered in our analysis for the sPREM, denoted by $M \equiv (\rho_m = 4.48, \rho_c = 11.0) \text{ g cm}^{-3}$, and compare them with the same expectations for two benchmark points *A* and *B* shown in Fig. 5 and chosen at the boundary of the 95% C.L. region. The energy threshold for muons is 1 TeV. This comparison illustrates the level of sensitivity of the angular bins with respect to ρ_m and ρ_c . A variation of the expected number of events per bin which is typically less than 5% is fully compatible with a statistics larger than 10^4 in ten years of running time.

It is worth reminding that these results are obtained in a very simplified PREM model, and this justifies the good level of sensitivity reachable on ρ_m and ρ_c determinations. Notice also that we do not take into account systematics related to the details of the experimental apparatus. Sensitivity to the full PREM detailed features is much weaker, as the number of density layers and corresponding density parameters sensibly grow. Nevertheless, information from NT would represent an independent confirmation of the *coarse grained* mantle-core transition and provide complementary information to geophysical techniques.

$\cos \vartheta$	sPREM (M)	A	B
[0, 0.2]	113436	113860	112876
[0.2, 0.4]	72393	75456	73981
[0.4, 0.6]	47334	48142	47790
[0.6, 0.8]	34105	34144	33503
[0.8, 1.0]	26781	27392	26780

Table 2. Number of expected ν_μ induced events in 10 years of operation of a NT placed at NEMO site in the five bins considered in our analysis for the sPREM, denoted as M $\equiv (\rho_m = 4.48, \rho_c = 11.0)$ g cm $^{-3}$, and for two points labeled by A $\equiv (\rho_m = 4.48, \rho_c = 11.5)$ g cm $^{-3}$ and B $\equiv (\rho_m = 4.53, \rho_c = 11.0)$ g cm $^{-3}$ (see Fig. 5). The energy threshold for muons is 1 TeV.

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