A BIOECONOMIC APPROACH TO OPTIMIZE MUSSEL CULTURE PRODUCTION

Runnig head: Bioeconomic approach for mussel culture

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Abstract

The fast rise of aquaculture practices during the last decades has increased the need of adopting culture strategies to optimize production and guarantee the sustainability of the sector. This study aims to provide a management tool to help mussel farmers identify optimal culture strategies and use production inputs efficiently. For this purpose, we evaluated the productivity and efficiency of different stocking densities and culture lengths by the joint application of parametric and non-parametric frontier analysis at the farm-scale. The translog production function outperformed the Cobb-Douglas model currently applied in most farm-scale frontier analyses. This model estimates that the optimal culture density is ca. 700 ind/m, given that at lower densities efficiency decreases (under-usage of available space) and mussel quality did not improve, and at higher densities mortality and dislodgements from the ropes led to economic losses. This work also showed that marginal analysis does not provide an accurate estimation of the economic efficiency when unitary costs and prizes are not constant. According to the Malmquist indices mussel farmers should shorten the culture period in order to improve their productivity. All these results support the joint use of parametric and non-parametric frontier analysis as management tool for optimizing input use and scheduling aquaculture production.

Keywords

Aquaculture management, culture strategies, Malmquist index, marginal analysis, stochastic frontier function.

1. Introduction

Aquaculture is the fastest growing food sector in the world, with production increasing at an annual rate of 7.8% between 1990 and 2010, and an expected annual growth up to 4.14% from 2014 to 2022 (FAO 2014). Nowadays aquaculture provides 50% of the fishery output for human consumption, of which 23.6% is shellfish culture (14.2 million tons; FAO 2014). With 80% of the total consumed shellfish being cultured, this is an important activity in many coastal zones worldwide. The fast rise of aquaculture practices points out the need of adopting culture strategies in order to optimize production and guarantee the sustainability of the sector. Industry-scale frontier analysis has been widely used to assist producers and decision-makers in identifying optimal production system designs, operation management strategies, and alternative development and policy approaches, although its use in aquaculture is limited when compared with agriculture or other manufacturing industries (Iliyasu et al., 2014). Farm-scale analysis of productivity and environmental impact of shellfish aquaculture has been addressed by Ferreira et al., (2007) and Hawkins et al., (2013), which developed simulation procedures based on the interaction between suspension-feeding bivalves and the environment.

The productivity and efficiency measures introduced by Farrell, (1957) motivated the development of several parametric and nonparametric techniques for frontier analysis. The stochastic frontier production function (SFPF) approach involving econometric estimation of parametric functions (Aigner et al., 1977; Meeusen and Broeck, 1977), and data envelopment analysis (DEA) involving linear programming (Charnes et al., 1978) are the most popular techniques used in frontier analysis. The main advantage of the SFPF is that it can decompose the deviation from the frontier in stochastic noise and technical inefficiency components. The main drawback of this

approach is the need of a functional form for the technology and the inefficiency error term, as the misspecification of the model can lead to biased estimations and wrong conclusions. DEA eliminates the need of a parametric assumption, but due its deterministic nature, this approach attributes all deviations from the frontier to inefficiency effects overlooking the stochastic noise. This drawback was partially overcame by the bootstrap procedure introduced by Simar and Wilson, (2000, 1998) to create confidence intervals for DEA scores. As neither approach is strictly preferable, Murillo-Zamorano and Vega-Cervera, (2001) suggested that the joint use of both techniques can improve the accuracy of frontier analysis. Nevertheless, as in other areas of knowledge, economic efficiency of aquaculture production has been analyzed either by stochastic frontier production functions or DEA (see Iliyasu et al., (2014) and references therein) and to our knowledge the joint use of both techniques is still lacking.

The Farm Aquaculture Resource Management (FARM, Ferreira et al., (2007)) and ShellSIM (Hawkins et al., 2013) are farm-scale models that simulate the interactions between suspension-feeding bivalves and the environment in order to estimate carrying capacity, shellfish production and quantify the ecological impact of aquaculture on the ecosystem. These models can be a useful management tool for both farmers and regulators, as they allow the development of culture strategies in order to optimize economic profits and minimize the environmental impact. Both procedures use marginal analysis based on a Cobb-Douglas SFPF model with stocking biomass as the unique variable input, in order to determine the optimal culture density. The dynamic ecological-economic model proposed by Nobre et al., (2009) also uses a Cobb Douglas model to estimate the marginal productivity of capital and labour. To our knowledge, more general parametric models, such as the translogarithmic SFPF, and nonparametric frontier analysis have not been used at farm-scale level.

The extensive culture of the blue mussel (*Mytilus galloprovincialis*), with a production volume that ranged between 200,000-300,000 tonnes and a production value that exceeded 100 million Euros in 2012 (www.pescadegalicia.com), is the main aquaculture industry in Galicia. Mussels are cultured in floating systems (rafts) consisting of a 500m^2 wood structure anchored to the seafloor, from which culture ropes and/or seed collectors are suspended. Nowadays, the number of ropes per raft is limited to 500. Besides, the maximum number of rafts allowed in the Galician Rias (ca. 3300) has been reached. Mussel culture is scheduled according to the availability of natural resources for feeding and seed recruitment, the biological cycle of mussels and the fluctuations of market demand (Labarta et al., 2004). Subjected to all these constraints, mussel farmers have focused on optimizing the use of available space in the raft to maximize profits, following two strategies: increasing culture densities and/or decreasing the length of the culture cycle.

This study aims to develop a management tool that allows mussel farmers to identify optimal farm-based culture strategies and use production inputs efficiently. To this purpose, we conducted an experiment to evaluate the performance of different culture strategies (testing different cycle lengths and mussel stocking densities) by the joint application of parametric and non-parametric frontier analysis at the farm-scale. We applied parametric frontier analysis to determine the optimal culture density and evaluated whether marginal analysis can be applied to estimate the economic efficiency of suspended mussel culture. We estimated the nonparametric Malmquist indices to analyze the productivity change along the culture period in order to determine the optimal cycle length.

2. Material and Methods

2.1. Experimental design

The study area was located in the raft polygon of Lorbé in Ría de Ares-Betanzos, on the NW coast of Spain (43°22'39.20''N, 8°12'39.77''W). This Ría has great bioeconomical importance due to extensive mussel culture (*Mytilus galloprovincialis)*.

Data were collected during the traditional thinning-out to harvest period, employing the culture and handling techniques used by the local industry (Labarta et al., 2004). In late April 2008, mussels from collector ropes deployed 8 months before (September 2007) were thinned out at seven densities (treatments), encompassing the current commercial densities in Galicia (600–800 ind/m). The mean shell length of these mussels was 48.78mm (sd=1.27), which is close to the minimum commercial size (50mm). Stocking biomass (Kg/rope) was measured as rope weight at the beginning of the culture (in this case at thinning-out). Production costs (€/rope) were obtained from a survey of several mussel aquaculture farms, and included labour, estimated as time spent per rope for thinning-out and harvesting, boat fuel consumption for deploying and harvesting the ropes, and raft occupation costs (Table 1, Appendix I). As mussels were obtained from collector ropes, their cost (€/Kg) was estimated as the occupation cost of these collector ropes in the raft.

Production data were collected monthly from late May to late November (see details in (Cubillo et al., 2012c) so that the length of growing season or cycle length (days) can be considered as an input. Density was calculated as the number of mussels per linear meter of rope (ind/m). Total production (Kg/rope) was estimated as the weight of commercial (>50 mm shell length) mussels. Production prices (€/Kg) and revenues (€/rope) were estimated taking into account the two markets: fresh sale

(mussels sold as fresh product) and industry sale (frozen, canned and processed mussels). Fresh sale prices are based on mussel size, measured as number of mussels per Kg (ind/Kg), according to the average classification used by several distribution companies (Pérez-Camacho et al., 2013): Extra1 (< 21 ind/Kg, 1€/Kg), Extra2 (21-27 ind/Kg, 0.9 €/Kg), Large (28-35 ind/Kg, 0.75 €/Kg), Normal (36-45 ind/Kg, 0.6€/Kg) and Small (46-70 ind/Kg, 0.5 €/Kg). Industry sale prices build on mussel quality in terms of mussel size (ten categories ranging from > 276 to < 98 ind/Kg tissue), and Condition Index measured as the meat to total weight ratio of mussels (from 12% to 27%), according to a pool of processing industries, so that small mussel (>276 ind/Kg tissue) prices ranged between 0.22 and 0.50 €/Kg and large mussel (< 98 ind/Kg tissue) prices between 0.35 and 0.78 €/Kg.

2.2. Data analysis.

We first conducted an exploratory analysis of the variables involved in the mussel culture process. We applied two-way repeated measures ANOVA to test the effects of density treatment and cycle length on production and product quality. In addition, we applied generalized additive models (GAM) to estimate the effect of stocking biomass and cycle length on the profits obtained by fresh and industry sale, and to analyze the differences between both. Section 2.2.1 provides detailed information about the GAM model. Model fitting was conducted with the mgcv package of R (R Core Team, 2013; Wood, 2006a)

The analysis of productivity and efficiency was conducted by the joint use of parametric (SFF) and non-parametric techniques (DEA). We applied Stochastic frontier analysis, considering stocking biomass (Kg/rope) and cycle length (days) as inputs, and total production (Kg/rope) as output to determine which density is closer to the

production carrying capacity of the system without exceeding it, i.e. the optimal density treatment. In addition, we estimated the non-parametric Malmquist indices for productivity, efficiency and technology change, considering stocking biomass (Kg/rope) and culture costs (€/rope) as inputs and total production (Kg/rope) or profits (€/rope), as outputs. This analysis allows us to determine the optimal cycle length for each market and the most profitable market for each cycle length. The parametric and non-parametric frontier analysis were conducted with the frontier (Coelli and Henningsen, 2011) and FEAR (Wilson, 2008) packages of R. Sections 2.2.2 and 2.2.3 provide information about these procedures.

2.2.1. Generalized additive models (GAM)

For both fresh and industry sale, we fitted the profits (P, €/rope) obtained as the difference between costs and revenues, according to cycle length (T, days) and stocking biomass (S, Kg/rope) by generalized additive models (GAM) with second order interaction (Hastie and Tibshirani, 1990; Wood, 2006b). As the response variables are normal, we assumed a Gaussian family with identity link function (Hastie and Tibshirani, 1990; Wood, 2006a). Our model can be expressed as follows:

$$E(P) = \alpha + f_1(S) + f_2(T) + f_{12}(S,T) \quad (1)$$

where, for each transaction, E(P) are the estimated profits, α is the intercept, f_j, j=1,2 the smooth terms for each covariate, which were represented by penalized regression splines, and f_{12} the smooth term for the interaction between stocking biomass and cycle length, estimated using a scale-invariant tensor product of penalized regression splines (Wood, 2006b). Finally, we obtained 95% confidence intervals for the predicted values in order to compare profits between fresh and industry sale.

2.2.2. Stochastic frontier production function (SFPF) with a model for technical inefficiency effects and marginal analysis

We applied one-step stochastic frontier analysis (see details in Appendix II) to estimate the potential production and efficiency levels of the different density treatments. Model selection was conducted by several likelihood ratio tests (Table 2). Our data rejected the Cobb-Douglas model for the stochastic frontier function (Appendix II). Total efficiency, deterministic efficiency and independence between inefficiency and density treatment were also rejected. Thus, we fitted the SFPF for total production (B, Kg/rope) by a translogarithmic model with stocking biomass (S, Kg/rope) and cycle length (T, days) as inputs and density treatment as inefficiency factor (Z) (Battese and Broca, 1997; Battese and Coelli, 1995). This model can be expressed as follows:

$$\begin{aligned}\ln B_{it} &= \beta_0 + \beta_1 \ln S_{it} + \beta_2 \ln T_{it} \\ &+ \frac{1}{2}\left(\beta_{11}\left(\ln S_{it}\right)^2 + 2\beta_{12} \ln S_{it} \ln T_{it} + \beta_{22}\left(\ln T_{it}\right)^2\right) + V_{it} - U_{it}\end{aligned} \tag{2}$$

where U_{it} is the estimator of the technical inefficiency, $TE_{it}=exp(-U_{it})$, and can be expressed as $U_{it} = z_{it}\delta + W_{it}$, where, z_{it} is the vector of dummy variables associated to each density treatment, δ is the associated vector of parameters and W_{it} are random error terms ($N(0,\sigma_w^2)$). Positive coefficients (δ > 0) indicate relative technical inefficiency while negative coefficients (δ < 0) point out relative technical efficiency. The more the estimated value differs from zero, the stronger the efficiency/inefficiency.

In order to measure the effect of any input change on total production we estimated the output elasticity for each input (Appendix II). The sum of these parameters yields the return to scale (RTS), which measures the percentage change in

output from a 1% change in all inputs. When RTS > 1 (RTS < 1) the production function exhibits increasing (decreasing) returns to scale, i.e. a simultaneous increase in all inputs by a certain percentage results in greater (lower) percentage increase in output. If RTS = 1, the farm has constant returns to scale, implying that a proportionate increase in inputs will lead to the same increase in output. The cross-elasticity of substitution H_{jk}, (Chiang et al., 2004) was estimated to measure the relationship between inputs (Appendix II). $H_{12} > 0$ indicates that the inputs are jointly complementary, i.e. we need to increase stocking biomass and cycle length together to raise total production. $H_{12} < 0$ indicates a competitive relationship between inputs, i.e. a decrease in stocking biomass could be compensated elongating the culture period, and viceversa.

Finally, we analyzed the economic efficiency of the stocking biomass (S) by comparison between the incremental benefit of an additional unit (VMP) and its incremental cost (P_x). If the value of the marginal product (VMP) of an input is greater than its cost (P_x), profit could be raised increasing the use of that input, and conversely. The efficient use of an input is achieved when the value of its marginal product equals its price. Marginal analysis is usually built under some regularity conditions: (i) inputs are unlimited, (ii) inputs purchase and output sales are made in a perfect competitive market situation, (iii) the farm is a small production system that sells only this product and (iv) mussel seed is the unique variable input, as other cost (such that lease or labour) are fixed (Ferreira et al., 2007). These conditions are not necessarily true in mussel suspended culture. On one hand, on contrast with assumption (iv) the relative raft occupation, labour and transport costs decrease as the stocking biomass increases (see Fig. A1 in Appendix I). On the other hand, as explained in Section 2.1 mussel prices depend on mussel size and quality. In this work, we conduct the marginal analysis for each cycle length taking into account the variability of costs and prices

along the density gradient. Thus, for each density treatment and cycle length, we estimate the ratio VMP/Px and check whether these values equal 1 to indentify optimal input use.

2.2.3. Malmquist productivity indices

Productivity change between sequential months for each density treatment was analyzed through the input-based Malmquist productivity, efficiency and technology indices. We obtained these indices following the estimation and bootstrap methods proposed by Simar and Wilson (1999) under the assumption of constant returns to scale. Productivity was measured in terms of total production (Kg/rope) and revenue (€/rope) for both fresh and industry sale. As we are interested in productivity change over time, we cannot consider cycle length as input, as we did above. Thus, our inputs are stocking biomass (Kg/rope), which depend on the density treatment but remains constant over time, and culture costs (defined as the sum of labour, transport and occupation, Appendix I), which depend on both density treatment and cycle length.

Given a set of density treatments ($i= 1, 2, ..., 7$) observed at times $t_1 < t_2$, the input-based Malmquist index for treatment i (Färe et al., 1992; Simar and Wilson, 1999) is defined as:

$$M_i\left(t_1,t_2\right)=\frac{D_i^{t_2/t_2}}{D_i^{t_1/t_1}}\left(\frac{D_i^{t_2/t_1}}{D_i^{t_2/t_2}}\frac{D_i^{t_1/t_1}}{D_i^{t_1/t_2}}\right)^{1/2}=\varepsilon_i\left(t_1,t_2\right)F_i\left(t_1,t_2\right), \qquad (3)$$

where $D_i^{t_j/t_k}$ is the Shephard input distance function for treatment i at time t_j relative to the technology at time t_k (Shephard, 1970). Values of $M_i\left(t_1,t_2\right)<1$ indicate

improvements in productivity, while values $M_i(t_1,t_2)>1$ indicate productivity regress from t_1 to t_2. When the estimated Malmquist index is 1, there is no productivity change.

The Malmquist productivity index can be decomposed into an index of input-based efficiency, the ratio outside the bracket in (3), and an index of input-based technology change, the geometric mean of the two ratios inside the bracket in (3), which measure the shift in the production frontier. As with $M_i(t_1,t_2)$, values of $\varepsilon_i(t_1,t_2)$ and $T_i(t_1,t_2)$ lower (greater) than unity reflect efficiency/technology progress (regress) between times t_1 and t_2.

3 Results

3.1 Exploratory analysis

Fig. 1a-1d shows an exploratory analysis of the population dynamics along the experiment. We observe a significant effect of cycle length, density treatment and their interaction (2-way repeated measures ANOVA, $p<0.001$) on density (ind/m), total production (Kg/rope) and mussel size (ind/Kg), while meat yield (Condition index), which is mainly determined by the reproductive cycle of mussels, depended only on cycle length, reaching its maximum values from June to September.

Total production (Fig 1b, Kg/rope) increased up to August for the higher density treatments (570-1150 ind/m) and up to September for the lower (220-500 ind/m). Despite the negative effects of overcrowding on mussel survivorship (Fig. 1a) and growth (Fig. 1c) total production increased along the density gradient. In June, commercial mussels (L > 50mm) accounted for 90% total rope weight, and from August onwards the percentage was over the 99%. For all density treatments, mussels reached the Medium commercial category (66mm and 37 ind/Kg) in August and the Large

category (70mm and 33 ind/Kg) in September. Only two density treatments, 220 ind/m and 700 ind/m reached the Extra2 category (73mm and 29ind/Kg) in November. Therefore, fresh sale prices (€/Kg) increased up to September (Fig 1e) and remained constant thereafter (Fig 1e). Industry-sale prices (€/Kg), as expected given their dependence on the condition index, were only affected by cycle length and reached maximum values between June and September (Fig 1f). Due to the small differences found in the size and quality of mussels among density treatments, the revenues per Kg were similar (Fig. 1e and 1f), while the revenues per rope increased along the density gradient for both fresh and industry sale (Fig. 2).

Figs. 2 and 3 show the estimated profits for fresh (Adjusted R2 = 0.801) and industry sale (Adjusted R2 = 0.77). For all density treatments, fresh sale profits increased over time, although this increase ameliorated from September onwards. Industry sale profits increased up to August and decreased thereafter. The higher densities (> 500 ind/m) amortized culture costs in June (L ≈57 mm) by industry sale and in July (L ≈61 mm) by fresh sale, while the lower densities needed an extra month to be profitable. Smaller mussels (up to August) provided higher profits through industry sale due to the increase in meat yield during summer, while larger mussels (>70 mm) are more suitable for fresh sale. In August, industry sale overcame at least a 15% fresh sale profits, whereas in September fresh sale overcame at least a 26% industry sale profits.

3.2 Stochastic frontier function and marginal analysis

Table 3 shows the parameters estimated by the translog SFPF model for total production introduced in section 2.2.2. Both output elasticities are positive and close to 0.5, implying that a 1% increase in any input would increase production by ≈0.5%, though the elasticity for cycle length (0.50) is significantly higher than the elasticity for

stocking biomass (0.47) (t-test, p =0.042). We obtained constant returns to scale (RTS = 0.973 = 1; t-test, p-value > 0.05), so that a given simultaneous increase in culture days and stocking biomass will give the same percentage increase in production. The Hicks substitution elasticity for stocking biomass and cycle length (H_{12} = 0.905 > 0) indicates a complementary relationship between inputs, i.e. they need to be increased together to raise total production. Finally, our results show that only 1.14% of the deviation from the stochastic frontier can be attributed to technical inefficiency.

The lower half of Table 3 shows the estimated inefficiency effects of each culture density and the respective technical efficiencies (TE). Relative inefficiency ($\delta > 0$) was statistically significant for mussels cultured at 220-570 and 800 ind/m, while relative efficiency ($\delta < 0$) was found for 1150 ind/m. Despite density-dependent mussel losses, technical efficiency increased with stocking biomass, being 700 ind/m and 1150 ind/m (which achieved total efficiency) the most efficient densities, whereas the lowest density operated 51.6% below the production frontier.

The results of the economic efficiency analysis for stocking biomass are shown in Fig. 4. Marginal costs (Px) increased linearly along the culture period and decreased along the density gradient. For fresh sale, marginal benefits (VMP) increased over time (Tukey HSD, p-value < 0.001) and decreased over the density gradient, 1150 reported the lower economic efficiency and 700-800ind/m were less efficient than 220-500ind/m (Tukey HSD, p-values < 0.001). For industry sale, the VMP stabilized in August (Tukey HSD, p-value > 0.1) and the densities of 700, and 1150 ind/m reported lower economic efficiency than 220-570 ind/m (Tukey HSD, p-value < 0.01). For both fresh an industry sale, the ratio between VMP and the marginal costs (Fig 4, bottom) shows the same temporal pattern as the VMP and remained constant along the density gradient (Tukey HSD, p-value > 0.05). As all ratios are below 1, optimal input use was not

reached for any market. Comparison between markets reported higher relative efficiency for fresh sale than for industry sale from September onwards for all density treatments.

3.3 Malmquist productivity indices

Consistent with Färe et al. (1992) we report the reciprocals of the original non-parametric indices (Tables 4-6 and Fig. 5), so that numbers greater than unity denote progress while numbers lower than unity denote regress. As expected given the low proportion of deviation from the production frontier attributed to technical inefficiency (1.14%), its effect on Malmquist productivity indices was very low, and changes in productivity over time were mainly explained by shifts in the production frontier.

The estimated indices for efficiency change (Table 4-6, Fig 5 centre) did not show a clear pattern along culture, except for the highest density (1150 ind/m) that reported constant efficiency over time.

Total production and fresh sale revenues reported technology progress up to September. The production frontier stagnated thereafter for the two lower densities, while the higher densities suffered a regress during October followed by a new increase during the last month. For industry sale prices technology progress ceased in August (Table 4-6, Fig 5 right).

Finally, the Malmquist indices reported productivity improvements up to September in all density treatments for total production and fresh sale revenues, while for industry sale some density treatments suffered productivity regress in September (Table 4-6, Fig 5 left). The productivity losses observed in October for the higher

densities (≥500 ind/m) and November for the lower (≤570) were caused by reductions in potential production and efficiency, respectively.

4. Discussion and conclusions

This work provides a productivity analysis for suspended mussel aquaculture at the farm-scale, based on monitoring of mussel growth and survivorship. Prior studies have focused on industry-scale analysis (see Iliyasu et al., (2014) and references therein) or have conducted farm-scale productivity analysis based on simulation models for mussel growth (Ferreira et al., 2007; Hawkins et al., 2013). Most research works on the production frontier in aquaculture have focused on efficiency measurement using either Stochastic Production Frontier (SPF) or Data Envelopment Analysis (DEA). This work incorporates empirical data to productivity analysis and evaluates the performance of different culture strategies (defined as mussel density and cycle length) through the joint application of parametric (SFPF) and non-parametric frontier analysis (Malmquist indices).

This study shows that both parametric (SFPF) and non-parametric (Malmquist indices) approaches reflect the effect of mussel population dynamics (intraspecific competition, mussel growth and mortality) on production. Population dynamics were previously described on the same data set by Cubillo et al., (2012b) and Fuentes-Santos et al., (2013). The former found a negative effect of stocking rate on mussel growth rates, and the later found significant mussel losses at higher density (>500 ind/m), being 1150ind/m the treatment with the highest mortality. Both studies concluded stronger competition effects at higher densities.

The current farm-scale productivity analyses use the Cobb-Douglas model (Ferreira et al., 2007; Hawkins et al., 2013; Nobre et al., 2009) to estimate the stochastic frontier function. However, when the effects of the inputs on production are not independent, we need more general models. Following the methodology applied at industry-scale level (Battese and Broca, 1997; Chiang et al., 2004; Iliyasu et al., 2014) we fitted a translog stochastic frontier function with density treatment as efficiency factor, which improved the understanding of multiple dependency and interaction between production inputs (stocking biomass and cycle length) and estimates the effect of the density treatment on technical efficiency. The likelihood ratio tests confirmed that the translog model is more accurate than the Cobb Douglas frontier function.

Most of the industry-scale studies in aquaculture have focused on technical efficiency and total production (Iliyasu et al., 2014). However, maximizing biological production does not lead to maximize profits, and management tools should rely on economic instead of technical efficiency. Following Ferreira et al., (2007), which stated that the profit maximization rule is based on marginal principles; we applied marginal analysis to determine the optimal stocking biomass. However, we should note that suspended mussel culture violates the principle of constant production costs (occupation, labour and transport), as these values depend on the density treatment. To estimate the marginal cost of the stocking biomass (Kg/m) we need to decompose each production cost into a constant part and a part that varies with the density treatment, and sum the latter to the cost of mussels (or mussel seed). However, in practice we cannot determine which proportion of each production cost depends on the density treatment. If we just consider the cost of mussel seed to estimate P_X we shall underestimate the marginal cost and obtain wrong conclusions in the comparison between density treatments. Estimating P_X as the sum of mussels, labour and occupation costs provides a

proper comparison between density treatments, but overestimates the marginal cost. Therefore we cannot rely on the comparison between VMP and P_X to determine the optimal input use in either case. Taking into account these drawbacks and that comparison between markets did not provide further information than that provided by the GAM models, we do not recommend the use of marginal analysis in suspended mussel aquaculture.

The use of the Malmquist productivity indices to measure productive growth at the industry-scale in aquaculture has gained popularity in recent years (Iliyasu et al., 2014). These works focus on optimizing total production, but did not considered economic capacity. Given that culture strategies should focus on maximizing profits instead on maximizing total production, we proposed to estimate the Malmquist productivity indices considering revenues as output. We point out that the variability in output prices regarding the quality of the product and the market (fresh or industry sale) should be taken into account in the economic analysis. These indices measured the change in economic capacity and efficiency along culture and allowed us to determine the optimal cycle length.

The parametric stochastic frontier analysis determined that 700 ind/m is the optimal culture density. The relative inefficiency observed at lower densities, which did not suffered mortality due to intraspecific competition but did not provide better mussel quality than higher densities, indicates an underuse of the available resources. The relative efficiency of 1150 ind/m, which suffered the strongest competition effects on mussel growth and survivorship (Cubillo et al., 2012a; Fuentes-Santos et al., 2013), indicates that this density exceeded the carrying capacity of the rope. Apart from the economic losses, mussel mortality also implies the increase of biodeposits beneath culture leases that alter the physical and chemical conditions of the bottom sediments,

and thus affect the natural biodiversity. As in (Ferreira et al., 2007; Hawkins et al., 2013) models, the environmental effects of mussel culture should be taken into consideration to develop decision making tools that guarantee the sustainability of suspended mussel culture.

The Malmquist productivity, efficiency and technology indices allowed us to determine the optimal cycle length. The risk of productivity regress from October onwards suggests that it is not worth extending the culture beyond September, i.e. when individuals reach lengths of ≈70 mm. In addition, the economic analysis points out that farmers would maximize profits in August (L = 66 mm) by industry sale and September (L = 70 mm) by fresh sale, due to the differences in the type of product that these two markets demand. These results together with the recent shift to smaller sizes (L ≤ 75mm) in mussel market, highlights the suitability of shortening the current cycle length.

Thus, this work provides a suitable management tool for optimizing input use in aquaculture practices and scheduling production according to market demand. Our results indicate that the current stocking densities in Galician mussel aquaculture (600-800ind/m) are close to the optimum culture density (700ind/m) and their technical efficiency is above 85%. However, according to the Malmquist indices mussel farmers should shorten the thinning-out to harvest period in order to improve their productivity. In addition to optimizing profits, this reduction of cycle length results in a more efficient use of the available space.

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References

Aigner, D., Lovell, C.A.K., Schmidt, P., 1977. Formulation and estimation of stochastic frontier production function models. J. Econom. 6, 21–37. doi:10.1016/0304-4076(77)90052-5

Battese, G.E., Broca, S.S., 1997. Functional Forms of Stochastic Frontier Production Functions and Models for Technical Inefficiency Effects: A Comparative Study for Wheat Farmers in Pakistan. J. Product. Anal. 8, 395–414. doi:10.1023/A:1007736025686

Battese, G.E., Coelli, T.J., 1993. A stochastic frontier production function incorporating a model for technical inefficiency effects. Department of Econometrics, University of New England Armidale.

Battese, G.E., Coelli, T.J., 1995. A model for technical inefficiency effects in a stochastic frontier production function for panel data. Empir. Econ. 20, 325–332. doi:10.1007/BF01205442

Charnes, A., Cooper, W.W., Rhodes, E., 1978. Measuring the efficiency of decision making units. Eur. J. Oper. Res. 2, 429–444. doi:10.1016/0377-2217(78)90138-8

Chiang, F.-S., Sun, C.-H., Yu, J.-M., 2004. Technical efficiency analysis of milkfish (Chanos chanos) production in Taiwan—an application of the stochastic frontier production function. Aquaculture 230, 99–116. doi:10.1016/j.aquaculture.2003.09.038

Coelli, T., Henningsen, A., 2011. frontier: Stochastic Frontier Analysis R package version 0.887.

Cubillo, A.M., Fuentes-Santos, I., Peteiro, L.G., Fernández-Reiriz, M.J., Labarta, U., 2012a. Evaluation of self-thinning models and estimation methods in multilayered sessile animal populations. Ecosphere 3, art71. doi:10.1890/ES12-00180.1

Cubillo, A.M., Peteiro, Laura G., Fernández-Reiriz, MJ, Labarta, Uxío, 2012b. Influence of stocking density on biomass production and survival of mussels (Mytilus galloprovincialis) grown in suspended culture., in: Physiomar 12: Proceedings of the 4th Physiomar International Meeting, Santiago de Compostela, Spain, 4th-8th September, 2012. p. 149.

Cubillo, A.M., Peteiro, L.G., Fernández-Reiriz, M.J., Labarta, U., 2012c. Influence of stocking density on growth of mussels (Mytilus galloprovincialis) in suspended culture. Aquaculture 342–343, 103–111. doi:10.1016/j.aquaculture.2012.02.017

Färe, R., Grosskopf, S., Lindgren, B., Roos, P., 1992. Productivity changes in Swedish pharamacies 1980–1989: A non-parametric Malmquist approach. J. Product. Anal. 3, 85–101. doi:10.1007/BF00158770

Farrell, M.J., 1957. The Measurement of Productive Efficiency. J. R. Stat. Soc. Ser. Gen. 120, 253–290. doi:10.2307/2343100

Ferguson, C.E., 2008. The Neoclassical Theory of Production and Distribution (Cambridge Books). Cambridge University Press.

Ferreira, J.G., Hawkins, A.J.S., Bricker, S.B., 2007. Management of productivity, environmental effects and profitability of shellfish aquaculture — the Farm Aquaculture Resource Management (FARM) model. Aquaculture 264, 160–174. doi:10.1016/j.aquaculture.2006.12.017

Fuentes-Santos, I., Cubillo, A.M., Fernández-Reiriz, M.J., Labarta, U., 2013. Dynamic self-thinning model for sessile animal populations with multilayered distribution. Rev. Aquac. n/a–n/a. doi:10.1111/raq.12032

Hastie, T.J., Tibshirani, R.J., 1990. Generalized Additive Models. Chapman and Hall/CRC.

Hawkins, A.J.S., Pascoe, P.L., Parry, H., Brinsley, M., Black, K.D., McGonigle, C., Moore, H., Newell, C.R., O'Boyle, N., Ocarroll, T., O'Loan, B., Service, M., Smaal, A.C., Zhang, X.L., Zhu, M.Y., 2013. Shellsim: A Generic Model of Growth and Environmental Effects Validated Across Contrasting Habitats in Bivalve Shellfish. J. Shellfish Res. 32, 237–253. doi:10.2983/035.032.0201

Iliyasu, A., Mohamed, Z.A., Ismail, M.M., Abdullah, A.M., Kamarudin, S.M., Mazuki, H., 2014. A review of production frontier research in aquaculture (2001–2011). Aquac. Econ. Manag. 18, 221–247. doi:10.1080/13657305.2014.926464

Labarta, U., Fernández-Reiriz, Pérez-Camacho, Alejandro, Pérez-Corbacho, E., 2004. Bateeiros, mar, mejillón. Una perspectiva bioeconómica., Serie Estudios Sectoriales. Fundación Caixa Galicia., A Coruña, Spain.

Meeusen, W., Broeck, J. van D., 1977. Efficiency Estimation from Cobb-Douglas Production Functions with Composed Error. Int. Econ. Rev. 18, 435–444. doi:10.2307/2525757

Murillo-Zamorano, L.R., Vega-Cervera, J.A., 2001. The use of parametric and non-parametric frontier methods to measure the productive efficiency in the industrial sector: A comparative study. Int. J. Prod. Econ. 69, 265–275. doi:10.1016/S0925-5273(00)00027-X

Nobre, A.M., Musango, J.K., de Wit, M.P., Ferreira, J.G., 2009. A dynamic ecological–economic modeling approach for aquaculture management. Ecol. Econ. 68, 3007–3017. doi:10.1016/j.ecolecon.2009.06.019

Pérez-Camacho, A., Labarta, U., Vinseiro, V., Fernández-Reiriz, M.J., 2013. Mussel production management: Raft culture without thinning-out. Aquaculture 406–407, 172–179. doi:10.1016/j.aquaculture.2013.05.019

R Core Team, 2013. R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Viena-, Austria.

Shephard, R.W., 1970. Theory of Cost and Production Functions. University Press.

Simar, L., Wilson, P.W., 1998. Sensitivity Analysis of Efficiency Scores: How to Bootstrap in Nonparametric Frontier Models. Manag. Sci. 44, 49–61. doi:10.1287/mnsc.44.1.49

Simar, L., Wilson, P.W., 1999. Estimating and bootstrapping Malmquist indices. Eur. J. Oper. Res. 115, 459–471. doi:10.1016/S0377-2217(97)00450-5

Simar, L., Wilson, P.W., 2000. Statistical Inference in Nonparametric Frontier Models: The State of the Art. J. Product. Anal. 13, 49–78. doi:10.1023/A:1007864806704

Troell, M., Naylor, R.L., Metian, M., Beveridge, M., Tyedmers, P.H., Folke, C., Arrow, K.J., Barrett, S., Crépin, A.-S., Ehrlich, P.R., Gren, A., Kautsky, N., Levin, S.A., Nyborg, K., Osterblom, H., Polasky, S., Scheffer, M., Walker, B.H., Xepapadeas, T., de Zeeuw, A., 2014. Does aquaculture add resilience to the global food system? Proc. Natl. Acad. Sci. U. S. A. 111, 13257–13263. doi:10.1073/pnas.1404067111

Wilson, P.W., 2008. FEAR: A software package for frontier efficiency analysis with R. Socioecon. Plann. Sci. 42, 247–254.

Wood, S., 2006a. Generalized Additive Models: An Introduction with R. CRC Press.

Wood, S., 2006b. Low-rank scale-invariant tensor product smooths for generalized additive mixed models. Biometrics 62, 1025–1036. doi:10.1111/j.1541-0420.2006.00574.x

APPENDIX I

Culture costs

Figure A1 shows total (€/rope) and marginal costs (€/Kg) for each density treatment along the culture period. Total and occupation costs increase linearly over time, while labour and transport can be considered constant over time. Total, labour and transport costs increased with stocking density, while occupation costs remain constant along the density gradient. However, marginal costs decreased with stocking density.

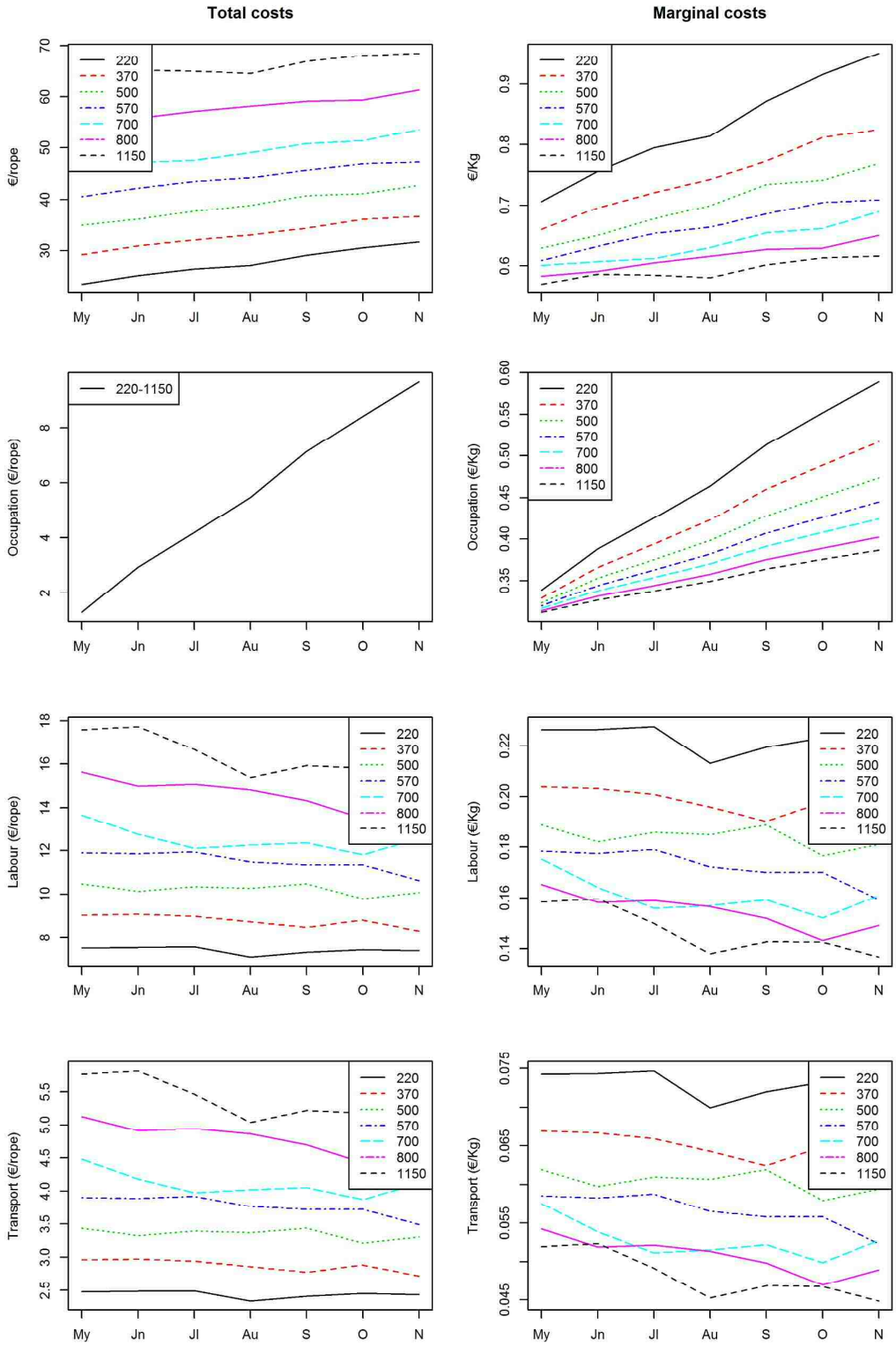


Fig A 1: Total (€/rope) and marginal (€/Kg) production costs by months and density treatment.

APPENDIX II

Parametric approach: Stochastic frontier production function (SFPF) with a model for technical inefficiency effects

In order to estimate the potential production and efficiency levels of the different density treatments we applied one-step stochastic frontier analysis assuming a translog frontier function with a model for inefficiency, which is assumed to depend on the density treatments (Battese and Broca, 1997; Battese and Coelli, 1995) Our model can be expressed as follows

$$Y_{it} = \exp(f(X_{it}) + v_{it} - u_{it}) \quad (4)$$

where Y_{it} is the output expressed as harvest production (*Kg/rope*) for the i-th density treatment at time *t*, X_{it}: is the vector of inputs, in our case stocking biomass (X_1) and cycle length (X_2), V_{it} is the stochastic error term and U_{it} is the estimate of the technical inefficiency $TE_{it}=exp(-U_{it})$. The stochastic error term are assumed to be independent and identically distributed $N(0,\sigma_v^2)$ and independent of U_{ti}. The distribution of the inefficiency error term is a truncation (at zero) of the normal distribution with mean $\mu = z_{it}\delta$ and variance σ_u^2, i.e $U_{it} = z_{it}\delta + W_{it}$, where, z_{it} is the vector of variables that may affect technical inefficiency, δ is the associated vector of parameters and W_{it} are random error terms ($N(0,\sigma_w^2)$). Positive coefficients ($\delta > 0$) indicate relative technical inefficiency while negative coefficients ($\delta < 0$) point out relative technical efficiency. The more the estimated value differs from zero, the stronger the efficiency/inefficiency. In this study, initial density was introduced as dummy variable to account for differences in efficiency across the density gradient.

The most common parametric model for the stochastic frontier function, $f\left(X_{it}\right)$, is the translog production frontier function:

$$\begin{aligned}\ln Y_{it} &= \beta_0 + \beta_1 \ln X_{1it} + \beta_2 \ln X_{2it} \\ &+ \frac{1}{2}\left(\beta_{11}\left(\ln X_{1it}\right)^2 + 2\beta_{12} \ln X_{1it} \ln X_{2it} + \beta_{22}\left(\ln X_{2it}\right)^2\right) + v_{it} - u_{it}\end{aligned} \tag{5}$$

where the interaction between stocking biomass and cycle length implies non-neutral technical change. If all $\beta_{jk} = 0$, then the previous model reduces to a Cobb–Douglas (C–D) SFPF model:

The parameters of the stochastic frontier and the model for the technical inefficiency effects were simultaneously estimated by maximum likelihood. The likelihood function is expressed in terms of the variance parameters $\sigma^2=\sigma_v^2+\sigma_u^2$ and $\gamma=\sigma_u/\sigma$, which measures the proportion of deviation from the frontier due to technical inefficiency (Battese and Coelli, 1993). Model selection for the frontier function and the inefficiency effects were performed by one-side generalized likelihood-ratio tests (LR):

$$LR = -2\left\{\ln\left\{L\left(H_0\right)/L\left(H_1\right)\right\}\right\} = -2\left\{\ln\left[L\left(H_0\right)\right] - \ln\left[L\left(H_1\right)\right]\right\} \sim \chi^2 \tag{6}$$

Where $L(H_0)$ and $L(H_1)$ are the likelihood functions under the null and alternative hypotheses, respectively. The stochastic frontier model selection was conducted testing the null hypothesis: H_0: $\beta_{jk} = 0$, i.e. testing whether the translog SFPF (eq. 3) can be reduced to a Cobb-Douglas SFPF. The inefficiency model selection was conducted by the following multistage hypothesis test:

1. H_0: $\gamma = \delta_0 = \delta_1 = \ldots = \delta_7 = 0$, which implies total efficiency, i.e. the model can be reduced to the traditional mean response function, without the inefficiency error term u_i.

2. H_0: $\gamma = 0$, which implies that the inefficiencies are not stochastic.
3. H_0: $\delta_1 = \ldots = \delta_7 = 0$, which implies that the inefficiency effects are independent of the density treatment.

The output elasticity for each input factor, X_j *(j=1, 2)*, defined as the percentage change of the i-th output at time *t* for a 1% change in the j-th input, is given by:

$$EX_{jit} = \frac{\partial \ln(Y_{it})}{\partial \ln(X_{jit})} = \frac{\partial Y_{it}}{\partial X_{jit}} \frac{X_{jit}}{Y_{it}} = \beta_j + \sum_{k=1}^{m} \beta_{jk} \ln(X_{kit}) \quad (7)$$

Since for the translog SFPF, EX_{jit} is different for each treatment and time, we use the sample mean of each input factor across all treatments and times, EX_j to represent EX_{jit}. The sum of these parameters is the return to scale (RTS), which measures the percentage change in output from a 1% change in all input factors. When RTS > 1 (RTS < 1) the production function exhibits increasing (decreasing) returns to scale, i.e. a simultaneous increase in all inputs by a certain percentage results in greater (lower) percentage increase in output. If RTS = 1, the farm present constant returns to scale, implying that a proportionate increase in inputs will lead to the same increase in output.

The cross-elasticity of substitution (Chiang et al., 2004) for factors *j* and *k* under the translog SFPF (eq. 3) model is defined as:

$$H_{jk} = \frac{\beta_{jk}}{EX_j + EX_k} - 1 \quad (8)$$

$H_{12} > 0$ indicates that the inputs are jointly complementary, i.e. we need to increase stocking biomass and cycle length together to raise total production. $H_{jk} < 0$ indicates a

competitive relationship between inputs, i.e. a decrease in stocking biomass could be compensated elongating the culture period.

The economic efficiency of an input can be analyzed by comparison between the incremental benefit of an additional unit and its incremental cost. Assuming constant unit input cost, P_x, and output price, P_y, the value of marginal product (VMP) is defined as:

$$VMP_{it} = MPP_{it} \cdot P_y \tag{9}$$

where MPP is the marginal physical product, which according to Ferguson, (2008) is equal to the elasticity of scale. If the value of the marginal product (VMP) of an input is greater than its price (P_x), profit could be increased by increasing the use of that input, and conversely. To achieve efficient use of an input, the value of its marginal product should be equal to its price.

Table 1: Summary of production costs included in the efficiency models**.**

€/rope	Min (220 ind/m)	Mean (sd)	Max (1150 ind/m)
Mussel	10.5	23.43 (8.77)	39.9
Labour	6.7	11.62 (3.02)	18.67
Transport	2.2	3.81 (0.99)	6.13
Occupation		1.38 €/month	

Table 2: Hypothesis test for stochastic production function and inefficiency models.

H_O	loglik H_0	loglik H_1	df	LR	p-value	
CD vs translog	93.374	106.316	3	25.883	1.01E-05	***
$\gamma = \delta_1 = \ldots = \delta_7 = 0$	76.699	106.316	8	59.235	2.88E-10	***
$\gamma = 0$	76.699	83.901	3	14.406	0.001	**
$\delta_1 = \ldots = \delta_7 = 0$	76.718	106.316	6	59.196	6.55E-11	***

(***) p-value < 0.001, (**) p-value < 0.01, (*) p-value < 0.05.

Table 3: Model parameters, output elasticities and technical efficiencies for the translog SFPF.

	Parameter	p-value		
Elacticies				
Stocking rate	0.473	<2.2e-16	***	
Days	0.500	<2.2e-16	***	
RTS	0.973	0.057		
σ^2	0.0198	<2.2e-16	***	
γ	0.0114	<2.2e-16	***	
Inefficiency factors (δ)				**TE**
220	0.725	7.67E-10	***	0.484
370	0.347	0.0002	***	0.707
500	0.164	0.0429	*	0.850
570	0.163	0.0187	*	0.850
700	0.084	0.1502		0.921
800	0.132	0.0026	**	0.877
1150	-1.025	1.68E-06	***	1.000

(***) p-value < 0.001, (**) p-value < 0.01, (*) p-value < 0.05.

Table 4: Changes in productivity, efficiency and technology for total production. Number greater (lower) than 1 indicate progress (regress).

Total production (kg/rope)												
Malmquist indices												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	1.788	**	1.294	**	0.986	**	1.253	**	1.219	**	0.989	**
370	1.555	**	1.323	**	1.141	**	1.216	**	1.113	**	0.911	**
500	1.500	**	1.327	**	1.202	**	1.181	**	0.917	**	1.077	**
570	1.800	**	1.147	**	1.273	**	0.992		1.001		0.911	**
700	1.458	**	1.156	**	1.202	**	1.168	**	0.860	**	1.381	**
800	1.454	**	1.371	**	1.208	**	1.032	**	0.831	**	1.312	**
1150	2.041	**	1.037	**	1.208	**	1.207	**	0.852	**	1.094	**
Efficiency												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	1.107	**	1.042	**	0.819	**	1.051		1.183	**	0.955	
370	0.963		1.065	**	0.947	**	1.021		1.096		0.880	**
500	0.929	**	1.082	**	1.000		1.000		0.981		0.957	
570	1.114	**	0.982		1.031		0.864	**	1.099	**	0.756	**
700	0.903	**	1.045	**	0.983	**	0.997		0.965	*	1.121	**
800	0.814	**	1.285	**	0.994		0.858	**	0.952	**	1.137	**
1150	1.087		1.000		1.000		1.000		1.000		1.000	
Technology												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	1.615	**	1.242	**	1.205	**	1.192	**	1.030		1.036	
370	1.615	**	1.242	**	1.205	**	1.192	**	1.015		1.036	
500	1.615	**	1.227	**	1.202	**	1.181	**	0.935	**	1.125	**
570	1.615	**	1.168	**	1.235	**	1.148	**	0.911	**	1.205	**
700	1.615	**	1.106	**	1.222	**	1.171	**	0.891	*	1.233	**
800	1.787	**	1.067		1.215	**	1.202	**	0.873	**	1.154	*
1150	1.878	**	1.037		1.208	**	1.207	**	0.852	**	1.094	

(***) p-value < 0.001, (**) p-value < 0.01, (*) p-value < 0.05.

Table 5: Changes in productivity, efficiency and technology for fresh sale revenues. Number greater (lower) than 1 indicate progress (regress).

Fresh sale (€/rope)												
Malmquist index												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	NA		1.498	**	1.279	**	1.253	**	1.330	**	0.997	**
370	6.014	**	1.403	**	1.291	**	1.672	**	1.003		1.093	**
500	2.807	**	1.413	**	1.361	**	1.403	**	0.963	**	1.074	**
570	NA		1.214	**	1.546	**	1.116	**	1.040	**	0.910	**
700	NA		1.320	**	1.331	**	1.367	**	0.858	**	1.581	**
800	NA		1.335	**	1.437	**	1.239	**	0.823	**	1.447	**
1150	NA		1.340	**	1.452	**	1.500	**	0.722	**	1.291	**
Efficiency												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	NA		1.122	**	0.893	**	0.876	**	1.303	*	0.831	**
370	2.004	**	1.051		0.901	**	1.177	**	1.000		0.911	*
500	0.935		1.069	**	0.950		1.026		1.025		0.810	**
570	NA		0.955		1.047		0.843	**	1.186	**	0.620	**
700	NA		1.000		0.944	*	0.991		1.049	**	1.019	
800	NA		1.005		1.015		0.853	**	1.078	**	0.966	
1150	NA		1.000		1.000		1.000		1.000		0.886	**
Technology												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	NA		1.335	**	1.432	**	1.429	**	1.021		1.200	**
370	3.001	**	1.335	**	1.432	**	1.420	**	1.003		1.200	**
500	3.001	**	1.322	**	1.432	**	1.367	**	0.939	**	1.325	**
570	NA		1.271	**	1.476	**	1.323	**	0.877	**	1.469	**
700	NA		1.320	**	1.409	**	1.379	**	0.818	**	1.551	**
800	NA		1.329	**	1.415	**	1.452	**	0.763	**	1.499	**
1150	NA		1.340	**	1.452	**	1.500	**	0.722	**	1.456	**

(***) p-value < 0.001, (**) p-value < 0.01, (*) p-value < 0.05.

Table 6: Changes in productivity, efficiency and technology for industry sale revenues. Number greater (lower) than 1 indicate progress (regress).

Industry (€/rope)												
Malmquist indices												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	2.986	**	1.374	**	1.023	**	1.138	**	1.011	**	0.957	**
370	2.649	**	1.399	**	1.083	**	1.180	**	0.965	**	0.811	**
500	3.133	**	1.418	**	1.210	**	1.003	**	0.892	**	0.960	**
570	4.087	**	1.219	**	1.341	**	0.782	**	0.900	**	0.890	**
700	2.378	**	1.168	**	1.128	**	1.093	**	0.772	**	1.321	**
800	3.281	**	1.464	**	1.187	**	0.982	**	0.703	**	1.314	**
1150	4.588	**	1.122	**	1.171	**	1.160	**	0.633	**	1.193	**
Efficiency												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	1.174	**	1.035		0.813	**	1.172	**	1.032		1.003	
370	1.042	*	1.054	**	0.862	**	1.216	**	1.000		0.849	**
500	1.232	**	1.080	**	0.962	*	1.039		1.000		0.926	*
570	1.607	**	0.972		1.029		0.816	**	1.112	**	0.775	**
700	0.935		0.980		0.903	**	1.068		1.042	**	1.086	**
800	1.166	**	1.271	**	0.977	**	0.891	**	1.037	**	1.091	**
1150	1.551	**	1.000		1.000		1.000		1.000		1.000	
Technology												
	M-Jn		Jn-Jl		Jl-Au		Au-S		S-O		O-N	
220	2.544	**	1.328	**	1.257	**	0.971		0.980		0.955	
370	2.544	**	1.328	**	1.257	**	0.970		0.965		0.955	
500	2.544	**	1.313	**	1.257	**	0.965		0.892	**	1.036	
570	2.544	**	1.254	**	1.303	**	0.959		0.809	**	1.148	**
700	2.544	**	1.191	**	1.249	**	1.024		0.740	**	1.217	**
800	2.815	**	1.152	**	1.214	**	1.102	**	0.678	**	1.204	**
1150	2.958	**	1.122	*	1.171	**	1.160	**	0.633	**	1.193	**

(***) p-value < 0.001, (**) p-value < 0.01, (*) p-value < 0.05.

Figure captions

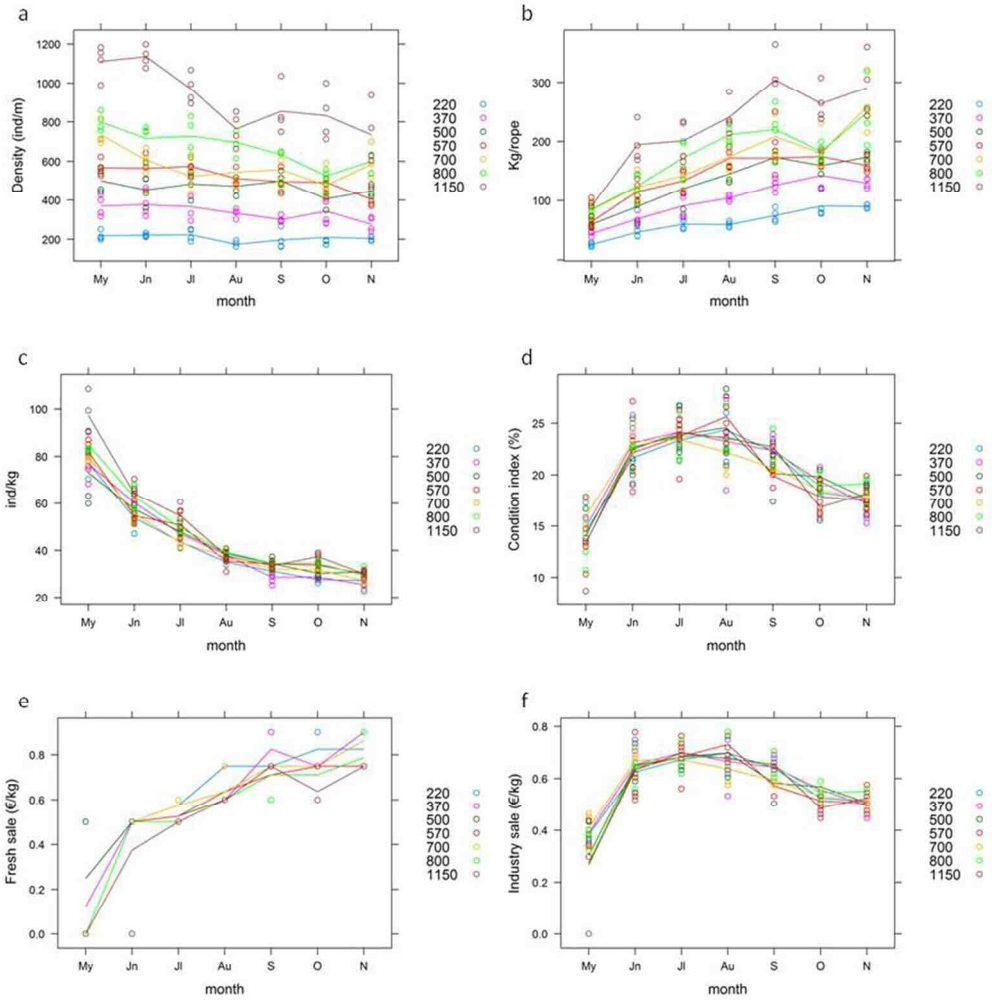
Fig. 1. Interaction plots of density (ind/m), total production (Kg/rope), individuals per kilogram of mussels (ind/Kg), individuals per kilogram of tissue (ind/Kg of tissue), condition index (%), fresh and industry sale prices (€/Kg) and costs (€/rope).

Fig. 2: GAM fit showing the effect of stocking biomass (Kg/rope) and cycle length (days) on fresh sale and industry sale profits (€/rope).

Fig. 3: GAM fits for the temporal evolution of profits obtained by fresh (black) and industry sale (red) by density treatment.

Fig. 4: Top: Marginal costs (P_x left) and VMP indices for total production of stocking biomass for fresh (centre) and industry (right) sale. Bottom: ratio between VMP and marginal costs for fresh and industry sale.

Fig. 5: Malmquist productivity, efficiency and technology indices for total production (top), fresh sale revenues (centre) and industry sale revenues (bottom).



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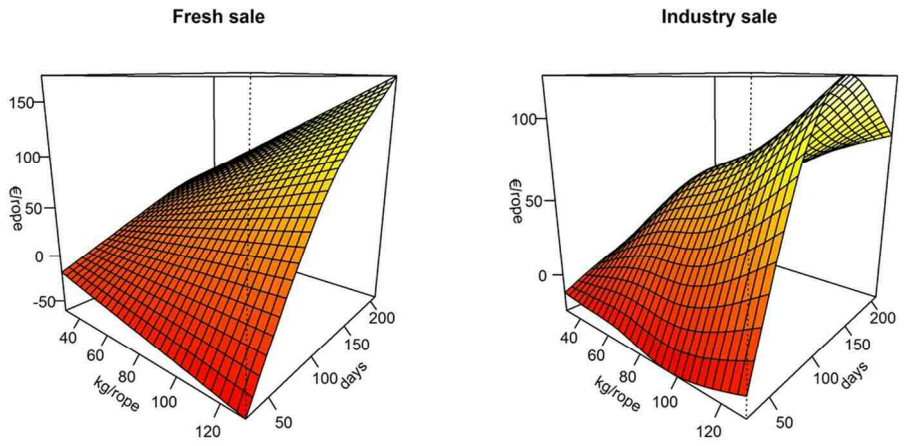

Fig. 2: GAM fit showing the effect of stocking biomass (Kg/rope) and cycle length (days) on fresh sale and industry sale profits (€/rope).
99x55mm (300 x 300 DPI)

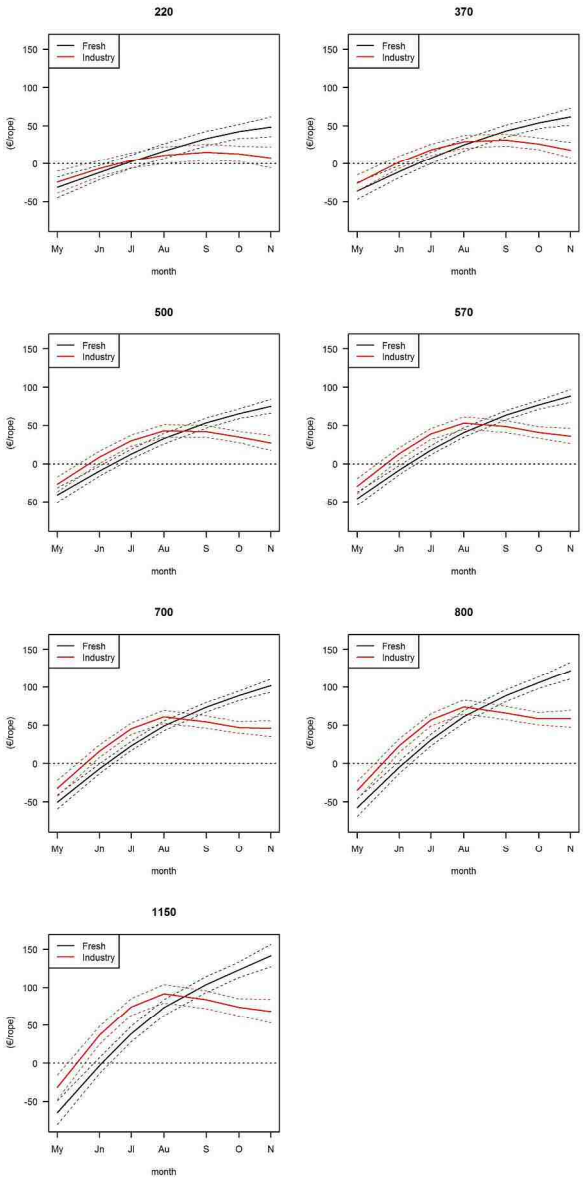

Fig. 3: GAM fits for the temporal evolution of profits obtained by fresh (black) and industry sale (red) by density treatment.
239x479mm (300 x 300 DPI)

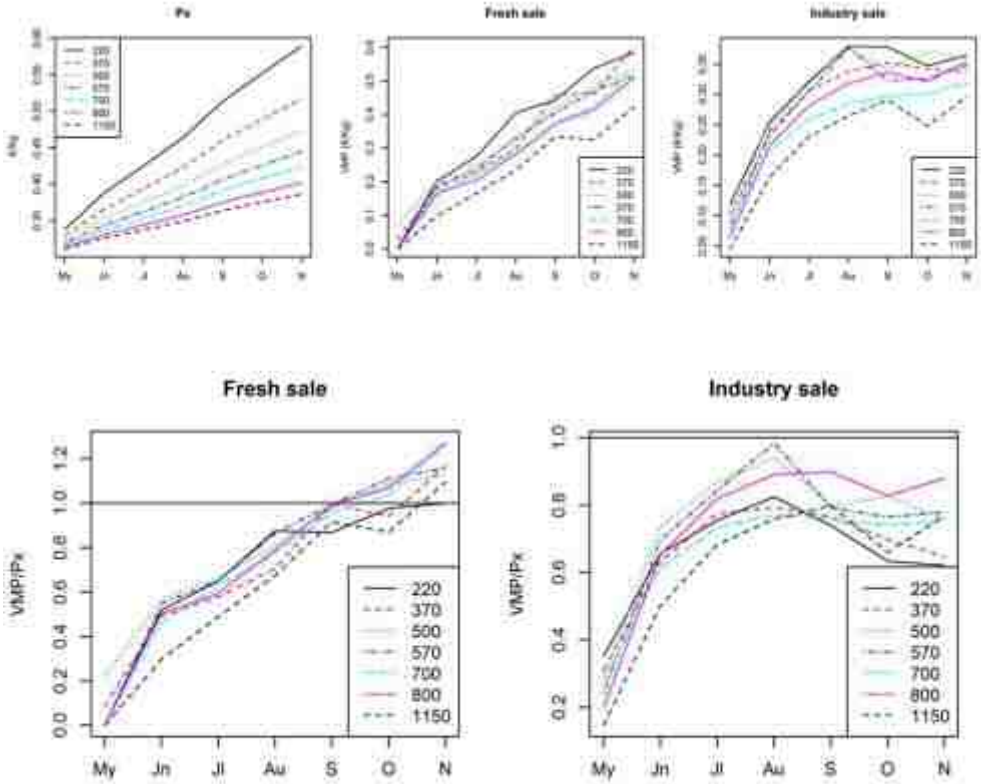

Fig. 4: Top: Marginal costs (Px left) and VMP indices for total production of stocking biomass for fresh (centre) and industry (right) sale. Bottom: ratio between VMP and marginal costs for fresh and industry sale.
160x137mm (150 x 150 DPI)

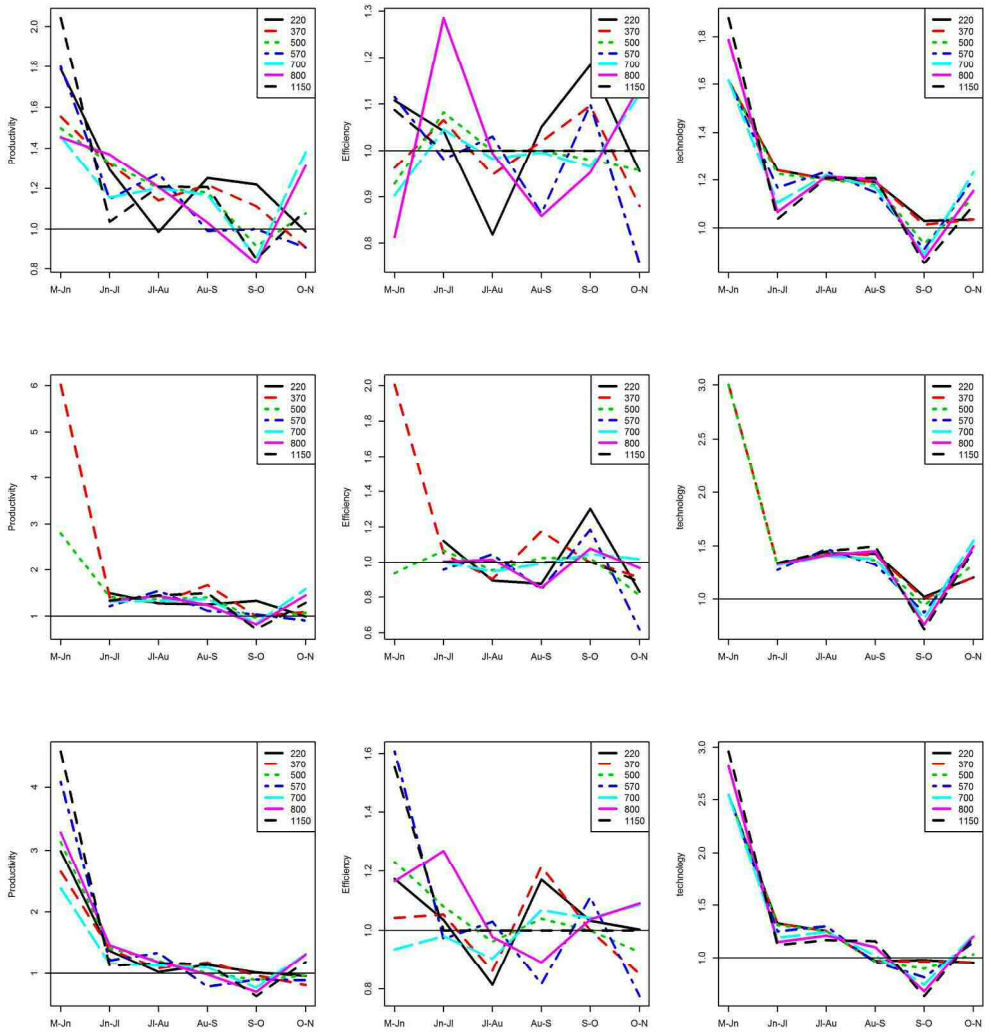

Fig. 5: Malmquist productivity, efficiency and technology indices for total production (top), fresh sale revenues (centre) and industry sale revenues (bottom).
219x241mm (300 x 300 DPI)