

# High resolution imaging of (100) kyanite surfaces using friction force microscopy in water

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## Abstract

In this paper we present high resolution friction force microscopy (FFM) images of the (100) face of kyanite ( $\text{Al}_2\text{SiO}_5$ ) immersed in water. These images show an almost rectangular lattice presumably defined by the protruding oxygens of  $\text{AlO}_6$  polyhedra. Surface lattice parameters measured on two-dimensional fast Fourier transform (2D-FFT) plots of recorded high resolution friction maps are in good agreement with lattice parameters calculated from the bulk mineral structure. Friction measurements performed along the [001] and [010] directions on the kyanite (100) face provide similar friction coefficients  $\mu \approx 0.10$ , even if the sequences of  $\text{AlO}_6$  polyhedra are different along the two crystallographic directions.

## 1. Introduction

Kyanite,  $\text{Al}_2\text{SiO}_5$ , is an important metamorphic nesosilicate, which is commonly found in rocks formed in ancient and present subduction zones [1, 2]. This mineral is the high pressure polymorphous of the aluminium silicate group with formula  $\text{Al}_2\text{SiO}_5$  (i.e, sillimanite, andalusite and kyanite). This group of minerals has been used by petrologists from long time ago to estimate pressure and temperature metamorphic conditions on the basis of their phase diagram. However, the

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30 use of the  $\text{Al}_2\text{SiO}_5$  phase diagram to infer metamorphic conditions is problematic due to the high  
31 metastability of all three mineral structures, which persist for long periods of time under P-T  
32 conditions far from equilibrium [3]. The metastability of  $\text{Al}_2\text{SiO}_5$  minerals is mainly due to the fact  
33 that transformations from one mineral to another are reconstructive and they involve breaking  
34 strong Si – O and Al – O bonds [4]. In the case of kyanite, the high pressure  $\text{Al}_2\text{SiO}_5$  polymorph, the  
35 arrangement of Si – O and Al – O bonds seems to be not only responsible for its metastability, but  
36 also for its remarkable hardness anisotropy. Therefore, the understanding of both the rheological  
37 properties of kyanite and its reactivity in geotectonic environments will be improved conducting  
38 detailed crystallochemical studies of this mineral and, particularly, of its surfaces.

39  
40 The main industrial use of kyanite is in refractory industry as a raw material to produce mullite,  
41 an important refractory mineral. Mullite is a rare mineral that only appear in a few uneconomical  
42 mineral deposits in the world [5]. The industrial process to produce mullite from  $\text{Al}_2\text{SiO}_5$  minerals  
43 is through calcination at temperatures higher than 1000 °C [6]. Kyanite has the lowest temperature  
44 decomposition of the three  $\text{Al}_2\text{SiO}_5$  minerals and, therefore, it is the most suitable to produce  
45 mullite [6]. Kyanite is also used in abrasive and electrical industries. Nowadays, new studies in  
46 kyanite applications propose other applications, such as its use to obtain metallurgical alumina [7].  
47 Both the development and improvement of new industrial uses of kyanite also requires a better  
48 understanding of its crystallochemical surface properties.

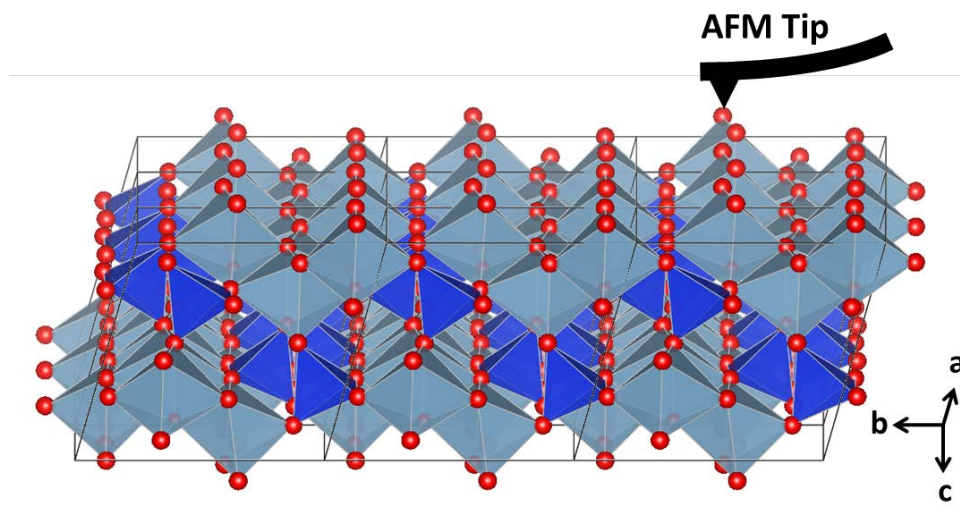
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50 In this work we show first images and friction measurements of kyanite (100) surfaces recorded  
51 using a Friction Force Microscopy (FFM) operating in contact mode in water. This technique was  
52 used in previous works by our group to obtain images with molecular resolution of mineral  
53 surfaces, organic molecules grown on minerals and organic crystals [8 – 12]. In addition, this  
54 method allows us to obtain the friction coefficient between probing tip and surface along different  
55 crystallographic orientations. Both high resolution images and friction coefficients obtained in this

paper are discussed on the basis of the structural features of kyanite (100) surface.

## 2. Materials and methods

### 2.1. The kyanite sample

Kyanite crystallises in the triclinic  $P\bar{1}$  space group with the following cell parameters:  $a = 0.71$  nm,  $b = 0.79$  nm,  $c = 0.56$  nm,  $\alpha = 89.99^\circ$ ,  $\beta = 101.15^\circ$ ,  $\gamma = 105.95^\circ$ , and  $Z = 4$  [13]. Kyanite structure can be described as formed by chains of edge-sharing  $\text{AlO}_6$  and  $\text{SiO}_4$  polyhedra running along the  $c$  axis (Fig. 1). This orientation of the chains of  $\text{AlO}_6$  and  $\text{SiO}_4$  polyhedra can be related to the different hardness of kyanite, measured on different crystallographic planes. Hence the hardness of kyanite in Mohs' scale is  $\approx 7$  for  $[100]$  and  $[010]$ , and  $\approx 5$  for  $[001]$ . Exfoliation of kyanite crystals along the  $(100)$  and  $(010)$  faces are perfect and poor, respectively. Along the  $(001)$  plane no exfoliation occurs. The combination of these three faces results in typical fibrous habit of kyanite [14].



**Fig. 1.** Structure of kyanite.  $\text{AlO}_6$  and  $\text{SiO}_4$  polyhedra are represented in light and dark blue respectively. Oxygens are represented as red spheres. The top face is the  $(100)$  surface and the tip is represented on it. The axis  $b$  and  $c$  correspond to the  $[010]$  and  $[001]$  directions, respectively. (Colours only in the online version). (Structure projection made with Vesta [15]).

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77 The sample used in this work was a kyanite from Brazil. The sample was confirmed to be  
78 kyanite (PDF number 11-0046) by X-ray powder diffraction conducted with a Siemens D-500  
79 diffractometer, equipped with a Cu-K $\alpha$  radiation source.

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## 81 **2.2. Friction Force Microscopy (FFM)**

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83 The study presented here was performed using a commercial AFM (Nanoscope Multimode IIIa,  
84 Veeco Instruments), equipped with a  $\sim 15 \times 15 \mu\text{m}^2$  scanner and a closed fluid cell. Kyanite crystals  
85 were freshly cleaved along (100) faces with a razor blade and placed in the AFM fluid cell. Then,  
86 deionised water (Mili-Q, 18 M $\Omega$ ·cm) was injected into the fluid cell. Both observations and data  
87 collection were carried out at room temperature operating in contact mode while recording height  
88 and lateral deflection signals. Scan areas ranged from  $2 \times 2 \mu\text{m}^2$  to  $10 \times 10 \text{ nm}^2$  and the scan rates  
89 varied from  $\sim 5$  Hz to  $\sim 61$  Hz. In all the cases, 512 lines per scan were recorded. Supersharps tips  
90 mounted on triangular cantilevers (Bruker SNL-10 D) were used for acquiring high resolution  
91 images.

92

93 Lateral deflection signals recorded with the AFM were used to map the friction forces while  
94 scanning square areas along the [010] and [001] directions on kyanite (100) faces at different  
95 loading forces. The experiments were carried on by applying increasing-decreasing cycles of  
96 normal force. The equation used to calculate lateral forces was [16]:

$$97 \quad F_L = \frac{3h}{2L} * k_T * S * V_L \quad (1)$$

98 where  $h$  is the height of the tip and half of the cantilever thickness,  $L$  is the length of the cantilever,  
99  $k_T$  is the torsional spring constant of the cantilever (calculated following Noy et al. [17]),  $S$  is the  
100 sensitivity of the photodetector in nm/V, and  $V_L$  is the difference of the averaged trace and retrace  
101 signals (in Volts) divided by 2. The normal force was estimated as [16]:

$$F_N = S * k_N * V_N \quad (2)$$

where  $k_N$  is the normal spring constant and  $V_N$  is the setpoint value (in Volts). Both sharp silicon nitride (Bruker NP-10 D) and supersharp silicon nitride (Bruker SNL-10 D) tips were used for performing nanotribological measurements.

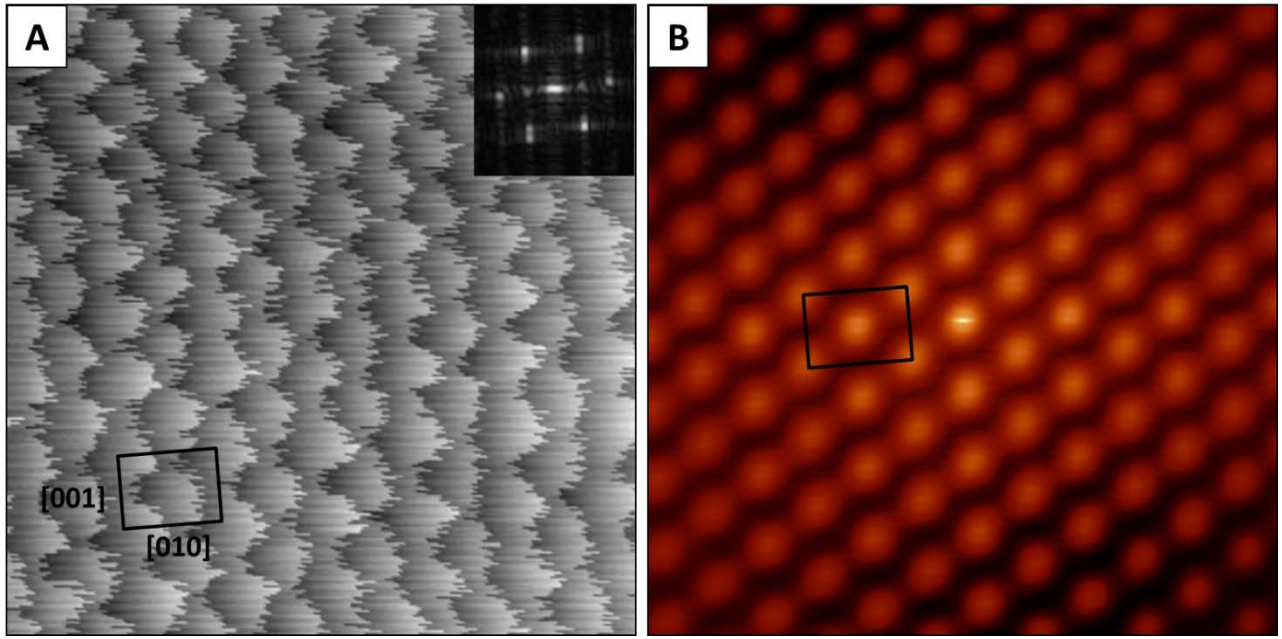
More than 100 AFM images were collected and analysed using the software developed by Nanoscope (5.30r3sr3) and Nanotec (WSxM) [17].

### 3. Results and Discussion

#### *3.1. High resolution FFM images of kyanite (100) surface*

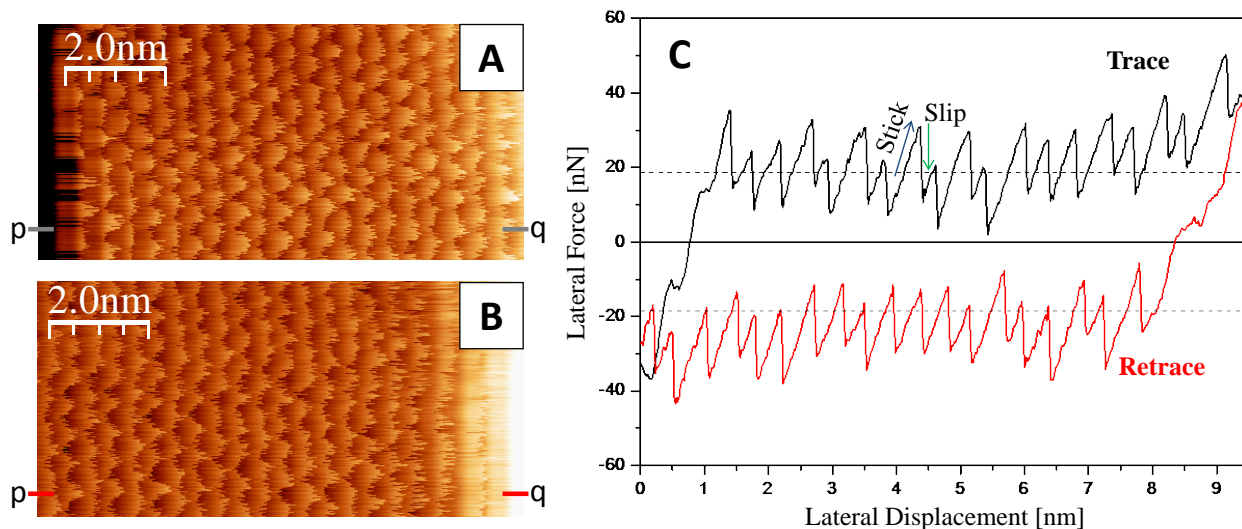
When small areas ( $10 \times 10 \text{ nm}^2$ ) of kyanite (100) surfaces are scanned almost parallel to the [010] direction, lattice resolved friction images are readily acquired. It is important to note that images with lattice resolution were obtained only when kyanite surfaces were fully immersed in water. This is mainly due to the fact that a homogeneous liquid environment eliminates capillarity forces (i.e. the formation of meniscus between the AFM tip and the surface) and the sliding process is not significantly perturbed by viscous forces [8-12]. As a result, the quality and resolution of recorded images is strongly improved.

The patterns observed in high resolution friction images show an almost rectangular centred lattice defined by five maxima of the friction force (Fig. 2). The main directions on the (100) surface defined by the maxima are [010] and [001]. Since the angle between these directions is  $89.99^\circ$  [13], the surface unit cell is almost rectangular.



**Fig. 2.** (A) High resolution friction image of (100) kyanite surface in water acquired with a misalignment of  $\approx 5^\circ$  from the [010] direction. Black rectangle shows the unit cell on the face. The inset shows a 2D-FFT map. (B) Autocorrelation image of image A. Dots show the maxima of friction. Black rectangle shows the unit cell. Image recorded with  $F_N = 32.56$  nN and  $F_L = 16.48$  nN. The size of both images is  $5.5 \times 5.5$  nm<sup>2</sup>.

Maxima in friction maps can be interpreted as the result of stick-slip phenomenon between the tip apex and selected atoms protruding out of the scanned surfaces (e.g. Pina et al. [8]). This is clearly visible in the images corresponding to a series of complete forward and backward scans along the surfaces (Fig. 3A, B), and, especially, in the cross sections showing saw-tooth profiles corresponding to long stick and much faster slip phases (Fig. 3C).

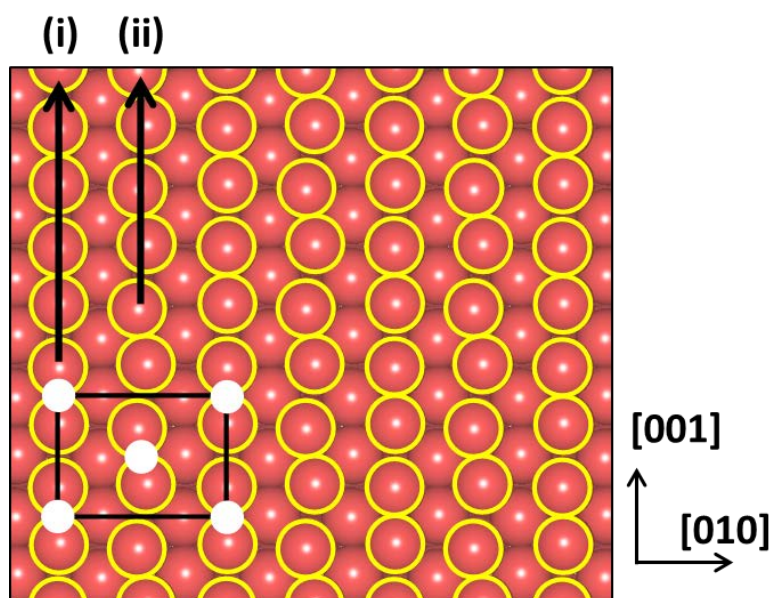


**Fig. 3.** High resolution images of kyanite (100) surface: A) trace friction image and B) retrace friction image. C) Lateral force corresponding to the p-q profile in Fig. 3A, B. The saw tooth pattern is characteristic of the stick-slip phenomenon. Blue arrow shows the stick event and green arrow the slip event. (Colours only in the online version).

In order to correctly identify the surface atoms which originate the friction maxima during the scan we refer to the kyanite (100) surface structure sketched in Figure 1. As can be seen in this figure, a number of oxygens atoms belonging to  $\text{AlO}_6$  polyhedra protrude out of the (100) face. A similar situation was observed in Pina et al. [8], where the friction maxima detected on the (104) face of calcite and dolomite were related to oxygen atoms protruding out of the surfaces. In that case, the correspondence was supported by a numeric analysis based on the Prandtl-Tomlinson (PT) model, which predicted lateral force maps at different scan directions consistent with the zigzag arrangement of those atoms. Note that, in the case of Pina et al. [8], the shortest distance between the protruding oxygens was 0.48 nm.

In the present case, Figure 4 shows the projection of protruding oxygens of the  $\text{AlO}_6$  polyhedra on kyanite (100) face. In this projection, two sequences of such atoms can be distinguished: (i) rows of oxygens aligned parallel to the [001] direction and (ii) oxygens running in a zigzag way along such a [001] direction. While distances between oxygens belonging to the same  $\text{AlO}_6$  polyhedron are less than 0.26 nm, distances between oxygens belonging to contiguous polyhedra

are slightly larger than 0.30 nm. A comparison with the peaks in Figure 2 shows that only half of the protruding oxygen atoms in the unit cell may be imaged in the friction maps. Since the distances between neighbour oxygens are well below those on calcite and dolomite (104) it is quite reasonable that the imaging process on kyanite (100) will be more influenced by convolution with the tip apex. With this in mind, we notice that the almost centred rectangular lattice in Figure 2 can be obtained if the tip sticks to a pair of protruding oxygen atoms coupled in two possible different schemes [respectively (i) and (ii) in Figure 4]. The stick-slip pattern observed with an atomically sharp tip would result in a double number of peaks.



**Fig. 4.** Kyanite structure projected on its (100) plane. Oxygens are represented by red circles and protruding oxygens are highlighted with yellow rims. Black rectangle shows the surface unit cell on the (100) surface. White dots indicate positions where friction maxima presumably occur. The (i) and (ii) black arrows show the two sequences of protruding oxygens (Colours only in the online version). (Structure projection made with Vesta [15]).

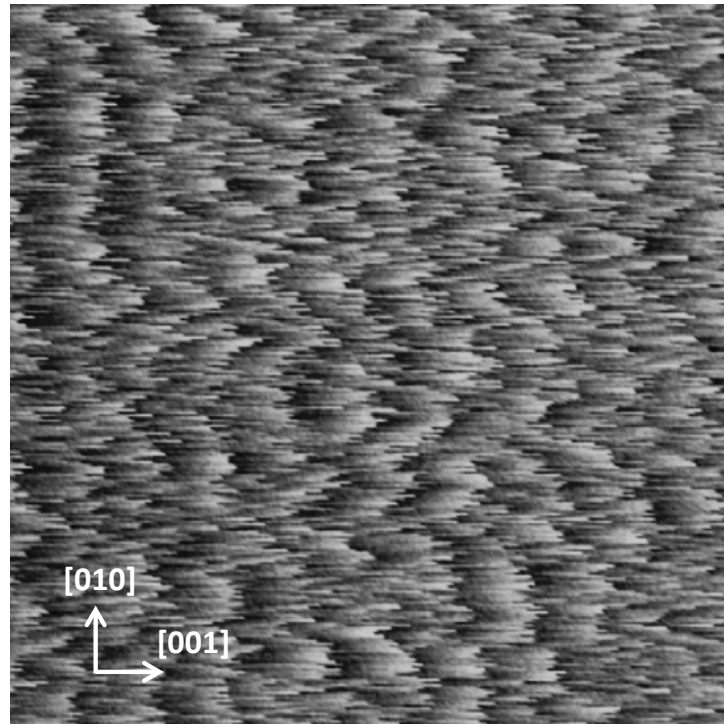
The centred rectangular lattice parameters were measured on 2D-FFT maps calculated from the high resolution friction images. These parameters are  $b_s = 0.82 \text{ nm} \pm 0.02$  and  $c_s = 0.56 \text{ nm} \pm 0.03$  nm, measured along [010] and [001] directions, respectively. These values are in good agreement with the lattice parameters obtained from the kyanite bulk structure, i.e.  $b_s = 0.79 \text{ nm}$  and  $c_s = 0.56$



176 nm [13]. The average difference between the parameters obtained from our friction maps and those  
177 derived from kyanite structure is less than 4%. This little difference indicates that kyanite (100)  
178 surfaces do not experience any significant reconstruction or relaxation phenomena in water at room  
179 temperature

180 We have also imaged the kyanite (100) surface while scanning almost parallel to the [001]  
181 direction (see Fig. 5). Note that the sample was physically rotated by 90° in order to perform these  
182 measurements. In this case, a characteristic distance comparable to  $c_s$  ( $c_s' = 0.52 \pm 0.03$ ) can still be  
183 distinguished, whereas the surface lattice looks quite distorted in the [010] direction. This may be  
184 due to the (unknown) atomic arrangement at the tip apex, preventing a commensurate contact upon  
185 sample rotation. Furthermore, a complete evaluation of the effect of the tip-surface interaction on  
186 the image resolution would also require a detailed simulation of tip trajectories based on the  
187 Prandtl-Tomlinson model [20], which is beyond the scope of this paper.

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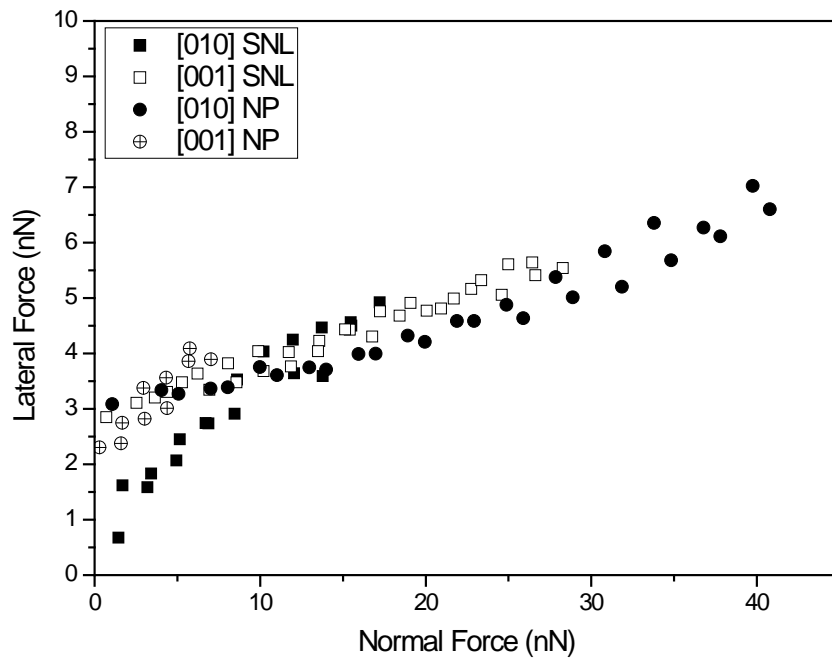
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190 **Fig. 5.** (A) High resolution friction image of (100) kyanite surface in water acquired when scanning along [001]  
191 direction. Image recorded with  $F_N = 23.33$  nN and  $F_L = 13.40$  nN. The size of the image is  $5.5 \times 5.5$  nm<sup>2</sup>

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### 3.2. Load dependence of the friction force

The average friction forces have been measured on areas of  $10 \times 10 \text{ nm}^2$  and  $500 \times 500 \text{ nm}^2$  while scanning almost parallel to the [010] and [001] directions on this face. Fig. 6 shows the variation of this “lateral” force,  $F_L$ , with the applied loading (normal) force,  $F_N$ . The applied load ranged from 0 to 40 nN. In this range of loading forces no wear was observed, which is consistent with the relatively high Mohs’ hardness of kyanite (100) surface ( $\approx 7$  for the [010] direction, and  $\approx 5$  for the [001] direction). The measurements were performed by increasing the normal force and then by decreasing it and using tips with two different nominal radii: SNL-10D (2 nm) and NP-10D (20 nm). By doing that we have checked the reproducibility of the measurements and evaluated the effect of tip contact areas on friction. As can be seen in Fig. 6, a similar dependency between loading force and measured friction for the two directions was obtained. Furthermore, the use of tips with different radii did not significantly affect our friction measurements.



**Fig. 6.** Lateral force vs. normal force graph measured along directions almost parallel to [010] (solid symbols) and [001] (open symbols). Squares show the experiments performed with SNL-10 D tips and circles show the experiments performed with NP-10 D tips.

From data shown in Fig. 6 we have calculated the friction coefficient as the slope of the  $F_L(F_N)$

222 curves ( $\mu = dF_L/dF_N$ ). The data are almost independent on both the tip radii and the sliding direction,  
223 and an average friction coefficient  $\mu \approx 0.10$  is obtained in all cases. A discrepancy is observed only  
224 in the very first data points acquired with the SNL tip along the [010] direction, where the tip was  
225 possibly very sharp and a negligible offset was measured [compared to the value  $F_L(0) \approx 3$  nN  
226 recorded in the subsequent measurements]. It is quite noticeable that, the average values of the  
227 friction forces are similar in the two directions in spite of the different resolution obtained in the  
228 FFM maps. While similar friction coefficients indicate comparable tip-surface interactions along the  
229 [001] and [010] directions, the different resolution obtained can be related to differences in tip  
230 configuration and tip trajectories when the scan is performed along such directions [21].

231

### 232 **3. Concluding remarks**

233

234 1.- In this paper we have reported first images with lattice resolution of the kyanite (100) faces  
235 using FFM in water. Maxima in the friction maps reflect the stick-slip motion of the probing tip  
236 pulled along the cleavage surface and the convolution between the tip and two protruding oxygens  
237 belonging to each  $\text{AlO}_6$  polyhedron. Interestingly, the resolution of the acquired images varies  
238 strongly with the scan direction, indicating different degrees of commensurability between the tip  
239 apex and the surface lattice.

240 2.- Maxima in the friction maps define an almost centred rectangular lattice with unit cell  
241 dimensions ( $b_s = 0.82 \text{ nm} \pm 0.02$  and  $c_s = 0.56 \text{ nm} \pm 0.03$ ) in good agreement with data derived from  
242 the reported bulk structure. Therefore, any significant reconstruction or relaxation phenomena in the  
243 kyanite (100) surface structure can be discarded.

244 3.- Systematic measurements of friction using tips with different radii and materials (silicon  
245 and silicon nitride) provided similar friction coefficients (in the order of  $\mu = 0.10$ ) when the kyanite  
246 (100) surface was scanned along two perpendicular crystallographic directions, i.e. [001] and [010].

247 Our results can be of interest for theoretical investigations on the relation between surface

commensurability and friction anisotropy on the atomic scale, which, so far, have mainly focused on graphite surfaces [19, 20, 22]. An extension of our experimental analysis to different mineral surfaces can be important for understanding the mechanical response of the material under shear with ultimate applications to earthquake dynamics.

## Acknowledgments

This work was supported by the Spanish Ministry of Economy and Competitiveness (Project MAT2012-24487). C.P. acknowledges to Spanish Ministry of Education, Culture and Sports a FPU grant. AFM observations were carried out at ICTS Centro Nacional de Microscopía Electrónica at the Complutense University of Madrid.

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