High-pressure optical absorption in InN: Electron density dependence in the wurtzite phase and reevaluation of the indirect band gap of rocksalt InN

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(Received 11 June 2012; published 24 July 2012)

We report on high-pressure optical absorption measurements on InN epilayers with a range of free-electron concentrations (5 × 10¹⁷–1.6 × 10¹⁹ cm⁻³) to investigate the effect of free carriers on the pressure coefficient of the optical band gap of wurtzite InN. With increasing carrier concentration, we observe a decrease of the absolute value of the optical band gap pressure coefficient of wurtzite InN. An analysis of our data based on the k·p model allows us to obtain a pressure coefficient of 32 meV/GPa for the fundamental band gap of intrinsic wurtzite InN. Optical absorption measurements on a 5.7-μm-thick InN epilayer at pressures above the wurtzite-to-rocksalt transition have allowed us to obtain an accurate determination of the indirect band gap energy of rocksalt InN as a function of pressure. Around the phase transition (~15 GPa), a band gap value of 0.7 eV and a pressure coefficient of ~23 meV/GPa are obtained.

DOI: 10.1103/PhysRevB.86.035210

PACS number(s): 78.66.Fd, 78.40.Fy, 71.20.Nr

I. INTRODUCTION

InN and related group-III nitride alloys such as InGaN and InAlN have enormous potential to develop novel applications for optoelectronics, photovoltaics, or high-frequency electronics. The revision of the band gap energy of wurtzite InN (w-InN) to a value of only E₉ ≈ 0.7 eV gave rise to renewed interest in these compounds, because their band gap energy may be tuned over a wide spectral range, from the near infrared to the ultraviolet. This remarkable property could be exploited to fabricate high-efficiency solar cells and light emitting diodes.1

Despite much effort to investigate the structural, electronic, optical, and vibrational properties of w-InN at ambient pressure, relatively little is known about the properties of this material as a function of pressure. X-ray diffraction (XRD) and Raman scattering studies showed that the wurtzite-to-rocksalt phase transition takes place at ~14 GPa.2–5 From these structural and lattice-dynamic investigations, values for the bulk modulus and mode Gruneisen parameters of both phases were obtained. In turn, several works have studied the pressure dependence of the fundamental band gap of w-InN and InGaN.6–10 In general, the pressure dependence of the optical-emission peak energy in InN and InGaN is weaker than that of the absorption edge.6,10 The observed differences have been attributed to a sizable contribution of impurity states to the optical emission of the samples. Other authors, however, by direct comparison of PL data with pressure coefficients obtained with ab initio calculations, conclude that the PL emission from w-InN and InGaN has a mainly band-to-band character.11

Kamińska et al.8 showed that conduction-band filling has a clear effect on the photoluminescence (PL) peak pressure coefficient dE₉/dP of w-InN. This effect can be attributed to a reduction of the Fermi energy with increasing pressure as a consequence of the increasing electron effective mass. However, with the PL data alone, it is not possible to rule out that the experimental dE₉/dP values are further reduced by impurity emission. Bearing in mind the different pressure coefficients measured so far in InN and InGaN with PL and absorption techniques, the determination of the absorption-edge pressure coefficients dE₉/abs/dP as a function of the free-carrier concentration could be highly informative with regard to the localized/band-to-band character of the PL emission.

It has been recently shown that rocksalt InN (rs-InN) is an indirect semiconductor with a band gap energy of ~1 eV around the transition pressure.12 However, in that work, the very low absorbance of the sample investigated (an InN epilayer with a thickness of 500 nm) allowed only the determination of the higher energy direct transition at the Γ point. Therefore, an accurate determination of the energy of the indirect band gap of rs-InN and its pressure dependence is necessary.

In the present work, we carry out high-pressure optical absorption measurements in w-InN and rs-InN. We investigate the effect of free carriers on the pressure coefficient of the optical band gap of w-InN. For this purpose, different samples with carrier concentrations in the 5 × 10¹⁷–1.6 × 10¹⁹ cm⁻³ range are employed. Optical measurements on the thickest epilayer available (5.7 μm) allow us to study in detail the wurtzite-to-rocksalt transition and to obtain an accurate determination of the energy of the indirect band gap of rs-InN and its pressure behavior.

II. EXPERIMENT

Four nominally undoped c-face w-InN epilayers were grown by molecular beam epitaxy on sapphire substrates. The background electron concentration (thickness) of these samples was 5 × 10¹⁷ cm⁻³ (5.7 μm), 2 × 10¹⁸ cm⁻³ (500 nm), 6.5 × 10¹⁸ cm⁻³ (400 nm), and 1.6 × 10¹⁹ cm⁻³ (400 nm).13,14 Flakes containing InN were detached from the substrates and
loaded, together with several ruby chips, into a 200-μm-diameter hole drilled on a 50-μm-thick Inconel gasket. The gasket was placed between the two diamond anvils of a membrane-type diamond anvil cell. Methanol–ethanol–water (16:3:1) was used as a pressure-transmitting medium, and pressure was determined from the fluorescence of ruby chips. Room-temperature optical absorption of the flakes was measured as a function of pressure using a tungsten lamp, spatial filters, and reflective objectives. For the mid-infrared spectral range, the measurements were performed using a single-grating monochromator and PbS or InAs detectors with lock-in amplification. For near-infrared and visible measurements, a multichannel spectrophotometer was employed.

III. RESULTS AND DISCUSSION

A. Wurtzite InN

Optical absorption measurements were carried out to investigate the electron density dependence of the band gap pressure coefficients of w-InN. Figure 1 shows the absorption coefficient $\alpha$ at different pressures for the two w-InN epilayers with low and high electron densities ($n = 5 \times 10^{17}$ and $1.6 \times 10^{19}$ cm$^{-3}$) in Fig. 1(a) and 1(b), respectively. Both figures show the expected blueshift of the absorption edge with increasing $P$ and the effect of conduction-band filling. The latter is evidenced in Fig. 1(b) by the higher energy of the absorption edge in the absorption spectra, i.e., in the spectra of the sample with $n = 1.6 \times 10^{19}$ cm$^{-3}$. From an analysis of the absorption coefficient at ambient pressure based on a sigmoidal dependence on photon energy, we extract for the sample with $n = 5 \times 10^{17}$ cm$^{-3}$ a band gap energy value of 0.65 eV. This value is in excellent agreement with that obtained with the same procedure for samples with similar electron densities (0.64 eV, see Ref. 16). With increasing $n$, we find that the band gap energy monotonically increases up to $\approx 0.8$ eV for $n = 1.6 \times 10^{19}$ cm$^{-3}$, in very good agreement with published values.

Figure 2 shows the pressure coefficient of the absorption edge $dE_{abs}/dP$, as a function of $n$, as extracted from the pressure-dependent optical absorption measurements on the different samples studied in this work. Data from Ref. 6 also obtained with optical absorption experiments have been included in the plot for comparison. As can be seen in the figure, $dE_{abs}/dP$ is reduced from 30–32 meV/GPa for the samples with the lowest electron densities down to $\approx 24$ meV/GPa for $n = 1.6 \times 10^{19}$ cm$^{-3}$. A similar observation was obtained by low-temperature PL measurements in Ref. 8 and attributed to conduction-band-filling effects. Data points from this work can also be found in Fig. 2. However, the $dE_{PL}/dP$ values reported in that work were consistently lower than those obtained with the present optical absorption measurements (e.g., 27.3 meV/GPa at $n = 3.6 \times 10^{17}$ cm$^{-3}$ and 20.8 meV/GPa at $n = 1.1 \times 10^{19}$ cm$^{-3}$; see Ref. 8). This observation seems to confirm that the pressure dependence of the PL emission in InN is in general weaker than that of the absorption edges. In Refs. 6 and 10, the difference between the pressure coefficients obtained with emission and absorption techniques was related to the possible participation of impurity states (i.e., of highly localized states with low-pressure coefficients) in the PL emission of InN and InGaN.

The solid line in Fig. 2 shows the result of a calculation of the pressure coefficient of the optical band gap as a function of $n$ in w-InN. This calculation was performed using an approximation of the two-band $k\cdot p$ Kane model in the small effective mass limit to take into account the nonparabolicity.

![FIG. 1. Optical absorption spectra at different hydrostatic pressures of two InN epilayers with free-electron concentrations of (a) $5 \times 10^{17}$ cm$^{-3}$ (thickness 5.7 μm) and (b) $1.6 \times 10^{19}$ cm$^{-3}$ (thickness 400 nm).](image-url)

![FIG. 2. (Color online) Pressure coefficient of the optical band gap of InN as a function of electron concentration. The data obtained in this work with high-pressure optical absorption measurements are plotted with circles. Data reported in Refs. 6 (triangle) and 8 (squares), obtained with optical absorption and PL measurements, respectively, have also been included in the plot. The curve is the calculated dependence based on the $k\cdot p$ model. For the calculation, a band gap pressure coefficient of 32 meV/GPa at a zero electron concentration has been used.](image-url)
of the conduction band of InN. Following Ref. 8, it was assumed that the pressure coefficient of the optical band gap \((dE_{\text{abs}}/dP)\) has two contributions: one from the band gap pressure coefficient in the intrinsic semiconductor \(dE_G/dP\) and a second one arising from the pressure dependence of the Fermi energy \(dE_F/dP\). The latter is a consequence of the flattening of the conduction band (i.e., of the increasing electron effective mass) with increasing pressure; therefore, it has a negative value. To calculate the derivative of \(E_F\) as a function of \(n\) and obtain the curve of Fig. 2, the Fermi energy was numerically calculated for different \(n\) and \(P\) values at room temperature by taking a zone-center electron effective mass value equal to \(m^*_e = 0.07m_e\) at ambient pressure.\(^{3}\) Pressure-dependent \(m^*_p(P)\) values were obtained using the expression \(m^*_p(P) \approx m^*_p(0) E_G(P)/E_G\) from the \(k-p\) theory, where \(E_G = 0.65\) eV is the band gap of InN at ambient pressure and \(E_G(P)\) is assumed to vary linearly with pressure, i.e., \(E_G(P) = E_G + (dE_G/dP)P\), where \(dE_G/dP\) is left as an adjustable parameter.

Within this approach, we find that a value of \(dE_G/dP = 32\) meV/GPa yields the best agreement between the theoretical and the experimental data over a large range of electron densities (Fig. 2). This pressure coefficient value is in very good agreement with the predictions of many-body perturbation theory in the \(G_0W_0\) approximation.\(^{19}\) Such calculations, which provide excellent \(E_G\) values for w-InN at ambient pressure (0.69 eV), yield \(dE_G/dP\) values in the range of 28–33 meV/GPa.\(^{19}\)

In the range of low electron densities \((n < 10^{18} \text{ cm}^{-3})\), where conduction-band-filling effects are expected to be small, the \(dE_{\text{abs}}/dP\) curve calculated using \(dE_G/dP = 32\) meV/GPa falls between the two data points obtained with optical absorption measurements plotted in Fig. 2 (one of them from Ref. 6). When \(n\) goes to zero, the Fermi energy exhibits some pressure dependence arising from the pressure dependence of \(m^*_e\) in the intrinsic semiconductor. As a consequence, for low electron densities, the calculated \(dE_{\text{abs}}/dP\) values in Fig. 2 tend not to \(dE_G/dP = 32\) meV/GPa but to a somewhat lower value (~30.5 meV/GPa).

As can be seen in Fig. 2, the reduction of \(dE_{\text{abs}}/dP\) predicted by the \(k-p\) calculation agrees well with the experimental data obtained by optical absorption measurements for the samples with higher electron densities, thus confirming that conduction-band filling is responsible for the reduction of \(dE_{\text{abs}}/dP\) with increasing \(n\). Our data and analysis suggest that the true value of \(dE_G/dP\) in intrinsic w-InN is 32 meV/GPa, in the upper limit of the calculations of Ref. 19. By using the bulk modulus \((B_0 = 125.5\) GPa) obtained by means of XRD in Ref. 2, we obtain a volume deformation potential for w-InN of \(dE_G/d\ln V = -4.0\) eV.

For sufficiently high electron concentrations, band gap renormalization effects arising from electron–electron interactions and carrier–ion correlations are expected to yield reduced band gap energies.\(^{18}\) These many-body effects partially compensate for the magnitude of the band gap increase arising from conduction-band filling and result in energy redshifts of \(\sim 150\) meV per decade of change of \(n\) above \(10^{19} \text{ cm}^{-3}\) in w-InN.\(^{18}\) Here, to evaluate the role of band gap renormalization on \(dE_{\text{abs}}/dP\), we calculated the pressure coefficients for the conduction-band shifts resulting from electron–electron interaction \((\Delta E_{e-e})\) and electron–ion interaction \((\Delta E_{e-i})\) as a function of \(n\). For this purpose, we used the expressions given in Ref. 18 for both \(\Delta E_{e-e}\) and \(\Delta E_{e-i}\) and we obtained their pressure derivatives by numerical methods. Below \(5 \times 10^{18} \text{ cm}^{-3}\), our calculations yield pressure coefficients for \(\Delta E_{e-e} + \Delta E_{e-i}\) lower than 0.6 meV/GPa. For electron concentrations close to that of our most heavily doped sample \((1.6 \times 10^{19} \text{ cm}^{-3}\), we find that \(d(\Delta E_{e-e} + \Delta E_{e-i})/dP \sim 2\) meV/GPa. Given that this value is still comparable to the experimental error of the pressure-dependent optical measurements, it can be assumed that band gap renormalization effects play a minor role in the results of Fig. 2. In contrast, in the ultra-heavily-doped regime \((n \sim 10^{20} \text{ cm}^{-3}\), we obtain pressure coefficients for the band gap renormalization shifts that are higher than 4 meV/GPa. Such values are expected to compensate for the reduced \(dE_{\text{abs}}/dP\) values predicted by the \(k-p\) calculations for high electron densities (Fig. 2). However, the \(k-p\) model is expected to fail in the ultra-heavily-doped range. Additional work would be desirable to ascertain the role of conduction-band filling and band gap renormalization on the high-pressure optical properties of ultra-heavily-doped w-InN.

B. Rocksalt InN

Rs-InN is an indirect semiconductor with a band gap energy of \(\sim 1\) eV.\(^{12}\) In this work, we perform a detailed study of the pressure dependence, up to 30 GPa, of the indirect band gap of rs-InN using a thick InN epilayer (5.7 \(\mu\)m). Figure 3 shows three absorption spectra obtained on the upstroke at 12.1, 15.3, and 17.4 GPa for this sample. The wurtzite-to-rocksalt phase transition is clearly observed as a change in the shape of the absorption edge with increasing pressure. At 15.3 GPa, the profile at higher photon-energy values of the spectrum still resembles that of the wurtzite phase. In contrast, from the absorption curve at 17.4 GPa, it can be concluded that the phase transition is complete. As discussed in Ref. 12, the pressure values at which the wurtzite-to-rocksalt phase transition is observed in InN by means of optical absorption measurements tend to be higher than those obtained with XRD or Raman-scattering measurements. This discrepancy may be attributed

![FIG. 3. (Color online) Optical absorption spectra at different hydrostatic pressures around the wurtzite-to-rocksalt transition of a 5.7-\(\mu\)m-thick InN epilayer with a free-electron concentration of \(5 \times 10^{17} \text{ cm}^{-3}\).](image-url)
to the presence of remaining, highly absorbing w-InN domains in the flakes around (or just above) the transition pressure.

High-pressure absorption measurements were obtained in the upstroke cycle up to 30 GPa and then in the downstroke cycle down to ambient pressure. Figure 4 shows the absorption spectra of rs-InN obtained in the downstroke cycle, from 30.2 GPa down to 4.4 GPa. The expected redshift of the absorption edge with decreasing pressure is observed. The absorption spectra of rs-InN obtained in the upstroke cycle ($P > 17.4$ GPa) yielded similar profiles and have not been included in the subsequent analysis. The characteristic shape of the indirect absorption edge is observed in the figure down to 4 GPa. Thus, a clear hysteresis effect is observed. As in Ref. 12 for the case of a much thinner epilayer, we find that for $P < 4$ GPa, the rocksalt-to-wurtzite backtransformation occurs (not shown).

The quadratic dependence of the low-energy tail of the absorption edge of rs-InN confirms the indirect nature of this semiconductor compound. In Fig. 5, we plotted the square root of the absorption coefficient of rs-InN for two pressure values (downstroke cycle). In both cases, a clear linear dependence arising from an indirect transition is observed. For a pressure of 13.4 GPa, close to the pressure at which the wurtzite-to-rocksalt transformation occurs, the low-energy tail can be assigned to an indirect band gap with an energy of 0.70 ± 0.05 eV. This value is lower than that previously measured in thinner epilayers (1 eV at 15.7 GPa, see Ref. 12). While in Ref. 12 the small thickness of the sample prevented the clear observation of the indirect absorption edge, since the transmittance was dominated by the allowed higher-energy direct transition at the Γ point, the present measurements provide a more accurate determination of the indirect band gap energy of rs-InN.

Previous theoretical works predicted a range of possible indirect band gap values for rs-InN from 0.5 to 1.9 eV. The present measurements indicate that the indirect band gap energy of rs-InN lies in the lower range of the theoretical calculations, i.e., in agreement with the results of Refs. 21 and 23. These two works predict that the lowest band gap of rs-InN corresponds to a $L - \Gamma$ transition.

From the spectra of Fig. 4, a pressure coefficient for the indirect band gap of rs-InN can be estimated from the shifts at constant absorption coefficient. We show in Fig. 6 the pressure dependence of the energy shift of the absorption edge at three values: 1100, 1500, and 2000 cm$^{-1}$. A pressure coefficient of 23 meV/GPa is extracted from a linear fit to the data of Fig. 6. This value, slightly lower than that of the direct band gap in the wurtzite phase (32 meV/GPa), allows us to obtain the volume deformation potential for the indirect transition in rs-InN. By using the bulk modulus of rs-InN ($B_0 = 170$ GPa$^3$), we obtain a value of $dE_G/d\ln V = −3.9$ eV, only slightly below the deformation potential of the direct fundamental band gap of w-InN.

IV. CONCLUSION

Conduction-band-filling yields reduced optical band gap pressure coefficients in w-InN with increasing carrier concentration. The experimental pressure coefficients in w-InN, measured with optical absorption experiments, are found to be higher than those obtained by PL measurements in previous works. A $k·p$ calculation allows us to reproduce the weakening of the experimentally determined band gap pressure coefficients with increasing electron density. We conclude that the best value for the band gap pressure coefficient in intrinsic w-InN is 32 meV/GPa. The wurtzite-to-rocksalt phase transformation is observed at ~15 GPa. Around the
transition pressure, a band gap of 0.7 eV is obtained for the rocksalt phase. From the high-pressure optical measurements, the pressure coefficient for the indirect band gap of rs-InN is obtained: 23 meV/GPa.

ACKNOWLEDGMENTS

This work was supported by the Spanish Ministry of Science and Innovation through Project No. MAT2010-16116.