# Improved determination of the $\mathbf{1}_0 - \mathbf{0}_0$ rotational frequency of $\mathbf{NH}_3\mathbf{D}^+$ from the high resolution spectrum of the $\nu_4$ infrared band

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# ABSTRACT

The high resolution spectrum of the  $\nu_4$  band of NH<sub>3</sub>D<sup>+</sup> has been measured by difference frequency IR laser spectroscopy in a multipass hollow cathode discharge cell. From the set of molecular constants obtained from the analysis of the spectrum, a value of  $262817 \pm 6$  MHz ( $\pm 3\sigma$ ) has been derived for the frequency of the  $1_0 - 0_0$  rotational transition. This value supports the assignment to NH<sub>3</sub>D<sup>+</sup> of lines at 262816.7 MHz recorded in radio astronomy observations in Orion-IRc2 and the cold prestellar core B1-bS.

Subject headings: Molecular data — Line: identification — ISM: molecules — methods: laboratory — techniques: spectroscopic

# 1. Introduction

The concentrations of ions in interstellar space are typically orders of magnitude lower than those of the most abundant neutral species (Petrie & Bohme 2007, Snow & Bierbaum 2008, Larsson et al. 2012) but, due to the fact that ion-molecule reactions are often barrier-less and have large rate coefficients, ions play a key role in the low-temperature gas phase chemistry of the interstellar medium (ISM) (Watson 1973, Herbst & Klemperer 1973, Herbst 2001). Many of the 20 cations detected up to date in the ISM (Petrie & Bohme 2007, Larsson et al 2012) are protonated derivatives of small molecules that can be formed in chains of proton transfer processes involving molecules with varying proton affinities (PA) (Burt et al. 1970, Carrasco et al. 2012a, Carrasco et al. 2013). The global initiator of these chains is assumed to be  $H_3^+$ , the most frequently produced ion in the ISM (Oka 2006), which is readily generated in the collisions of  $H_2$  molecules with  $H_2^+$  ions. Due to the low PA (422.3 kJ mol<sup>-1</sup>) of the hydrogen molecule (Burt et al. 1970, Hunter & Lias 1998),  $H_3^+$  has a high tendency to transfer a proton and return to  $H_2$ . Among the small molecules most common in the ISM (CO, N<sub>2</sub>, HCN, H<sub>2</sub>O, NH<sub>3</sub>, CH<sub>2</sub>O, CH<sub>4</sub>, CH<sub>3</sub>OH), ammonia has the highest proton affinity (PA=853 kJ mol<sup>-1</sup>) and consequently NH<sub>4</sub><sup>+</sup>, once formed, will be stable toward further reactions with the most abundant species. In fact, astrochemical models predict  $NH_4^+$  to become the dominant ion in some warm astronomical environments where  $\mathrm{NH}_3$  desorbs from interstellar grains and becomes available for gas phase ion-molecule chemistry (Rodgers & Charnley 2003, Harada et al. 2010, Aikawa et al. 2011). It should be noted that, in spite of the concentration enhancement provided by grain desorption,  $NH_3$ always represents a small fraction of the neutral species inventory. The dominance of  $NH_4^+$ in the ion distributions of laboratory plasmas containing just small fractions of NH<sub>3</sub> has also been experimentally demonstrated (Carrasco et al. 2011, Carrasco et al. 2013).

Interstellar  $NH_4^+$  is not limited to warm environments. It is also assumed to play a

key role in the low temperature gas-phase formation of ammonia in cold clouds (Nejad et al. 1990). In this case, the suggested route starts with the reaction between  $N^+$  and  $H_2$  to yield  $NH^+$  and proceeds through successive hydrogenation steps to the formation of  $NH_4^+$  that transforms into  $NH_3$  through dissociative recombination with electrons. The first step in this route is endoergic for para-hydrogen molecules in their ground state, but slightly exoergic for ortho-hydrogen, and Dislaire et al. (2012) have shown that realistic ortho/para ratios could explain the relative abundances of nitrogen hydrides observed in dark clouds. In general, the high gas-phase chemical stability of  $NH_4^+$  in the ISM, which is mostly destroyed just in collisions with electrons, suggests that it can build up to high concentrations in different astronomical environments and, given its paramount importance for nitrogen chemistry in space, it is a desired goal for astronomical searches. Unfortunately,  $NH_4^+$  is a spherical top molecule with no permanent electric dipole moment and thus unsuitable for radioastronomic observation. As far as we know, the ion has never been detected in the ISM. However, deuterated variants of  $NH_4^+$  do possess a permanent dipole moment and could, in principle, be observed. Variously deuterated ammonia molecules, likely related to deuterated ammonium, are observed in dense cores, where fractionation leads to an enhancement of the molecular deuterium content (Roueff et al. 2005) and, in particular, all deuterated isotopologues of NH<sub>3</sub> have been detected in the cold prestellar cloud B1-bS (Lis et al. 2002).

Spectroscopic data useful for astronomic observations are available for the monodeuterated ammonium ion. Specifically, a frequency of  $262807 \pm 9$  MHz  $(\pm 3\sigma)$  was predicted by Nakanaga & Amano (1986, hereafter N&A (1986)) for the  $1_0 - 0_0$  transition of NH<sub>3</sub>D<sup>+</sup>. This value was derived using the ground-state molecular constants obtained by those authors from their high resolution spectroscopic measurements of the  $\nu_4$  infrared band of the ion. Recent work by Cernicharo et al. (2013, accompanying letter) has established the presence of an emission line at 262816.7 MHz in Orion-IRc2 and in B1-bS. The frequency is approximately 10 MHz higher than that estimated by Nagaka and Amano for monodeuterated ammonium and thus exceeds slightly the  $3\sigma$  uncertainty of the spectroscopic value, strongly suggesting that the feature can correspond to this species. In the present work we have refined the previous spectroscopic measurements of N&A (1986) further constraining the frequency of the  $1_0 - 0_0$  transition and providing additional support for the assignment of the observed 262816.7 MHz emission feature to the presence of NH<sub>3</sub>D<sup>+</sup>.

#### 2. Experimental details

The experimental setup used in this work is similar to that described elsewhere (Tanarro et al. 1994a, 1994b). It consists of an IR difference-frequency laser spectrometer (Doménech 1990, Bermejo et al. 1989), and a hollow cathode discharge reactor refrigerated by room-temperature water, with multipass optics in a White cell configuration, similar to the design of Foster & McKellar (1984).

The IR radiation is generated by difference-frequency mixing, following the scheme of Pine (1974), of an Ar<sup>+</sup> laser and a tunable ring dye laser in a LiNbO<sub>3</sub> crystal. Tuning the dye laser, while keeping the Ar<sup>+</sup> laser frequency locked, tunes the IR frequency, which is the difference between that of the Ar<sup>+</sup> laser and that of the ring dye laser. In our experiment, the Ar<sup>+</sup> laser is frequency locked to a hyperfine transition of <sup>127</sup>I<sub>2</sub>, (a<sub>3</sub> component of the P(13) 43 – 0 transition, known with an accuracy ~ 0.1 MHz, (Quinn 2002)) and has a residual frequency jitter less than 1 MHz and long-term stability of the same order of magnitude. The wavelength of the ring dye laser (also frequency stabilized, with a residual jitter of ~ 3 MHz) is measured in just 1 ms at each data point of the spectrum by a high accuracy wavemeter based on Fizeau interferometers (High Finesse WSU10) with a manufacturer-stated absolute accuracy of better than 10 MHz (3 $\sigma$ ). The Ar<sup>+</sup> laser is

used to calibrate the wavemeter and thus insure its accuracy throughout the experiments. The linewidth of the IR beam is the combined linewidth of those of the visible lasers, i.e.  $\sim 3$  MHz. The internal coherence of the infrared frequency scale is limited by that of the wavemeter. From repeated measurements of N<sub>2</sub>O lines in the 3300 – 3400 cm<sup>-1</sup> region, and their comparison with the values in the HITRAN 2008 database (Rothman et al. 2009, Toth (2004)), we have verified a reproducibility and internal coherence of our IR frequency scale better than  $1.2 \times 10^{-4}$  cm<sup>-1</sup> (4 MHz) rms and a systematic offset of  $6 \times 10^{-4}$  cm<sup>-1</sup> (18 MHz), which is within the combined uncertainty of the wavemeter and the quoted uncertainty limits for those line frequencies in HITRAN ((1-10)×10<sup>-4</sup> cm<sup>-1</sup>, or 3 – 30 MHz).

The IR beam traverses the multipass cell 12 times, giving an effective absorption length of 9 meters inside the discharge. In order to improve the detection sensitivity, both the IR beam and the discharge are amplitude-modulated, at 14.2 and 5.5 kHz, respectively, and the IR signal is detected by an InSb detector connected to a dual-phase lock-in whose reference frequency is the sum of the other two (i.e. 19.7 kHz). In this way, only changes in the IR beam intensity, due to species whose concentration is modulated in the discharge, are detected. The three frequencies are derived from a common oscillator by appropriately chosen integer dividers (Domingo et al. 1994), therefore, insuring phase stability between the three of them. The detection time constant is 100 ms with 12 db/oct roll off. The ring dye laser scans at  $0.005 \text{ cm}^{-1}\text{s}^{-1}$  rate. Each line has been recorded 10 times and the results averaged in a grid spaced  $0.001 \text{ cm}^{-1}$ .

The discharge is modulated at 5.5 kHz through an audio amplifier, a step-up transformer and a circuit designed to avoid the transformer core saturation, since the hollow cathode discharge acts inherently as an electric rectifier. Typical discharge conditions are 200 mA and 400 V rms. The relatively high modulation frequency has been chosen to favor the detection of ionic species, whose lifecycles follow closely the on-off condition of

the discharge, and to minimize undesired absorption signals associated with much slower processes like concentration change of the neutral species caused by multistep wall reactions (Carrasco et al. 2012b, 2013). Nevertheless, we have observed spectral signatures from NH<sub>3</sub> due to a combination of population and Doppler width changes that occur with the small temperature change on the "on" periods of the discharge, similar to those observed in Tanarro et al. (1994a) for other stable species. Note that the kinetic temperature deduced from the observed Doppler widths of the ions is ~ 315 K, i.e. very near the temperature of the refrigerated cathode.

A 32 Pa (0.32 mbar) gas flowing mixture of  $NH_3$  (37%) +  $D_2$  (63%) is used in the discharge as plasma precursor. Gas flows, measured with rotameters at 5 × 10<sup>4</sup> Pa (500 mbar) absolute input pressure, were 15 ml/min and 30 ml/min for  $NH_3$  and  $D_2$ , respectively. In the hollow cathode discharges used, efficient atomic recycling at the metallic cathode wall (Jiménez-Redondo et al. 2011, Carrasco et al. 2011) leads to an extensive isotopic scrambling both in the neutrals and ions. Most of the initial  $NH_3$  is transformed into  $N_2$  and  $H_2$  and the pressure raises to ~ 46 Pa (~ 0.46 mbar). The mixture proportions, flow rate and pressure were empirically selected to maximize the  $NH_3D^+$  concentration.

Although the ion concentrations have not been directly measured in the present experiment, previous kinetic studies and Langmuir probe measurements by our group (Carrasco et al. 2011, Carrasco et al. 2013) on comparable hollow cathode discharges of  $H_2/N_2$  mixtures, indicate that the ion distributions in our cell should be dominated by  $NH_4^+$ , with smaller concentrations of  $N_2H^+$  and  $H_3^+$  (and their deuterated variants) and that the total ion densities should be of the order of  $\sim (1-5) \times 10^{10}$  cm<sup>-3</sup>, with electron temperatures of  $\sim 3.0 \pm 0.5$  eV. These density values are also consistent with estimates made from the measured cathode current and glow region dimensions using Bohm's velocity (Lieberman & Lichtenberg 1994). The concentrations of the main individual ions and, in particular, of  $NH_3D^+$  are estimated to be in the  $10^9 - 10^{10}$  cm<sup>-3</sup> range.

It must be noted that this set-up is very similar to the one used by N&A (1986). The main differences between them are: the IR frequency measuring system (a high accuracy wavemeter for the dye laser in our case, and calibration with N<sub>2</sub>O IR absorption lines with  $1 \times 10^{-3}$  cm<sup>-1</sup> (30 MHz) accuracy in the previous work), the detection scheme at the sum frequency vs. detection at the discharge frequency, the different frequencies of the discharge (5.5 kHz vs. 17 kHz), the rather different proportion of NH<sub>3</sub> and D<sub>2</sub> in the gas mixture (~ 1 : 2 in our case vs. 1:10 in the previous work), the different absorption path lengths (9 m in this work vs. 20 m in the previous one) and the IR power available (~ 1  $\mu$ W in this work vs. ~ 10  $\mu$ W in the previous one). We would like to emphasize that our experiment has been guided and facilitated extensively by the previous study of N&A (1986). The major experimental improvement of the present study is due to the availability of a more precise frequency scale and a more favorable ratio of precursors in the discharge.

## 3. Results and discussion

We have recorded 114 lines between 3268.4 and 3414.7 cm<sup>-1</sup>. Not all the spectral interval has been scanned. Instead, we have chosen to scan selected regions around the line frequencies calculated with the constants provided by N&A (1986). In each region, 10 recordings have been made and averaged, in order to improve the signal to noise ratio. From the repeatability of the shape of the most intense lines, and from the fact that no broadening is observed in the averages, we are assured that the frequency scale derived from the wavemeter is highly reproducible. The predictions, new assignments and fits have been made with the help of the PGOPHER program (Western 2010). A ~ 1 cm<sup>-1</sup> wide region of the spectrum in the central part of the band is shown in Figure 1, which can be compared with Figure 1 of N&A (1986). The more prominent features are due to NH<sup>4</sup><sub>4</sub>, which we have

identified throughout the spectrum with the measurements and predictions of Schäfer et al. (1984). Our more favorable intensity ratio between  $NH_3D^+$  and  $NH_4^+$  signals as compared with those of N&A (1986) is worth noting. Figure 2 shows some more examples of more isolated lines of  $NH_3D^+$  in the *P*- and *R*- regions.

Each averaged line has been fit to a Gaussian function, to derive its line center. Standard deviations of the center frequency derived from these fits are  $(1 - 4) \times 10^{-4}$  cm<sup>-1</sup> (3 - 12 MHz). The line center frequencies have been fit to the same Hamiltonian used in the work of N&A (1986), with the only exception of the sign of the  $q_+$  (rotational *l*-doubling) parameter, since PGOPHER uses the opposite sign convention for it in its matrix elements. For completeness, we give here the expressions used for the energy levels, which are common for a prolate symmetric-top. For the nondegenerate ground-state, ignoring spin-rotation effects:

$$E''(J, K) =$$

$$B''J(J+1) + (A'' - B'')K^{2}$$

$$- D''_{J}J^{2}(J+1)^{2} - D''_{JK}J(J+1)K^{2} - D''_{K}K^{4}$$
(1)

+ higher order centrifugal distortion terms,

and for the degenerate  $v_4 = 1$  state

$$E'(J,k) = \nu_0 + B'J(J+1) + (A' - B')k^2 + (-2A'\zeta + \eta_J J^2 + \eta_K k^2)lk$$
(2)  
- D'\_J J^2 (J+1)^2 - D'\_{JK} J(J+1)k^2 - D\_K k^4   
+ higher order centrifugal distortion terms,

with the off-diagonal matrix elements, responsible for the rotational *l*-doubling,

$$\langle J, k+2, l+1 | H | J, k, l-1 \rangle = \frac{1}{2} q_+ [(J(J+1) - k(k-1))(J(J+1) - k(k+1))]^{\frac{1}{2}}$$

$$(3)$$

A and B are the rotational constants perpendicular and parallel, respectively, to the symmetry axis. The D constants account for the centrifugal distortion effects. J and K are the usual rotational quantum numbers, with K = |k|. Recall that Coriolis interaction splits  $k \neq 0$  levels in the degenerate vibrational state into +l and -l levels (involving the parameters  $\zeta$ ,  $\eta_J$  and  $\eta_K$  above) and that the ( $\Delta k = \pm 2, \Delta l = \pm 2$ ) interaction splits the  $k = l = \pm 1$  levels into pairs (involving the  $q_+$  parameter). For a more detailed description of the vibration-rotation Hamiltonian and the matrix elements used here the reader is referred to Papousek & Aliev (1982) and PGOPHER's documentation (Western 2010), respectively.

Finally, 76 lines have been fitted, 15 more than in the N&A (1986) work. The lines that have not been included in the fit either show interference from  $NH_4^+$  or  $NH_3$  features, have very poor signal to noise ratio, or show abnormally high linewidth (indicating a possible overlap). Besides, we have restricted ourselves mostly to lines with  $J, K \leq 7$ , in order to avoid using sextic and higher centrifugal distortion constants. Restriction to these quantum numbers, even at the expense of reducing the number of observations included in the fit, provides a better description of the low lying levels that we pursue, avoiding the correlations between parameters that appear as the number of degrees of freedom is increased without a much larger number of observations.

Table 1 shows the observed frequencies, observed minus calculated residuals and the assignments of the fitted lines. The standard deviation of the fit is  $5 \times 10^{-4}$  cm<sup>-1</sup>. Table 2 shows the resulting constants and their standard deviations  $(1\sigma)$  derived from the fit. Since  $\nu_4$  is a perpendicular band of a symmetric top,  $A'', A', D''_K$ ,  $D'_K$  and  $\zeta$  cannot be independently determined from the observations, so A'' and  $D''_K$  have been constrained to the same values as in the N&A (1986) paper. As indicated there, this choice of parameters affects  $\nu_0$ ,  $\zeta$ , A' and  $D'_K$  values, while the rest remain unaffected. Specifically, the frequency of the  $J_K = 1_0 - 0_0$  pure rotational transition, namely 2B'' - 4D'', does not depend on any of these parameters, so our estimation is not influenced by the constraints. Table 2 also shows the results from N&A (1986), showing that the most significant changes are in the *B* and *D* rotational constants. From the *B''* and  $D''_J$  values, we obtain a frequency for the  $1_0 - 0_0$  transition of 262816.8 MHz, in good agreement with the observation of Cernicharo et al. (2013, accompanying letter). We are aware that the near perfect match is probably fortuitous, given the precision of the individual IR frequencies and the statistical uncertainty of the parameters derived from the fit.

In order to summarize, based on our observations and the analysis described above, we propose a value of  $262817 \pm 6$  MHz  $(\pm 3\sigma)$  for the frequency of the  $1_0 - 0_0$  pure rotational transition of NH<sub>3</sub>D<sup>+</sup>. Our IR measurements improve upon those of N&A (1986) thanks to a more precise frequency scale and a larger number of observed lines. This frequency is in good agreement with that of the feature detected in Orion-IRc2 and B1-bS (Cernicharo el al. 2013, accompanying letter), thus supporting the identification of NH<sub>3</sub>D<sup>+</sup> in the ISM.

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### REFERENCES

- Aikawa, Y., Furuya, K., Wakelam, V. et al. 2011, in IAU Symp. 280, The Molecular Universe, ed. J. Cernicharo & R. Bachiller, (Cambridge: Cambridge University Press), 33
- Bermejo, D., Domenech, J. L., Cancio, P., Santos, J., Escribano, R., 1989, in Proc. of the IX Conf. on Laser Spectroscopy, Laser Spectroscopy IX, ed. Feld, M.S., Thomas J.E. & Mooradian, A. (San Diego: Academic Press),126
- Burt, J. A., Dunn, J. L., McEwan, M. J. et al. 1970, J. Chem. Phys. 52, 6062
- Carrasco, E., Jiménez-Redondo, M., Tanarro, I., Herrero, V. J., 2011, Phys. Chem. Chem. Phys., 13, 19561
- Carrasco, E., Herrero, V. J., Tanarro, I., 2012a, J. Phys. D: Appl. Phys., 45, 305201
- Carrasco, E., Jiménez-Redondo, M., Tanarro, I., Herrero, V. J., 2012b, PPCF 54, 124019
- Carrasco, E., Tanarro, I., Herrero, V. J., Cernicharo, J., 2013, Phys. Chem. Chem. Phys., 15, 1699.
- Cernicharo, J., Tercero, B., Fuente. A, Domenech, J. L., Cueto, M. et al. 2013, ApJL, (accompanying letter)
- Dislaire, V., Hily-Blant, P., Faure, A., et al., 2012, A&A 537, A20
- Doménech, J.L. 1990, Espectroscopía infrarroja de muy alta resolución. PhD Thesis, Madrid: Universidad Complutense, http://hdl.handle.net/10261/76991
- Domingo, C., Tanarro, I., Sanz, M. M., et al. 1994, Proceedings of SPIE, 2124, 227

- Foster, S. C., McKellar, A. R. W. 1984, J. Chem. Phys. 81, 3424
- Harada, N., Herbst, E., & Wakelam, V. 2010, ApJ, 721, 1570
- Herbst, E. 2001, Chem. Soc. Rev. 30, 168
- Herbst, E. & Klemperer, W. 1973, ApJ, 185, 505
- Hunter, E. P. L.& Lias, S. G. 1998, J. Phys. Chem. Ref. Data, 27, 413
- Jiménez-Redondo, M., Carrasco, E., Herrero, V. J. & Tanarro I. 2011, Phys. Chem. Chem. Phys. 13, 9655
- Larsson, M., Geppert, W. D. & Nyman G., 2012, Rep. Prog. Phys. 75, 066901
- Lieberman, M. A. & Lichtenberg, A. J. 1994, Principles of plasma discharges and materials processing (New York: Wiley & Sons)
- Lis, D. C., Roueff, E., Gerin, M. et al. 2002, ApJ 571, L55
- Nakanaga, T., Amano, T., 1986, Can. J. Phys. 64, 1356
- Nejad, L. A. M., Willams, D. A. & Charnley, S. B., 1990, MNRAS, 246, 183
- Oka, T. 2006, PNAS, 103, 12235
- Papoušek, D. & Aliev, M.R. 1982, Molecular Vibrational/Rotational Spectra, Amsterdam: Elsevier Scientific.
- Pine, A. S. 1074, JOSA, 64, 1683
- Petrie, S. & Bohme, D. K. 2007, Mass Spectrom. Rev. 26, 258
- Schäfer, E., Saykally, R. J. & Robiette, A. G. 1984, JChPh 80, 3969
- Snow, T.P. & Bierbaum, V. 2008, ARAC, 1, 229

- Rodgers, S.D. & Charnley, S. S. 2003, ApJ, 585, 355
- Roueff, E., Lis, D. C., van der Tak, F. F. S., et al. 2005, A&A, 438, 585
- Western, C. M. (2010), PGOPHER, a Program for Simulating Rotational Structure (2010, v 7.1.108). University of Bristol, http://pgopher.chm.bris.ac.uk
- Quinn, T. J., 2003, Metrologia 40, 103
- Rothman L. S., Jacquemart, D., Barbè, A. et al. 2009, J. Quant. Spectrosc. Radiat. Transfer, 110, 533
- Tanarro, I., Sanz, M. M., Bermejo, D., Domingo, C., Santos, J., 1994a, J. Chem. Phys., 100, 238
- Tanarro, I., Sanz, M. M., Domingo, C., et al. 1994b, J. Phys. Chem., 98, 5862
- Toth, R.A., 2004,

http://mark4sun.jpl.nasa.gov/n2o.html

Watson, W. D. 1973, ApJ 183, L17

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$\nu_{\rm obs}/{\rm cm}^{-1}$	(o-c) <sup>a</sup>	J'	K'	l	J''	K''
3275.00762	1.2	5	5	-1	6	6
3277.36239	6.3	5	4	-1	6	5
3279.75397	4.3	6	1	1	7	0
3281.97669	1.2	5	2	-1	6	3
3284.24462	-0.6	5	1	-1	6	2
3286.24996	-7.2	4	4	-1	5	5
3286.48992	-2.0	5	0		6	1
3288.58604	4.2	4	3	-1	5	4
3288.71980	3.2	5	1	1	6	0
3290.89042	-1.4	4	2	-1	5	3
3293.16846	-3.7	4	1	-1	5	2
3297.46387	0.7	3	3	-1	4	4
3299.77847	-0.8	3	2	-1	4	3
3302.06568	4.4	3	1	-1	4	2
3306.56586	6.1	3	1	1	4	0
3310.93202	2.8	2	1	-1	3	2
3313.19858	2.9	2	0		3	1
3315.44070	1.7	2	1	1	3	0
3319.76669	3.7	1	1	-1	2	2
3322.03737	5.4	1	0		2	1
3330.84074	6.5	0	0		1	1
3334.30357	-7.6	6	2	-1	6	3

Table 1. Fitted lines, residuals after the fit and the quantum numbers assignment.

Table 1—Continued

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$\nu_{\rm obs}/{\rm cm}^{-1}$	(o-c) <sup>a</sup>	J'	K'	l	J''	K''
0007	( )					
3334.68004	-9.7	4	2	-1	4	3
3334.81962	-1.3	3	2	-1	3	3
3336.32317	5.3	7	1	-1	7	2
3336.57102	2.0	6	1	-1	6	2
3336.96581	-8.1	4	1	-1	4	2
3337.11283	5.2	3	1	-1	3	2
3338.81264	3.3	6	0		6	1
3339.03585	-7.1	5	0		5	1
3339.22520	1.5	4	0		4	1
3339.37658	-3.1	3	0		3	1
3339.49136	-0.3	2	0		2	1
3339.56780	-2.2	1	0		1	1
3341.02311	-0.8	6	1	1	6	0
3341.25759	0.8	5	1	1	5	0
3341.45410	-2.9	4	1	1	4	0
3341.61294	-0.1	3	1	1	3	0
3341.73208	-4.0	2	1	1	2	0
3342.63625	-6.3	8	2	1	8	1
3342.94920	0.8	7	2	1	7	1
3343.22602	6.0	6	2	1	6	1
3343.46451	-0.2	5	2	1	5	1
3343.66511	-3.0	4	2	1	4	1

Table 1—Continued

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$\nu_{\rm obs}/{\rm cm}^{-1}$	(o-c) <sup>a</sup>	J'	K'	l	J''	K''
3343.82666	-5.2	3	2	1	3	1
3345.11471	3.2	7	3	1	7	2
3345.39715	-1.2	6	3	1	6	2
3345.64164	-4.0	5	3	1	5	2
3345.84661	-10.1	4	3	1	4	2
3346.01221	-9.4	3	3	1	3	2
3347.25607	-5.2	7	4	1	7	3
3347.54483	1.6	6	4	1	6	3
3347.79345	-4.4	5	4	1	5	3
3348.00364	4.6	4	4	1	4	3
3350.57916	-6.1	1	1	1	0	0
3359.26698	6.9	2	1	1	1	0
3361.47942	-8.8	2	2	1	1	1
3367.91091	-0.9	3	1	1	2	0
3370.12020	-0.8	3	2	1	2	1
3372.30329	-3.2	3	3	1	2	2
3376.51343	4.9	4	1	1	3	0
3378.71679	7.8	4	2	1	3	1
3380.89518	4.8	4	3	1	3	2
3383.04468	3.0	4	4	1	3	3
3385.07123	-1.3	5	1	1	4	0
3387.26751	7.7	5	2	1	4	1

, 1			<b>T Z</b>			<b>T</b> 5/1
$\nu_{\rm obs}/{\rm cm}^{-1}$	(o-c) <sup>a</sup>	J'	<i>K'</i>	l	<i>J</i> ″	K''
3389.44028	4.5	5	3	1	4	2
3391.58446	1.2	5	4	1	4	3
3393.58543	-2.2	6	1	1	5	0
3393.69878	6.8	5	5	1	4	4
3400.07709	0.8	6	4	1	5	3
3402.05462	-7.8	7	1	1	6	0
3408.26843	5.6	8	0		7	1
3408.52168	-3.1	7	4	1	6	3
3410.62517	5.8	7	5	1	6	4
3414.72838	-2.9	7	7	1	6	6

Table 1—Continued

<sup>a</sup>(o-c)=( $\nu_{\rm obs} - \nu_{\rm calc}$ )/10<sup>-4</sup> cm<sup>-1</sup>

Constants $/cm^{-1}$	This work	N&A (1986)		
<i>A</i> ″	$5.852^{a}$	$5.852^{\rm a}$		
B''	4.3834351(294)	4.38327(5)		
$D_J''$	$6.1363(373) \times 10^{-5}$	$5.87(9) \times 10^{-5}$		
$D_{JK}^{\prime\prime}$	$1.4689(293) \times 10^{-4}$	$1.52(6) \times 10^{-4}$		
$D_K''$	$0.0^{a}$	$0.0^{\mathrm{a}}$		
$ u_0$	3341.07498(17)	3341.0764(3)		
A'	5.818834(37)	5.81871(9)		
B'	4.3640729(278)	4.36391(5)		
$D'_J$	$5.4024(339) \times 10^{-5}$	$5.13(10) \times 10^{-5}$		
$D'_{JK}$	$9.705(296)\!\times\!10^{-5}$	$1.02(7) \times 10^{-4}$		
$D'_K$	$3.801(91) \times 10^{-5}$	$3.1(3) \times 10^{-5}$		
$\zeta$	0.0582020(76)	$0.058191(14)^{b}$		
$\eta_J$	$-4.2581(686)\!\times\!10^{-4}$	$-4.23(13) \times 10^{-4}$		
$\eta_K$	$1.744(74) \times 10^{-4}$	$1.76(18) \times 10^{-4}$		
$q_+$	$-3.393(98) \times 10^{-4c}$	$2.93(19) \times 10^{-4}$		

Table 2. Constants derived from the fit

<sup>a</sup>Constrained in the fit

<sup>b</sup>Calculated from the values of A' and A' $\zeta$  given

in N&A (1986)

<sup>c</sup>Sign convention is opposite to that of N&A (1986)

Note. — Numbers in parentheses are one standard deviation in units of the last quoted digit, as derived from the fit. For this work we give all the significant digits necessary to reproduce the calculated line frequency values.

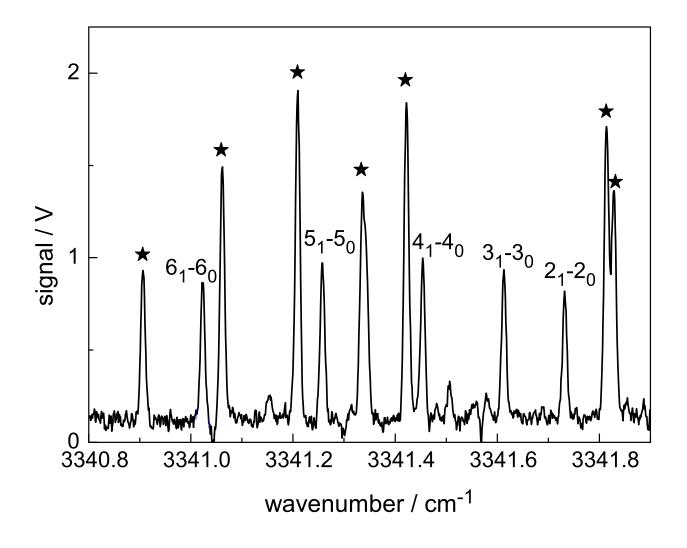


Fig. 1.— Portion of the  $\nu_4$  band of NH<sub>3</sub>D<sup>+</sup> near the band center. The labeled lines belong to the  $(J, K' = 1) \leftarrow (J, K'' = 0)$  progression  $({}^{r}Q_0(J)$  in branch notation), and are the same as those shown in Figure 1 of N&A (1986). Lines marked with an asterisk belong to NH<sub>4</sub><sup>+</sup>.

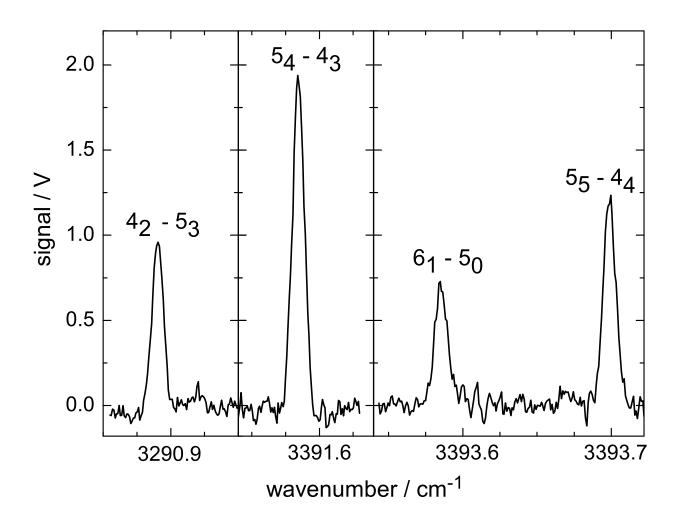


Fig. 2.— Additional examples of  $\nu_4$  lines recorded in this work. One horizontal division is  $0.025 \text{ cm}^{-1}$ .