The low temperature rotational relaxation of N$_2$ studied with resonance enhanced multiphoton ionization.

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Abstract

The rotational relaxation of molecular nitrogen has been investigated down to temperatures of about 5K with a combination of resonance-enhanced multiphoton ionization and supersonic beam time of flight techniques. The average rotational relaxation cross section obtained shows a maximum value of 50-60 Å$^2$ at 20-30 K. For lower temperatures this cross section decreases and reaches a value smaller than 30 Å$^2$ at T ≈ 5 K. For temperatures above 30 K, the cross section decreases slowly as the temperature grows and converges approximately to the determinations from other non-jet techniques and theoretical estimates available for T > 80 K. The results are compared to previous measurements from other groups using different methods and general good agreement is found. However, we observe a significant discrepancy with some of the data from electron beam induced fluorescence that yield much larger cross sections for temperatures lower than 30 K

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1. Introduction

The rotational relaxation of molecular nitrogen has been studied over a wide temperature range with different experimental techniques including shock waves, thermal transpiration, ultrasonic methods, broadening coefficients of spectral lines and various kinds of spectroscopic measurements performed on free jets (see, for instance, refs 1-9). Experimental data below \( \approx 80 \) K have been derived exclusively from free jets and molecular beam experiments.\(^7,^9,^12\) Theoretical treatments of varying complexity combining the gas dynamics of the supersonic flow with the kinetics of molecular energy transfer have been developed for the study of free jets,\(^8,^{13-19}\) but the lack of a precise knowledge of the flow field and of reliable data on the state-to-state energy transfer kinetics has precluded a rigorous comparison of theory and experiment. Ultimate progress in the field will certainly require more detailed calculations and thorough measurements of the local jet parameters with good spatial resolution.\(^20,^21\)

Theoretical values of the cross sections for \( \text{N}_2 \) rotationally inelastic collisions based on a direct solution of the three dimensional (3D) equations of motion with a realistic intermolecular potential have been obtained using the method of quasiclassical trajectories (QCT),\(^22-25\) but are restricted up to date to temperatures above 100 K. For lower temperatures, theoretical estimates have been worked out with semiempirical models developed mostly from higher temperature data (see refs 26-29 and references therein). Given the existing difficulties for the application of rigorous theoretical treatments one must resort in general to very simple models involving drastic approximations, in order to derive relaxation data from the measurements. In most cases the average rotational energy, characterized by a local rotational temperature, \( T_r \), is assumed to be coupled to the translational temperature of the jet through a linear relaxation equation and the actual degree of coupling between rotation and translation is described by an effective relaxation cross section, \( \sigma_r \), or by other suitable parameter (relaxation time, \( \tau_r \), rotational collision number, \( z_r \)) related to \( \sigma_r \).
Most experimental studies of \( \text{N}_2 \) rotational relaxation in supersonic free jets are based on the measurement of rotational temperatures using either Raman techniques or the electron-beam induced fluorescence (EIF) method. Electron-beam induced fluorescence has a high sensitivity and EIF measurements have been reported both along the axis of nitrogen free jets\(^{5,7,30-32} \) and in the molecular beams extracted from them, at the end of the expansion.\(^{10,11} \) However, the derivation of ground state rotational populations from the EIF data is not trivial and can often be controversial (see, for instance, the discussion in refs 8, 33 and in the references therein). In fact, the cross sections derived with the EIF method by different authors exhibit occasionally noteworthy discrepancies. For the \( \approx 10-50 \) K temperature range, the reported \( \sigma \) values\(^{5,17} \) can decrease from 200 to 40 \( \text{Å}^2 \) or have an average effective value of \( \approx 14 \text{Å}^2 \),\(^{10,11} \) depending, mainly on the criteria followed for the data analysis.

Raman techniques provide a very direct sampling of the rovibrational state populations in the ground electronic state, but due to their comparatively low sensitivity they cannot be easily applied to the measurement of rotational temperatures at the end of the expansion or in very low density free jets, which are precisely the conditions for which the breakdown of equilibrium between translation and rotation is more clear. Although, in principle, the derivation of \( T_r \) from Raman measurements is nearly straightforward, significant discrepancies in the reported relaxation data can also be found in the literature. The \( \sigma \) inferred by the rotational collision numbers reported in the coherent antistokes Raman spectroscopy (CARS) experiment of ref 12 decrease from 200 to 80 \( \text{Å}^2 \) in the temperature interval 15-40 K, whereas those from the Stimulated Raman Spectroscopy (SRS) measurements of reference 9 vary from 50 to 30 \( \text{Å}^2 \) over the same temperature range.

In an attempt to clarify the discrepancies on the low temperature rotational relaxation of \( \text{N}_2 \) we have used a different spectroscopic technique, namely resonance-enhanced multiphoton ionization (REMPI), for the measurement of rotational temperatures. This method was applied by Mazely and Smith \(^{34} \) for the measurement of rotational temperatures along the axis of a free jet of nitrogen and has been applied more recently\(^{35} \) to studies of relaxation in binary mixtures. Taking advantage of the high
sensitivity of this technique we have used it for the determination of the terminal rotational temperatures in the molecular beams skimmed from a large set of nitrogen free jets. In addition to the $T_r$ measurements, terminal flow velocities and translational temperatures have been determined from time of flight (TOF) measurements. In this way, the end of the expansion and the breakdown of equilibrium between translation and rotation are sampled over a wide range of conditions. The validity of simple jet models is analyzed and the rotational relaxation cross sections obtained are discussed and compared to previous works.

The most relevant aspects of the experimental setup used in the present investigation are described in Section 2. The experimental results and their analysis are presented and discussed in detail in Section 3 and summarized in Section 4, where final conclusions are drawn.

2. Experimental

Free jets of pure nitrogen were formed by expanding the gas from a commercial solenoid driven pulsed valve. The source pressures, $p_o$, ranged from $\approx 10$ to 2500 mbar and the pulsed valve was kept at room temperature ($T_o=296$ K) through all the measurements. The aperture time gate and voltage of the solenoid valve were set to generate nearly square gas pulses of 1 ms duration that were monitored with a fast ionization gauge. The TOF and REMPI measurements were performed on the central part of the gas pulses (quasi steady state) and special care was paid to the determination of the effective nozzle diameter, $d_{eff}$, from measurements of the gas flow to the expansion chamber$^{36}$. The $d_{eff}$ values were found to be $\approx 0.4$ mm ($\pm 10\%$) as compared to the nominal diameter of 0.5 mm. The gas pulses were expanded into a 50 l chamber pumped by a 2000 l s$^{-1}$ oil diffusion pump and the axial part of the expanding gas was collimated with a skimmer; the resulting molecular beams were then introduced into the REMPI or TOF analysis systems.

The set-up for the REMPI measurements is shown schematically in Figure 1. The skimmer used for the connection between the expansion and the REMPI detection
chamber is a commercial one of aerodynamic type (Beam Dynamics) with an approximate hyperbolic profile and a very thin wall ($\approx 100$ $\mu$m at the tip) having a 0.5 mm inner diameter. For the conditions of the present experiment, with mostly not too strong expansions and relatively large nozzle-skimmer distances, no significant skimmer interference is expected. Nevertheless, REMPI spectra for the largest values of $p_d^2d_{eff}$ were also recorded for various nozzle skimmer distances in the 3.5-5.5 cm range and no appreciable differences were observed. The source-skimmer distance was finally chosen within 4.0-5.5 cm at each working pressure, in order to optimize the beam intensity in the detection chamber versus the effusive flow of background gas from the expansion chamber through the skimmer orifice. The detection chamber for the REMPI experiments was pumped by a 56 l/s turbomolecular pump. Typical pressures in the expansion and detection chambers during the experiments were $10^{-5}$-$10^{-4}$ and $10^{-6}$ mbar, respectively. Valve and laser were synchronized to a repetition rate of 10 Hz. The ionization UV radiation was focused with a 25 cm focal length lens in the beam axis, 21 cm downstream from the skimmer. The laser shot was delayed with respect to the pulsed valve in order to interact with the $N_2$ molecules 0.3 ms after the beginning of the 1 ms long plateau of the gas pulse. No changes in the spectra were observed along the plateau except within 0.1 ms from the edges.

$N_2$ is detected in a quantum state specific manner by 2+2 REMPI via two photon resonant excitation to the $(1,0)$ vibrational band of the $a^1\Pi_g < -$ $X^1\Sigma_g^+$ transition. The same laser pulse used to excite the initial two-photon transition also ionizes the excited molecule. The required tunable UV radiation at 283-285 nm was generated by frequency doubling of the output of a Nd:YAG-pumped dye laser (Continuum NY81-20/ND60). The dye laser was operated with a mixture of rhodamine 590 and 610 optimized to provide a flat output power between 560 and 578 nm. The UV laser pulses are linearly polarized and have time and frequency widths of 6 ns and 0.1 cm$^{-1}$ (3 GHz), respectively. The power dependence of the REMPI signal was measured to be quadratic for pulse energies in the 1-3 mJ range. The experiments were run with 2 mJ/pulse and the measured ion intensities were corrected with the square of the laser energy at each wavelength, as given from the output of a fast photodiode recorded simultaneously to the ion signal. The laser focus (ca. 0.01 mm$^3$) intersected the axis of the supersonic
molecular beam at the midpoint between the repeller and the extractor plates which were at a distance of 10 mm from each other and were biased to \( V_0 = 1300 \text{V} \) and \( V_1 = 1050 \text{V} \), respectively. The extractor plate is followed downstream towards the detector by three additional parallel plates with voltages dropping gradually to ground. The \( \text{N}_2^+ \) photoions are accelerated by the system of plates into a 21 cm long field-free region towards a microchannel plate (Hamamatsu F2225-21S, diameter 42 mm). The time-dependent ion signal was recorded after amplification in a digital oscilloscope (Tektronix TDS524A) interfaced to a personal computer. The full width at half maximum (FWHM) of the temporal profile of the \( \text{N}_2^+ \) peak was 10 ns and the oscilloscope was operated at 1 ns resolution.

The arrangement for the TOF measurements of the \( \text{N}_2 \) molecules, has been described elsewhere\(^{9,36} \) and only the most relevant details will be given here. It consists of three interconnected vacuum chambers. The beam source is located in the first of these chambers; the second chamber houses a mechanical chopper and provides for differential pumping and the third one houses the quadrupole mass spectrometer (QMS) used for detection and mass discrimination. The nozzle-skimmer distance was usually \( \approx 4.5 \text{ cm} \) and the pulse frequency of the valve was made slow enough as to keep the average background pressure in the \( 10^{-4} - 10^{-5} \text{ mbar} \) range, in order to avoid attenuation of the beam. Two different skimmers were used in the measurements, the same aerodynamic skimmer used in the REMPI measurements for source pressures between \( \approx 200 \) and \( 2500 \text{ mbar} \) and a conical one with a 1.8 mm diameter for the whole range of source pressures investigated (10-2500 mbar). This second skimmer was necessary in order to improve the signal to noise ratio in the TOF spectra of the beams coming from the weakest expansions. As indicated above, for the conditions of the present experiment no significant skimmer effects are expected and, in fact, in the range of \( p_{\text{d} \text{eff}} \) values studied with both skimmers no appreciable differences were found in the velocity distributions derived from the measurements. In addition, TOF spectra for a fixed \( p_{\text{d} \text{eff}} \) were also recorded at different nozzle-skimmer distances between \( \approx 3.5 \) and \( 5.5 \text{ cm} \) and again, no significant differences were detected in the time of arrival distributions even for the highest source pressures used. In the chopper chamber, beyond the skimmer, the pressure was lower than \( 5 \times 10^{-6} \text{ mbar} \). The geometric gate function of the mechanical
chopper used for the modulation of the gas pulses could be well approximated by a
gaussian with a FWHM of 31 and 22 μs for the larger and smaller skimmer, respectively.
The molecules selected by the chopper were detected in the third chamber with the
quadrupole mass spectrometer under background pressure always in the 10⁻⁷ mbar range.

For the conditions of this experiment (T₀ = 296 K, d_eff ≈ 0.4 cm , p₀d_eff ≤ 100
mbar cm), N₂ aggregation processes are expected to be negligible and in fact no nitrogen
dimers or higher aggregates were detectable with the QMS. The probability of dimer
formation depends on the frequency of three body collisions and should scale
approximately with p₀²d_eff. In ref 9, where the same source conditions and experimental
set-up were used for the TOF measurements, the onset of dimerization, estimated as the
point where the QMS signal corresponding to the mass of the dimer-ion is 0.5% of that
of the monomer-ion, was found at p₀d_eff ≈ 150 mbar cm, which corresponds to a value of
p₀²d_eff larger by a factor of two than that of the strongest expansions of the present
work.

3. Results and discussion

The terminal rotational temperatures of the different N₂ expansions studied were
determined from the simulation of the molecular beam REMPI spectra. The intensity of
each rotational line in the (2+2) REMPI spectrum is given by:

\[ I_{N',N''} = F \frac{S_{N',N''}}{2N''+1} P_{N''} \]  

(1)

where S_{N',N''} are the two-photon line strength factors for the N'← N'' rotational
transitions of the a¹Π_g(v=1) ← X¹Σ_g⁺(v=0) band as given in Table I, 37 and F is a global
(i.e., independent of N' and N'') normalization factor which accounts for the vibrational
and electronic parts of the two-photon absorption probability and for the absolute density
of molecules in the ionization region. P_{N''} represents the relative population of each
rotational level N'' of the N₂ molecules. The T_{r,N''} were obtained from a linear least
square fit of the measured REMPI spectra. The T_{r,N''} values were then derived from the
Boltzmann plots of the rotational populations. Within the error of the measurements, no significant deviations from Boltzmann distributions were obtained even for the highest $P_{N''}$ states. In particular, the same temperature fits correctly the population of the ortho (even $N''$) and para (odd $N''$) nitrogen species. These were treated as independent systems with spin-degeneracy weights 2:1, i.e., it is assumed that the room temperature ortho/para ratio in the source remains "frozen" during the supersonic expansion. Furthermore, it must be remarked that the angular momentum of the $N_2$ molecules in the beam was assumed to be isotropically distributed in space, since no appreciable changes due to possible alignment effects were observed in REMPI measurements performed with different relative orientations of the laser polarization and the flow axis of the molecular beam.

The energies of the individual rotational levels $E_r$ were calculated from a Dunham-type expansion with the coefficients given by Kompa and coworkers, who concluded that both the ground state $X^1 \Sigma_g^+ (v=0)$ and the excited state $a^1 \Pi_u (v=1)$ can be considered to be essentially free from perturbations due to predissociation and $\Lambda$-type doubling for rotational levels up to $N = 35$. Each rotational transition in the measured REMPI spectra was simulated with a peak of Lorentzian shape with a best-fit full width at half maximum (FWHM) of 0.12 cm$^{-1}$. The whole spectrum, once calculated, was convoluted with a Gaussian function (FWHM 0.10 cm$^{-1}$) to account for the instrumental contribution to the measured linewidth. The assignment of the observed rotational lines is given in detail in Figure 2 where the simulation of a room temperature bulb spectrum is shown for reference.

Figure 3 shows three typical REMPI spectra recorded under different expanding conditions for the molecular beam. The simulated spectra obtained in each case with the best fit rotational temperature $T_r$ are also shown for comparison. As can be seen in the figures, the intensities of the peaks associated with the O, P, Q, R and S rotational branches constitute a sensitive probe for the rotational temperature of the $N_2$ molecules in the supersonic molecular beam. The intense rotational cooling attained in the strongest expansions is apparent in this figure. At large source stagnation pressures, $P_o > 1.5$ bar ($P_o \Delta_{eff} > 60$ mbar cm), the measured spectra are dominated by the S(0) and S(1)
transitions with a smaller contribution from the S(2), Q(1) and P(2) transitions (see upper panel of Figure 3), as corresponds to best-fit rotational temperatures of $T_r < 10$ K. A careful observation of the upper panel of Fig.3a reveals that in the spectra measured for the most intense expansions a weak signal coming from background thermal molecules is also observed which can be easily subtracted from the cold spectrum of the N$_2$ beam. With decreasing stagnation pressure the rotational temperature of the N$_2$ in the beam becomes progressively higher, as can be recognized in the REMPI spectra from the increasing relative intensity of the lines originating from excited rotational states. In the limit of high Knudsen number, $Kn_0$, ($p_{eq}d_{eff} = 0.4$–0.6 mbar cm, $Kn_0 \approx 0.01$), the number of binary collisions during the expansion is extensively reduced, which leads to a poor rotational relaxation with best-fit temperatures as high as $T_r = 115\pm15$ K.

The final velocity distributions of the molecular beams were measured as in refs 9, 36. The QMS detector sampled the velocity distribution, parallel to the axial streamline of the expansion. We have made the usual assumption that this distribution is of the “drifting Maxwellian” type$^{15}$ i.e. a Maxwell distribution characterized by a temperature $T_f$, travelling with the flow velocity, $u$. For a detector sensitive to the number density we have: $^{39}$

\[ f(v_f) \propto v_f^2 \exp[-(v_f-u)^2/\alpha_f^2], \]

where $\alpha_f = (2kT_f/m)^{1/2}$, with $k$ the Boltzmann constant and $m$ the molecular mass. The terminal values of the flow velocity $u_\infty$ and parallel temperature, $T_f_\infty$ were obtained from the standard deconvolution of the time of flight data.$^{40}$ Time of arrival distributions for three characteristic expansions are shown in Figure 4 together with their theoretical simulations.

The whole set of terminal flow velocities, translational and rotational temperatures measured in this work is shown in Figure 5. For the rationalization of these experimental data, we have made the same assumptions as in ref 9: a) The supersonic expansion close to the axial streamline has an approximate spherical symmetry and is continuous, i.e. describable in terms of local macroscopic variables, until a given distance (‘quitting surface’). Beyond that point collisions cease abruptly (‘sudden freeze’) and the flow becomes molecular. b) The source energy is conserved along a streamline, the specific heat is constant and the translational motion behaves in an approximate isentropic way. c) In the continuous flow region the different molecular degrees of
freedom may not be in equilibrium with each other, but thermal equilibrium is approximately maintained within each degree of freedom so that characteristic (Boltzmann) temperatures $T_b$, $T_n$, and $T_v$ can be used for the description of the translational, rotational and vibrational energetic modes respectively. The N$_2$ vibrational degree of freedom does not participate in the expansion, given its very small room temperature excitation and the high number of collisions required for its relaxation.$^4$ d) Rotation is coupled to the translational thermal bath of the jet through:

$$\frac{dT_r}{dt} = -\frac{1}{\tau_r} (T_r - T_t)$$  \hspace{1cm} (2)

where $\tau_r$ represents the rotational relaxation time and $T_t$ corresponds to the local translational temperature of the jet. The inverse of the rotational relaxation time can be viewed as the collision frequency for rotational relaxation and can be expressed in terms of an effective rotational relaxation cross section, $\sigma_r$, by means of $(\tau_r)^{-1} = 4n(kT_t/nm)^{1/2}\sigma_r$ where $m$ is the molecular mass, $k$ is the Boltzmann constant and $n$ is the jet local density.

Under the assumptions of the previous paragraph, the following balance equation, derived from the conservation of energy, holds along the jet centerline.$^{15}$

$$T_0 = \frac{5}{7} T_t + \frac{2}{7} T_r + \frac{mu^2}{7k}$$ \hspace{1cm} (3)

where it has been taken into account that the rotational contribution to the specific heat, $C_r$, is equal to $k$ for a linear diatomic molecule. Towards the end of the expansion, when collisions cease, equilibrium is no longer maintained among the different components of the translational temperature. For expansions of approximate spherical symmetry, it is customary to consider a component parallel to streamlines, $T_f$, and two components perpendicular to streamlines, $T_\perp$. Within the sudden freeze model, $T_t = T_f = T_\perp$. Along the continuous free jet until the quitting surface. As the expansion proceeds beyond this point, the perpendicular components of the translational temperature suffer a further
geometrical cooling and tend to zero with increasing distance to the nozzle exit, but \( T_f \), \( u \), and \( T_r \) remain frozen. The \( u_\infty \) and \( T_{f,\infty} \) determined from our TOF measurements hence correspond to the flow velocity and translational temperature at the quitting surface. These terminal flow velocities and translational temperatures are shown in the upper and lower panel of Figure 5, respectively, as a function of \( p_0 \Delta d_{\text{eff}} \), which is a measure of the Knudsen number in the beam source. For a given \( p_0 \Delta d_{\text{eff}} \) value, the measured terminal parallel temperature is taken as the criterion for the location of the quitting surface, i.e. the expansion is assumed to proceed until the point where the isentropic temperature reaches \( T_{f,\infty} \). The \( T_{f,\infty} \) versus \( p_0 \Delta d_{\text{eff}} \) data of the present work could be well fitted by modeling the terminal parallel speed ratio \( S_{f,\infty} = (m u_\infty^2 / 2 k T_{f,\infty})^{1/2} \), with the expression \( S_{f,\infty} = 1.02 \cdot (Kn_\infty)^{-0.31} \), in good agreement with the predictions of current models from the literature.\(^{15,41}\)

For the derivation of \( \sigma_f(T_r) \) from the present measurements, eq 2 is integrated numerically for each \( p_0 \Delta d_{\text{eff}} \) along the jet axis until \( T_r \) reaches the value given by the best fit curve to the measured \( T_{f,\infty} \). At this point of the expansion, the calculated rotational temperature is compared to the measured \( T_{r,\infty} \) and the rotational relaxation cross section is varied until a good fit to the experimental data is obtained. A functionality of the type:

\[
\sigma_f(T_r) = A \left( \frac{300}{T_r} \right)^{1.3} \left( \frac{B}{T_r} \right)^{\beta^2} 
\]

(4)

was found to be flexible enough to account for the whole temperature interval relevant for our experiments. Similar expressions have been used in previous works.\(^7\) The parameters giving a best fit to the data were \( A = 13 \, \text{Å}^2 \) and \( B = 8 \, \text{K} \); the theoretical \( T_{r,\infty}(p_0 \Delta d_{\text{eff}}) \) obtained with these parameters is represented as a solid line in the lower panel of Figure 5 together with the measured temperatures. For the numerical integration of eq 2, the isentropic relations with \( \gamma = 7/5 \) were used in order to express the local Mach number, \( M \), and derive the translational temperature, \( T_f \), the jet number density, \( n \), and the flow velocity, \( u \), as a function of the distance to the nozzle exit.\(^{15,43}\) This procedure does not take into account that the actual \( \gamma \) varies in the course of the expansion when
the local rotational temperature lags behind the translational one. Although this approximation has proven to be adequate for small deviations of $T_r$ from the isentropic behavior, it is not obvious that it should be appropriate here, given the wide range of expansion conditions sampled in the present work. In order to verify its validity we tried also a correction suggested by Labowski et al.,\textsuperscript{44} by adjusting the energy balance equation (3) at each integration step. Terminal rotational temperatures obtained elsewhere with this correction were in good agreement with the results of a more rigorous calculation based on the method of characteristics.\textsuperscript{15} In order to implement this correction, we used a $\gamma = 7/5$ equilibrium expansion, but decreased the external enthalpy by the amount corresponding to the ‘lagging’ rotational energy $C_r \Delta T_r$. With the new source enthalpy thus obtained, the flow variables were re-scaled before the next integration step. The terminal rotational temperatures obtained with a given $\sigma_r(T_r)$, were unaffected by this correction for $p_{\infty}d_{\text{eff}}$ values larger than 0.8 mbar cm; For the lowest $p_{\infty}d_{\text{eff}}$ investigated ($\approx 0.4$ mbar cm) the corrected rotational temperatures were lower by about 3 K than those obtained by assuming a constant $\gamma = 7/5$; this difference is fully within the experimental uncertainty in the determination of $T_{r,\infty}$.

The energy balance at the quitting surface is readily obtained from eq (3) and from the considerations of the previous paragraphs as

$$T_0 = \frac{5}{7} T_{t,\infty} + \frac{2}{7} T_{r,\infty} + \frac{m \omega_{\infty}^2}{7k}$$

(5)

The energy balance equation at the end of the expansion has been occasionally used by other authors to obtain terminal rotational temperatures of $N_2$ with data from time of flight measurements. However, this procedure is inaccurate since most of the energy is carried by the flow velocity and a small experimental uncertainty in $u_{\infty}$ leads to a large error in $T_{r,\infty}$.\textsuperscript{9,10} In the present case, the terminal flow velocity and all the relevant temperatures have been determined experimentally and one can use equation (5) in order to check the hypothesis of conservation of energy along the jet centerline. Since the introduction of a quitting surface is a gross oversimplification of the actual physical processes, it is not entirely clear where it must be placed. It should be stressed that, when
checking the energy conservation, we have considered the translational temperature to be isotropic \( (T_L = T_\perp) \) at the quitting surface and thus we have also included the contribution of the perpendicular components at the end of the expansion, as reflected in eq 5. In previous works it has been often assumed that the energy balance is better satisfied by making \( T_\perp \approx 0 \) K, thus implying that the anisotropy in \( T_t \) begins before the actual freezing of \( T_L \).\(^{13}\) Experimental measurements by Poulsen and Miller\(^{10}\) seem to support this assumption, but as we shall see later, this is related to the higher rotational temperatures reported in ref 10, in comparison to the ones obtained in the present work.

In the upper panel of Figure 5, the experimental \( u_\infty \) values are compared to those calculated with eq 5. The thick solid line represents the actual energy balance as obtained with the experimental temperatures (the best fit curves for \( T_{L,\infty} \) and \( T_{r,\infty} \) and \( T_0 = 296 \) K). The totally isentropic behavior \( (T_{r,\infty} = T_{L,\infty}) \) for \( \gamma = 7/5 \) is also shown for reference in the figure with a thinner solid line. As can be seen, the measured values lie always slightly below the predictions of the energy balance equation. In particular, the experimental points become gradually lower than those from the energy balance curve with decreasing \( p\Delta d_{\text{off}} \) in the \( \approx 0.5-5.0 \) mbar cm range. This deviation cannot be entirely accounted for by the uncertainty in the determination of \( T_{L,\infty} \) or \( T_{r,\infty} \). In this range, the source Knudsen number reaches comparatively high values \( (Kn_\infty \approx 0.01 \) for the mildest expansions considered). Under these circumstances, the assumption of ideal hydrodynamic flow underlying the isentropic model may not be justified and part of the source enthalpy might be lost due to heat conduction or viscous effects. In any case, the largest deviations observed are of the order of \( \approx 5\% \) which means that, even for the lowest \( p\Delta d_{\text{off}} \) values, more than \( 90\% \) of the initial source energy is conserved along the jet centerline until the end of the expansion. For \( p\Delta d_{\text{off}} > 10 \) mbar cm the deviations between the measurements and estimates of the energy balance equation are much smaller and the energy derived from the measured \( u_\infty, T_{L,\infty} \) and \( T_{r,\infty} \) account for \( 97-98\% \) of that in the source. It should be noted that the assumption of \( T_\perp \approx 0 \) K, supported by the measurements of Poulsen and Miller\(^{10}\) would give even higher values of the terminal flow velocity and consequently a larger difference between the measured \( u_\infty \) and that from the energy balance.
The $\sigma(T)$ derived from the present REMPI measurements is represented in Figure 6 by a solid line with error bars. For temperatures lower than 300 K, the cross section grows with decreasing temperature and reaches a maximum of about 55±20 Å² at $T_i = 20$-30 K. For lower temperatures $\sigma_i$ decreases down to $\approx 30±10$ Å² at $T_i = 5$-10 K. The sensitivity of the experiment decreases markedly for $T_i$ higher than $\approx 80$-100 K, but in this temperature region the present values agree approximately with those from quasiclassical trajectories$^{23}$ and ultrasonic measurements.$^{3}$ In view of the relatively large uncertainties in $\sigma_i$ and given its smooth evolution with temperature, it might be tempting at first sight to use an average constant relaxation cross section; however, this procedure does not give a good fit to the experimental data over the whole temperature range studied. Specifically, a decrease in $\sigma_i$ below 20 K is needed in order to account for the final rotational temperatures of the strongest expansions. These results are compared in Figure 6 with the $\sigma(T)$ reported in two recent literature works. In both cases, a linear relaxation equation analogous to eq 2 and a translational temperature corresponding to that of the $\gamma=7/5$ isentrope were assumed for the derivation of the rotational relaxation cross sections. The $\sigma(T)$ of Abad et al.$^9$ which is based on the analysis of their free jet SRS spectra and covers the temperature range 15-100 K, are consistent with the present results. However, the cross sections of Belikov et al.$^7$ extending down to 6 K and based on EIF measurements performed also on free jets of N₂, are clearly at variance with the present ones in the temperature interval between 30 and 6 K, where the $\sigma(T)$ of ref 7 grows rapidly with decreasing $T_i$ and reaches values of several hundred Å² below 15 K.

The use of the $\sigma(T)$ of ref 7 within the model of the present work (integration of eq 2 until $T_i = T_{\gamma=7/5}$) cannot reproduce the final rotational temperatures of our REMPI measurements as shown by the dashed line if Figure 5. In particular, the very large relaxation cross sections for the lowest $T_i$ lead to $T_{\gamma=7/5}$ values significantly smaller than those experimentally observed in our group at $p_{\text{tot,diff}} > 4$ mbar cm (see inset in Figure 5).

Terminal rotational temperatures measured with the EIF method in supersonic molecular beams of nitrogen from room temperature sources, have been reported by Poulsen and Miller$^{10}$ (for $p_{\text{tot,diff}} = 0.6$-5.0 mbar cm) and by Faubel and Weiner$^{11}$ (for $p_{\text{tot,diff}} = 6$ - 66 mbar cm). These results are compared in Figure 7 to the REMPI measurements of the present work. As indicated in the introduction, the
deduction of ground state rotational populations of N₂ from the electron beam induced fluorescence spectra is not straightforward. The method is based upon the promotion of ground state nitrogen molecules \( N_2(X^3\Sigma_g^-, \nu = 0, N) \) to the \( N_2^+(B^1\Sigma_g^+, \nu'=0, N') \) ionic excited state by electron impact and subsequent study of the \( N_2^+(B^1\Sigma_g^+, \nu'=0, N') \rightarrow N_2^+(X^3\Sigma_g^+, \nu''=0, N'') \) fluorescent emission. The main complications are related to the evaluation of the transition probabilities for the electron impact processes and to possible perturbations of the sample by the electron beam. In his pioneering work, Muntz\(^{30}\) assumed dipole selection rules (\( \Delta N = \pm 1 \)) for the primary excitation process. More recently, other groups\(^{32,42,48,49}\) refined the model by introducing higher order transitions (\( \Delta N > 1 \)) associated with the presence of low energy secondary electrons. In spite of these refinements, the interpretation of EIF data has remained controversial\(^{50-52}\). The need for a precise experimental determination of the electron impact transition probabilities, and the convenience to verify the electron beam results with data from optical spectroscopic methods has been stressed in a recent work.\(^{33}\)

In the experiment of Poulsen and Miller, the “electric dipole” (ED) model of Munz\(^{30}\) was used for the derivation of the rotational temperatures. In the work of Faubel and Weiner, both the electric dipole model and the “ejected electron interaction” (EEI) model of Coe et al\(^{32}\) were employed for the data analysis. Faubel and Wiener found that, for a given set of points, the EEI model yields rotational temperatures lower by 30-40 % than those of the ED model. For this experiment, the uncertainties in the rotational temperatures associated with the procedure for data analysis are shown as error bars in Figure 7. As can be seen, the EIF \( T_r, \infty \) values from refs 10,11 are systematically higher than the present REMPI ones. In the two EIF experiments an averaged (temperature independent) rotational cross section, \( \sigma_r \approx 14 \text{ Å}^2 \), was derived from the measured data by using also a sudden freeze model. This value for the cross section, when compared to our best-fit \( \sigma(T_d) \) (Fig.6), reflects the discrepancies in \( T_r, \infty \) shown in Figure 7 and is too low to account for our data, especially in the region of higher terminal temperatures (milder expansions) investigated by Poulsen and Miller. The disagreement is smaller with the measurements of Faubel and Weiner corresponding to lower terminal temperatures. Terminal translational temperatures were also provided in the mentioned works, and are
coincident with ours within the mutual experimental uncertainty; they have not been represented in the figure for clarity of display.

Although in the present work no measurements have been performed in the free jet region before the end of the expansion, the $\sigma_r(T_J)$ obtained from our data in conjunction with eq 2 can be used to simulate the free jet results from previous literature works. In Figs. 8 and 9, we show the results of such simulations. The data represented in Figure 8 correspond to optical spectroscopic methods, and those of Figure 9 to EIF measurements. The calculated $T_r$, represented by solid curves, have been drawn until the position of the quitting surface, except in the lower panel of Figure 8, where the measured data stretch far beyond this point and the curve has been prolonged with a line corresponding to $T_r=0$.

The SRS measurements of Abad et al.⁹ (Figure 8a) are satisfactorily reproduced with the rotational relaxation cross sections of the present work. It seems that in the lowest temperature region ($T_r < 10$ K) a smaller cross section could give a better fit, but the experimental uncertainty is too large to draw conclusions.

Figure 8b shows the simulation of the CARS measurements reported by Ilyukhin et al.¹⁺² for two supersonic expansions without clustering. The simulation gives again a good global account for the data. For the stronger expansion, the experimental rotational temperatures do not deviate from the isentrope over the $x/d_{eff}$ range studied, in accordance with the calculation. In this case the $\sigma_r(T_J)$ of this work provides just a lower limit to that compatible with the measurements. For the milder expansion the simulation yields values of $T_r$ somewhat higher than the measured ones for temperatures lower that 20 K. It is worth noting that the rotational relaxation cross sections deducible from the rotational collision numbers, $\sigma_r$, and gas kinetic cross sections, $\sigma_r(T_J)$ reported in ref 12 are larger than 100 Å² for temperatures below 30 K. Application of eq 2 with such large relaxation cross sections leads to $T_r$ values lower than the experimentally measured ones for the milder expansion. The deviation of the calculated curve from the experimental points (not shown for clarity) is of similar magnitude but of opposite sign than that obtained with the present $\sigma_r(T_J)$. This reflects the comparatively low sensitivity of many
jet measurements to the precise value of $\sigma_\gamma$ and stresses the usefulness of the present molecular beam experiments that sample terminal temperatures and evince the breakdown of equilibrium between translation and rotation in a more direct way.

Finally, Figure 8c displays the rotational temperatures for a relatively mild expansion of $N_2$ derived by Mazely and Smith\textsuperscript{34} from REMPI measurements. In this case, the measured rotational temperatures sample the whole transition region from the free jet to the molecular flow. The location of the quitting surface is easily recognized as the point where the model $T_r$ and $T_i$ become frozen. Although the continuous free jet data exhibit a certain dispersion, most of the points in the relevant asymptotic region are quite well reproduced with the present relaxation cross sections.

Further measurements of the rotational temperature in free jets of nitrogen from room temperature sources from various Raman techniques\textsuperscript{53-55} are also available in the literature (not shown in Figure 8). All these data are in good agreement with the temperatures predicted from the $\sigma_\gamma(T_r)$ of this work.

Figure 9 shows the simulation of the results of two EIF experiments from different groups. In each case, a weak and a strong expansion with comparable $p_d\alpha$ have been selected among the larger set studied by both groups. In the upper panel, the rotational temperatures obtained by Marrone\textsuperscript{31} with the ED model are displayed. As can be seen, the overall trend, including the points of deviation of the rotational temperatures from the $\gamma=7/5$ isentrope, is well reproduced by the calculated curves, but the experimental rotational temperatures are somewhat larger than those predicted with the present cross sections. In contrast to these results, the measurements of Coe et al.\textsuperscript{32} (lower panel of Figure 9), who used the EEI model for the analysis of the fluorescence data, lead to rotational temperatures smaller than those predicted with our relaxation cross sections. Much higher cross sections than those obtained in this work would be necessary in order to account for the lowest temperature measurements. However, it is worth noting that, as shown by the authors, the same experimental data lead to higher temperatures and to a worse agreement with the assumption of a Boltzmann distribution for the rotational levels of the $N_2$ molecules in the jet, when the ED model is used for the
analysis of the fluorescence spectra. Measurements of rotational temperatures in free jets of nitrogen by the EIF method have also been reported by other groups. A critical discussion of these results and of the conflicting interpretation of the data can be found in refs 8, 33 and in the references cited therein.

The use of a rotational temperature in studies of rotational relaxation in free jets has been sometimes questioned due to the possibility of different relaxation kinetics for the individual rotational states.\textsuperscript{35} Furthermore, for the very strong cooling attained in some of the jet experiments, the mere concept of a temperature for the characterization of the distribution of the few remaining rotational states may be dubious. In this respect it should be noted, that a possible departure from Boltzmann equilibrium would not invalidate the estimates of the average relaxation cross section obtained with eq 2, since $T_r$ can be considered as a convenient shorthand for the average rotational energy. The actual occurrence of non-Boltzmann distributions of rotational levels in free jets of N\textsubscript{2} has been much debated. In many of the EIF experiments an overpopulation of the higher rotational levels is found, whereas in all of the experiments based on optical spectroscopic methods mentioned above, approximate Boltzmann distributions are reported within the experimental uncertainty. In the present work no significant deviation from Boltzmann type populations was observed even for the coldest supersonic beams investigated, for which the relative population of rotational states are well reproduced with temperatures as low as $T_r \approx 7$ K (see Figure 3). In any case, there seems to be a general agreement about the fact that for the lower levels, where most of the rotational energy is concentrated, the assumption of a Boltzmann distribution is justified.

The considerations of the previous paragraphs indicate that a good overall agreement exists between the results of this work and most of the measurements from other groups based on optical spectroscopic methods, but discrepancies are found with some of the EIF results both in the higher\textsuperscript{10} and lower\textsuperscript{7,32} end of the temperature range investigated. The most significant discrepancy between the results of this work and others from the literature concerns the magnitude of the rotational relaxation cross sections for temperatures lower than 20 K. Whereas our results indicate that $\sigma_\tau(T_j)$ has an average value of $\approx 30$ Å\textsuperscript{2} in the 5-25 K temperature interval, the relaxation cross
sections reported by Belikov et al. or those implied by the $T_r$ measured by Coe et al. are much larger (several hundred $\AA^2$) and certainly incompatible with our data.

In the absence of accurate dynamical calculations for the low temperature interval relevant to the observed discrepancy, we will give a simple and intuitive argument in qualitative support of our results. A rough estimate of the likelihood of rotational energy transfer by collisions is provided by the adiabaticity or Massey parameter \(\xi = t_{\text{coll}} / t_{\text{rot}}\), where \(t_{\text{coll}}\) represents the collision time and \(t_{\text{rot}}\) the rotational period. The collision time is usually defined as \(a / \langle V\rangle\), where \(a\) is the range of the intermolecular potential and the average collision velocity is given by \(\langle V\rangle = (8kT / \pi m)^{1/2}\). The probability of rotational energy transfer decreases with increasing \(\xi\) and the region of \(\xi > 1\) (collision slower than rotation) is generally taken as the adiabatic regime of inefficient energy transfer. In Figure 10 we have represented the evolution of \(\xi\) with temperature for our system, together with our best fit $\sigma_r(T)$ for the calculation of $t_{\text{rot}}$ at a given temperature, we have taken average rotational period of the rotational levels, $N$, that can relax (i.e., those with $N \geq 2$) and for the calculation of $t_{\text{coll}}$ we have assumed that $a \approx 3.8 \AA$ is the length parameter of a N$_2$-N$_2$ Lennard-Jones potential. As can be seen, $\xi$ increases abruptly at low temperature, $T < 30$ K, toward the adiabatic regime, precisely where our observations yield a marked decrease of the rotational relaxation cross section. Hence, these qualitative considerations are congruent with our data and render very unlikely a large increase of the rotational relaxation probability in the 5-30 K temperature range, as proposed in previous works.

4. Summary and Conclusions

The technique of resonance-enhanced multiphoton ionization has been applied to the determination of terminal rotational temperatures in supersonic molecular beams extracted from free jets of nitrogen. These data, together with measurements of terminal flow velocities and translational temperatures obtained from time of flight measurements, have been used for the estimate of the cross section for rotational energy relaxation at low temperature ($T \approx 5$-100 K).
The present data suggest that the isentropic hypothesis used in most free jet models is in general well justified. For hydrodynamic expansions of N₂ from room temperature sources, the condition of conservation of energy along the jet centerline, underlying isentropic behavior is fulfilled within 97-98%, for values of the source Knudsen number smaller than 0.001 and, even for \( Kn_0 \approx 0.01 \), more than 90% the source energy is conserved at the end of the expansion.

From our terminal rotational temperatures the average relaxation cross section has been estimated over a wide temperature range extending down to approximately 5 K. The cross sections for rotational relaxation found in this work have a maximum value of approximately 50-60 Å² at 20-30 K. For lower temperatures this cross section decreases and reaches a value smaller than 30 Å² at \( T \approx 5 \) K. At temperatures larger than 30 K, the cross section decreases slowly with growing temperature and converges approximately to the determinations from other non-jet techniques and theoretical estimates for \( T \approx 80-100 \) K.

The literature values of free jet rotational temperatures measured with different optical spectroscopic methods are, in general, well reproduced with the relaxation cross section derived from our experimental data. The results from electron-beam induced fluorescence experiments are more dependent on the data reduction scheme and, for temperatures lower than 30 K, some of them yield very large cross sections clearly at variance with the findings of the present work. Classical arguments based on the value of the Massey parameter support the present data and show that for the low temperatures investigated, collisions tend to enter the adiabatic regime, where the probability of energy transfer between rotation and translation should decrease markedly. Nevertheless, further experiments and theoretical calculations are needed in order to assess the likelihood of rotational relaxation of nitrogen at very low temperatures.
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Tables

Table I: Line strengths, $S_{N'N''}$, for the coherent absorption of two linearly polarized photons leading to the $a^1\Pi_g(v=1,N') \leftarrow X^1\Sigma_g^+(v=0,N'')$ rotational transitions of $N_2$.

<table>
<thead>
<tr>
<th></th>
<th>O branch</th>
<th>P branch</th>
<th>Q branch</th>
<th>R branch</th>
<th>S branch</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{N'N''}$</td>
<td>$\frac{N''(N''-2)}{3(2N''-1)}$</td>
<td>$\frac{N''+1}{6}$</td>
<td>$\frac{2N''+1}{2(2N''+1)(2N''+3)}$</td>
<td>$\frac{N''}{6}$</td>
<td>$\frac{(N''+3)(N''+1)}{2(2N''+3)}$</td>
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Figure captions.

Figure 1. Schematic view of the experimental set-up used for the REMPI measurements: PN, pulsed nozzle; S, skimmer; R, reflector; E, extractor; SL, steering plates; MCP, micro channel plate detector; FD, fast ionization detector; UV, ultraviolet laser beam.

Figure 2. Experimental (top) and simulated (bottom) (2+2) REMPI spectra of $N_2$ at room temperature (see text for details).

Figure 3. Three typical molecular beam REMPI spectra recorded for different expansion conditions. The simulated spectra and the best fit rotational temperature $T_{r,\infty}$ used in the simulations are also shown for comparison.

Figure 4. Time of arrival distributions measured in the molecular beams corresponding to three typical expansions: The points represent the experimental results and the solid line the theoretical simulations. The best fit terminal flow velocity, $u_\infty$ and parallel translational temperature, $T_{f,\infty}$ are also indicated.

Figure 5. Top: Terminal flow velocities, $u_\infty$, as a function of $p_0d_{\text{eff}}$. The points stand for experimental values. The thick solid line represents the terminal flow velocity obtained from energy conservation (eq 5), with the measured values of the terminal rotational and translational temperatures, the thin solid line represents the $u_\infty$, corresponding to the $\gamma=7/5$ isentropic behavior with the sudden freeze criterion used in the text. Bottom: Circles and squares represent the measured terminal rotational and parallel translational temperatures, respectively, as a function of $p_0d_{\text{eff}}$. Open and solid symbols refer to measurements performed with different types of skimmers (see text). Solid lines are the best fit curves obtained with the present model. See text for details. The dashed curve is the prediction for $T_{r,\infty}$ derived from the relaxation cross sections of ref 7. The inset is an enlargement of the lowest temperature region.
Figure 6. Cross-section for the rotational relaxation of N₂ molecules as a function of temperature. Solid line with error bars: derived from the present REMPI experiments. Dashed line: Adapted from ref 9. Dotted line: Adapted from ref 7.

Figure 7. Terminal rotational temperatures as a function of \( p_i d_{\text{eff}} \). Solid triangles: from ref 10; solid squares: from ref 11; open circles: present REMPI measurements. The solid line represents the best fit of present work. See text for details.

Figure 8. Simulations of rotational and translational temperatures in the free jet expansions. In the three panels, the symbols are the experimental data obtained by optical spectroscopic methods and taken from the literature references indicated in the figures. The solid curves show the evolution of \( T_r \) calculated with eq 2 using the rotational cross sections obtained in the present work. The dashed line represents the evolution of the translational temperature, \( T_t \), which is assumed to be that of the \( \gamma=7/5 \) isentrope.

Figure 9. Same as figure 8 but for EIF measurements.

Figure 10. Evolution of the Massey parameter, \( \xi \), with temperature together with the best-fit \( \sigma_r(T) \) from the present work.
Fig 1  Aoi et al.
Fig 2. Aoiz et al.
Experiment
$P_d d_w = 59 \text{ mbar cm}$

Simulation
$T_{ref} = 8 \text{ K}$

REMPI Signal (arb. units)

4.5 mbar cm

28 K

0.9 mbar cm

70 K

One-Photon Wavelength (nm)
Fig. 4  Aoi et al.
Fig. 9, Aoiz et al.
Fig 10: 

\[ \xi = \frac{t_{\text{coll}}}{t_{\text{rot}}} \]

\[ \sigma_f \]

Temperature (K)

Relaxation Cross Section (A^2)