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Effects of translational, rotational, and vibrational energy on the dynamics of the D + H₂ exchange reaction. A classical trajectory study

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Quasiclassical trajectory (QCT) calculations for the D + H₂(v,j) → HD + H system have been performed on the Liu, Siegbahn, Truhlar, Horowitz (LSTH) potential energy surface in order to study the combined effects of translation, rotation, and vibration on the reactivity. The range of initial conditions covered has been \( E_r = 0.25-1 \) eV, \( v = 0, 1, \) and \( 2 \) and \( j = 0-12 \).

Integral cross sections, opacity functions, solid angle differential cross sections, and the energy partitioning among the products' degrees of freedom have been obtained. The minimum in the dependence of the total cross section with rotational excitation observed in previous QCT calculations for \( v = 0 \) and \( v = 1 \) at low collision energies is here verified also for \( v = 2 \). The center-of-mass (c.m.) angular distributions of the scattered HD product are predominantly backward with respect to the direction of the D incoming atom, at low energies, but they broaden markedly and become more forward with increasing total energy. Translational and vibrational excitation in the reactants are largely adiabatic and tend to remain as translation and vibration in the products. Where they can be compared, present results are in good agreement with recent quantum mechanical calculations and with experimental measurements.

I. INTRODUCTION

The role played by translational and by internal energy in chemical change at a molecular level and its relationship to the properties of the potential energy surface (PES) which govern a given reaction has deserved much attention since the early systematizations of Polanyi and co-workers.1-3 Good reviews covering different aspects of the subject are now available.4-9 The effects of the specific energy modes on direct reactions of the A + BC type have been studied in detail by means of quasiclassical trajectory (QCT) calculations on both model and real systems with different, mostly semiempirical potential energy surfaces and, when possible, compared to experimental results.10-11 Initially, the ease to perform and visualize calculations for collinear collisions attracted much attention to the study of the distinct role of translation and vibration on reaction probability permitting us to gain some insight; in particular, the fact that translational energy (\( E_r \)) is more effective in promoting reaction for systems with an early barrier, whereas vibrational energy (\( E_v \)) is more efficient for reactions with a late barrier, was clearly established.12

More recently, extensive work has also been devoted to the effect of rotational energy (\( E_R \)) on reactivity,6,7,13-22 but in spite of some progress, no simple general assertions can be made about the influence of rotation on a reaction and the shape of the corresponding PES.

The prototypic H + H₂ reaction and its isotopic variants, for which the PES is known from \textit{ab initio} calculations to a great accuracy,23-25 provides a very good occasion for the investigation of the role of the different energy modes on the reaction dynamics. Previous QCT calculations have shown specifically that the total reaction cross section (\( \sigma_R \)) grows monotonically with both translational and vibrational energy in the postthreshold region26-32 (at least up to \( E_r \approx 1 \) eV), and that an increase in the rotational excitation of the H₂ molecule at low collision energies (\( E_r < 0.6 \) eV) leads to a minimum in \( \sigma_R \).33-35 Due to the mentioned accuracy in the knowledge of its PES, the H₂ system constitutes a unique ground for the comparison and experimental test of distinct theoretical approaches. The situation has become specially interesting in later times,36,37 since the severe experimental difficulties associated with the study of the H + H₂ system at a detailed microscopic level are being gradually overcome and a wealth of experimental data is becoming available.37-56 On the other hand, important progress in the methodology of quantum dynamical calculations has led to the extension of the pioneering exact 3D quantum scattering calculations by Schatz and Kuppermann57 on H + H₂ to higher energies and to isotopic variants of the reaction.58-74

Specifically, for the D + H₂ reaction, the overall agreement between the theoretical calculations [exact quantum mechanical (QM)59,68,69 and QCT31,32,75] and experimental measurements [which now include angle and velocity distributions from crossed molecular beams42,45,46,48,55,56 as well as products' internal state distributions from coherent anti-Stokes Raman spectroscopy (CARS)49,51 and resonantly enhanced multiphoton ionization (REMPI)53,54 under single collision conditions] is good, but there exist some discrepancies. In particular, a detailed comparison between recent molecular beam differential cross sections (angle and velocity resolved) by Buntin, Giese, and Gentry55 and by Contin-
etii, Balko, and Lee with the exact quantum mechanical results by Zhang and Miller (on the LSTH surface) and by Zhao, Truhlar, Schwenke, and Kouri [on the double many-body expansion (DMBE) surface] for the D + H₂→ HD + H reaction, has apparently shown differences (the experiments indicate that the HD backward scattered products exhibit a higher rotational excitation than the theoretical predictions). This could suggest that some of the regions of the current potential energy surface might not be accurate enough. However, a very recent ab initio reevaluation of the H₃ potential, specially of the bending configurations at high energies, has shown an excellent agreement with both the LSTH and the DMBE fits of previous ab initio points.

In former papers, we have performed quasiclassical calculations of total and differential cross sections for the D + H₂→ HD + H system in a range of conditions of interest to recent experiments and for the comparison with exact quantum mechanical results. In the present work, we extend our QCT study of the D + H₂ (vJ) reaction in order to systematically cover the v = 0–2, J = 0–12, and Eₜ = 0.25–1 eV intervals. This allows a consideration of the combined effects of translation, rotation, and vibration on reactivity. The relevance of QCT calculations is not only limited to the range of energies and angular momenta where exact QM calculations are not yet feasible or too cumbersome. It is also important to ascertain the validity of classical mechanics in predicting chemical attributes and to evoke the appearance of specific quantum effects such as dynamical resonances.

The present data might also be useful for future tests of the potential energy surface since they include a large set of initial conditions, many of them pertaining to those regions where the accuracy of the PES is not so firmly established.

II. QCT CALCULATION AND METHOD

The overall methodology followed in the present calculations is well described in the excellent reviews available. All the trajectories are calculated on the LSTH potential energy surface. The integration of the differential set of equations of motion is carried out by using a Hamming predictor-corrector method with a fixed step size initialized by a fourth-order Runge–Kutta integration. Accuracy and stability in the integration is addressed in the usual way by checking the conservation of both total angular momentum and total energy. With a step size of 5×10⁻¹⁷ s, the conservation of total energy was invariably better than 1 in 5×10⁶.

Calculations are carried out at selected Eₜ, v, and J values; namely, v = 0, 1, and 2 and Eₜ and J covering the ranges of 0.25–1.00 eV and of 0–12, respectively. The values of vibrational and rotational energies are calculated from the full Dunham expansion for H₂ for reactants and HD for products. Internal energy is deposited by placing the molecules at the beginning of the trajectory in alternatively the inner and outer turning points corresponding to the specific vibrational quantum numbers.

The rest of the initial conditions are sampled by an unbiased Monte Carlo method from the original distributions of the collision parameters. The maximum impact parameter is chosen such that no reactive trajectories are contained in the last few bins of the histogram of the opacity function, ranging from 0.7–2.0 Å depending on Eₜ, v, and J values. The initial reaction shell radius, i.e., the initial D–H₂ center-of-mass distance, is set in the interval of 5–6 Å depending on the phase of H–H rotational motion.

Assignment of final quantum numbers has been done by fitting the internal energy to the full Dunham expansion of vibrationalrotational energies of the HD molecule. The values v′ and J′ so obtained are rounded to the nearest integer, following the standard histogram method, i.e., the probability for each reactive trajectory of having a quantum number n is Pn(v) = 1 if n = nₑ and Pn(v) = 0 if n ≠ nₑ, with nₑ being the nearest integer to the real quantum number v as calculated by the aforementioned procedure. Those trajectories yielding HD with vibrational energy between the minimum of the potential and E(v′ = 0) are taken as reactive with v′ = 0.

The use of the quadratic smooth sampling method to assign final quantum numbers does not produce any substantial change in values of the vibrationally state resolved cross section.

In the present as well as in former works, the reactivity and final state functions are calculated by the method of moments expansion in Fourier series. This method has the advantage over the histogrammic one that it yields continuous functions describable by few coefficients and, therefore, much easier to handle. Legendre expansion (or, for this respect, any other suitable expansion in orthogonal functions) is completely equivalent to the Fourier expansion here employed.

The opacity function P_r(b) can be written in terms of the normalized function G(b) as a cosine Fourier series

\[ G(b) = \frac{\pi b^2}{\sigma_R} P_r(b) \sim 1 + \sum_{n=1}^{M} c_n \cos(n\pi \beta), \]

where \( b \equiv b' / b_{max} \) is the unbiased sampling variable, with \( b_{max} \) being the limiting or maximum impact parameter. The coefficients of the expansion (1) are given by

\[ c_n = \frac{2}{N_r} \sum_{i=1}^{N_r} \cos(n\pi \beta_i), \]

where the sum in Eq. (2) is upon the \( N_r \) reactive trajectories, each with \( \beta_i = b_i / b_{max} \), being the impact parameter of the \( i \)th trajectory. Once the coefficients \( c_n \) are determined, the opacity function is given by

\[ P_r(b) = \frac{\sigma_R}{\pi b_{max}^2} G(\beta(b)). \]

Several criteria have been used to truncate series (1) to \( M \) terms. The simplest one is to stop the expansion whenever the uncertainty \( \gamma_n \) (standard deviation, 68% confidence limit) of the coefficient \( c_n \) is of the order or less in absolute value than the \( c_n \) value itself. However, some of the \( c_n \) can be naturally small and the truncation would be incorrect. One means to avoid this is to compute the partial sums of the...
squares of the deviations of the $c_n$ from $y_n$, using as a stopping criterion the comparison of the successive partial sums with $M$ and $M + 1$ terms. The truncation takes place when these sums reach the same value.$^{84}$

In the present work, the Smirnov–Kolmogorov statistical test$^{85}$ is employed as an additional stopping criterion. The number of coefficients is changed until the deviation of the observed and fitted cumulative probability distributions is small enough with a significance level of 70%–95%. This last criterion has proved to be very useful since the addition of more terms in the series (1) normally leads to a deterioration of the statistics due to the generation of noise.

The estimation of the error of the coefficients of the series is given by$^{84}$

$$\gamma_n^2 = \text{var}(c_n) = \frac{4}{N_r} \text{var}\{\cos(n\pi\beta)\} = \frac{4}{N_r}\left\{4\langle \cos^2(n\pi\beta) \rangle - c_n^2 \right\},$$

where $\text{var}(\cdot)$ refers to the variance and $\langle \cdot \rangle$ to the average over the ensemble of values of $\beta_k$ from the $N_r$ reactive trajectories. It can be shown that the upper limit of $\gamma_n^2$ is $4^4 2/N_r$. The error of the series $G(\beta)$ will then be given by

$$\text{var}\{G(\beta)\} = \sum_{n=1}^{M} \left[ \frac{\partial G(\beta)}{\partial c_n} \right]^2 \gamma_n^2 = \sum_{n=1}^{M} \gamma_n^2 \left\{\cos(n\pi\beta)\right\}^2.$$  \hspace{1cm} (5)

Notice that the error will be minimum for $\beta = 0, 1$ and maximum for $\beta = 1/2$, and that this error increases in general as the number of terms increases.

Finally, the statistical error $\varepsilon$ (which will correspond to the 68% of significance level, provided that the number $N_r$ is large enough) of the opacity function $P_r(b)$ will be given by

$$\varepsilon[P_r(b)] = \left\{\text{var}\{P_r(b)\}\right\}^{1/2}$$

with

$$\text{var}\{P_r(b)\} = \text{var}(c_R) \left[ \frac{G[b(b)\beta]}{\pi b_{\text{max}}^2} \right]^2 + \left[ \frac{dG[b(\beta)]}{d\beta} \right]^2 \text{var}\{G[b(\beta)]\}$$

$$= \langle P_r(b) \rangle^2 \left[ \frac{N - N_r}{N_r \cdot N} \right] + \frac{\sigma_R^2}{\pi b_{\text{max}}^2} \sum_{n=1}^{M} \gamma_n^2 \cos^2(n\pi\beta(b)).$$

(7)

Figure 1(a) displays a comparison of the Fourier cosine expansion and the histogram method for the determination of the opacity function $P(b)$ in three different cases. Following Ref. 72 and accordingly the bins have equal size in $\beta = b/\beta_{\text{max}}$ and in $x = 1/2(1 - \cos \theta)$. The most probable errors in each bin are similar to error bars calculated for Fourier fits (see the text).

As can be seen, the agreement is excellent in all the cases. Error bars, calculated with expression (6), are shown at two values of $b$ for each $P_r(b)$, to illustrate the uncertainty of the determination. The most probable error (68% confidence level) in any bin of the histogram is given by

$$\varepsilon[P_r(\beta)] = \frac{N_{r_k}}{N_k} \left( \frac{N_k - N_{rk}}{N_k N_{rk}} \right)^{1/2}. \hspace{1cm} (9)$$

The uncertainties calculated by both methods are very similar.

When the statistical weight for different trajectories is not the same, for instance, when importance sampling$^{80}$ is used or when for final state resolved functions the quadratic smooth sampling is employed, function $G(\beta)$ becomes

$$G(\beta) = \frac{\pi b_{\text{max}}^2}{\sigma_R} W(b) P_r[b(\beta)] \sim 1 + \sum_{n=1}^{M} c_n \cos(n\pi\beta)$$

and now the coefficients can be found as

$$c_n = \frac{2}{S_{N_r=1}} \sum_{j=1}^{N_r} W_j \cos(n\pi\beta_j) = 2 \langle \cos(n\pi\beta) \rangle,$$ \hspace{1cm} (11)

where

FIG. 1. Comparison of the Fourier moment expansion and the usual histogram methods for (a) opacity function $P(b)$ and (b) solid angle differential cross section. The figure shows the results at three different collision energies. The error bars in the Fourier fitting represent the uncertainty (68% confidence interval) calculated as described in the text. Note that the histograms are constructed following the uniform phase space criterion (Ref. 72) and accordingly the bins have equal size in $\beta = b/\beta_{\text{max}}$ and in $x = 1/2(1 - \cos \theta)$. The most probable errors in each bin are similar to error bars calculated for Fourier fits (see the text).
\[ \beta_i = \int_0^{s_b} P_0^i(b) \frac{2b}{b_{max}} db = \int_0^{s_b} \frac{2b}{b_{max}} W(b) \]  

and

\[ S_N = \sum_{i=1}^{N} W_i. \]  

The sampling variable is now given by Eq. (12), where \( P_0^i(b) \) is the importance sampling function.\(^{60}\)

The opacity function is given by

\[ P_r(b) = \frac{\sigma_R}{\pi b_{max}^2} P_0^i(b) G[\beta(b)] \]  

with

\[ \sigma_R = \frac{S_{N_r}}{\sum_{i=1}^{N} W_i}. \]

The statistical error of the opacity function (14) is obtained as in Eq. (6) with the variance being

\[ \text{var}[P_r(b)] = [P_r(b)]^2 \left[ \frac{N - S_{N_r}}{NS_{N_r}} \right] + \left[ \frac{\sigma_R}{\pi b_{max}^2} P_0^i(b) \right]^2 \times \text{var}[G(\beta)]. \]  

The var \([G(\beta)]\) is given by Eq. (5) and the error of the nth coefficient \( \gamma_n \) is now given by

\[ \gamma_n = 4S_{N_r}^{-1} \text{var}[\cos(n\pi \beta)] = S_{N_r}^{-1} \left[ 4\cos^2(n\pi \beta) - c_n^2 \right]. \]  

A treatment entirely analogous holds for the representation of the solid angle differential cross section \( d^2 \sigma_{R}/d\omega \). In this case, the adequate variable is chosen to fulfill the criterion of "uniform phase space" (see Ref. 80), i.e.,

\[ \chi = 1/2(1 - \cos \theta), \]  

where \( \theta \) is the scattering angle with respect to the direction of the incoming atom. The variable \( \chi \) is bounded in \([0, 1]\). The solid angle differential cross section is, in terms of the normalized function \( g(\chi) \), also expanded in cosine series

\[ \frac{d^2 \sigma_R}{d\omega} = \frac{\sigma_R}{4\pi} \frac{g(\chi)}{4\pi} \left[ 1 + \sum_{n=1}^{N_r} a_n \cos(n\pi \chi) \right]. \]  

The coefficients are given as in Eq. (2)

\[ a_n = \frac{2}{N_r} \sum_{i=1}^{N_r} \cos(n\pi \chi_i). \]  

The same truncation criteria applied in series (1) are valid for Eq. (19).

The statistical error (68% confidence level) of the solid angle differential cross section is the square root of its variance given by

\[ \text{var(} \frac{d^2 \sigma_R}{d\omega}) = \left( \frac{d^2 \sigma_R}{d\omega} \right)^2 \left[ \frac{N - N_r}{NN_r} + \sum_{n=1}^{N_r} \gamma_n^2 \cos^2(n\pi \chi) \right], \]  

where \( \gamma_n \), the uncertainties of the coefficients, are given by the equivalent to expression (4).

Figure 1(b) represents the \( d^2 \sigma_R/d\omega \) for the same three cases as Fig. 1(a). The curves are the cosine expansions. Their statistical uncertainties at three values of \( \theta \) are shown in each case. The same figure contains the corresponding histograms built with bins equally spaced in \( \chi \). Again, the agreement is excellent with similar uncertainties in both cases, but with the advantage, in the case of the continuous curves, of being describable by less data. When state resolved differential cross sections are calculated, the sums in Eq. (20) are restricted to those reactive trajectories which yield products at the indicated quantum number. If quadratic smooth sampling (or importance sampling) is used, analogous expressions to Eqs. (11) and (17) will hold for the coefficients \( a_n \) and their uncertainties \( \gamma_n \), respectively.

For the continuous probability functions of the translational and rotational fractions of the total energy available to the products, the same method has been employed. Instead of a cosine series, a sine series could be used, especially when the function to be expanded becomes null in \( \chi = 0 \) and \( x = 1 \). In some cases, a smoothing procedure could be convenient (see Ref. 84).

The total number of calculated trajectories relevant to this work has been 950 000.

III. RESULTS AND DISCUSSION

A. Total reaction cross section

The absolute values of the total reaction cross section \( \sigma_R(\nu_i, E_F) \) for the \( D + H_2 \rightarrow HD + H \) system as a function of translational, rotational, and vibrational energy are shown in Figs. 2–8 and their values are listed systematically in Table I.

The behavior of the reaction cross section as a function of rotational energy is portrayed in Fig. 2 for the three first vibrational states of the \( H_2 \) molecule and at several collision energies. Undoubtedly, the most salient feature is the presence of a minimum in the dependence of \( \sigma_R \) with \( E_R \) at low collision energies, say, below 0.65 eV. This effect has already been shown in previous calculations carried out on the \( H_2 \) system for \( H_2(v = 0) \) \(^{33}\) and \( H_2(v = 1) \).\(^{34,35}\) Present work shows that such a minimum, at \( j \) values between \( j = 4–6 \), exists even when the molecule is in its \( v = 2 \) level.

For all three vibrational quantum numbers studied here, the minimum gets gradually more shallow with increasing \( E_F \) and eventually disappears at a collision energy of \( \sim 0.65 \) eV, as first shown by Boonenberg and Mayne\(^{33}\) in their QCT calculations for the \( H + H_2(\nu = 0) \) reactive system. At the collision energy of 1 eV, \( \sigma_R \) increases monotonically with \( E_R \). As can be seen, the decrease in absolute value of \( \sigma_R \) in the region where the minimum exists is more pronounced in going from \( v = 0 \) to \( v = 2 \). However, this representation could be misleading. In fact, the relative decrease in reactivity associated with this minimum becomes less prominent with increasing vibrational quantum number of \( H_2 \). This is clearly shown in Fig. 3, where the \( \sigma_R(j,v)/\sigma_R(j = 0,v) \) values for each vibrational number as a function of the \( H_2 \) rotational quantum number are displayed at 0.35 and 0.45 eV of collision energy. It is apparent that the relative decrease is more dramatic for \( v = 0 \) than for \( v = 1 \) and \( v = 2 \). At 0.35 eV, the cross section in \( v = 0 \) is, at the minimum, 5% of that for \( j = 0 \), whereas it is 80% in the case of \( v = 2 \). It is interesting to note how the relative minimum shifts toward higher values of \( j \) in going from \( v = 0 \) to \( v = 2 \).
FIG. 2. Total reaction cross section (in $\text{Å}^2$) for the $\text{D} + \text{H}_2(j)\rightarrow\text{HD} + \text{H}$ system as a function of $\text{H}_2$ rotational energy (eV) at the indicated translational energies (0.25, 0.35, 0.45, 0.65, and 1.00 eV) and for the three first $\text{H}_2$ vibrational levels $v = 0$ (lower panel), $v = 1$ (middle panel), and $v = 2$ (upper panel). Errors in $\sigma_R$ (68% standard deviation) are of the order or smaller than the size of the represented points (see Table I). The lines through the points are polynomial fittings to the points.

This effect was already observed in a QCT study of $\text{H} + \text{H}_2(j = 0)$ by Barg, Mayne, and Toennies.\textsuperscript{30}

The present results are in good agreement (mostly within experimental error) with the total cross section values obtained from the existing experiments with microscopic resolution for $\text{D} + \text{H}_2(v = 0)$\textsuperscript{38,49} and $\text{D} + \text{H}_2(v = 1)$.\textsuperscript{46}

QCT total cross-section values for this reaction had been calculated previously at some of the collision energies.

FIG. 4. A 3D plot of the reaction cross section (in $\text{Å}^2$) as a function of translational $E_T$ and rotational energy $E_R$ (in eV) for the $\text{H}_2$ vibrational quantum number $v = 0$. 
considered here, especially for \( v = 0 \) (Refs. 31 and 75) and in some cases for \( v = 1 \) (Refs. 31, 34, and 68). The agreement is, in general, good, but there is a discrepancy, greater than the statistical error, between present values and those of Ref. 31 in the results for \( v = 1 \) at \( E_T \) above 0.45 eV. This is probably due to the fact that in Ref. 31, and only for \( v = 1 \), those trajectories with vibrational energies below the products' zero point energy have been considered as nonreactive (see above). In the present work, such a criterion has not been used in any case.

Recently, exact quantum mechanical results\textsuperscript{59,69} have also yielded values of \( \sigma_R(E_T) \) over a wide range of translational energies. Due to practical difficulties, the quantum mechanical calculations are limited to low values of the rotational quantum number of the \( \text{H}_2 \) molecule.

There is a remarkable general concordance between the QCT results and exact quantum mechanical ones, not only in the total cross sections, but also in more detailed reactivity functions and product state distributions as already discussed in previous work.\textsuperscript{32,67}

Figure 8 displays a detailed comparison of QM \( \sigma_R(E_T) \) values from Refs. 59 and 69 and present QCT results. As can be seen, the agreement for \( v = 0 \) is better at low translational energies. At energies above 0.6 eV, QM results are systematically larger. The slight differences between the two QM calculations\textsuperscript{59,69} are probably due to the different potential energy surfaces used. For the reaction with \( v = 1 \), the concordance between QCT and QM is even better at total energies comparable to those of the \( v = 0 \) case. A similar agreement between QCT and QM results has been reported very recently by Zhao et al.\textsuperscript{70} for the \( \text{H} + \text{D}_2 \) isotopic analog of this reaction.

Several numerical models of varying complexity have been developed in an attempt to relate the reactivity attributes observed in the reactions of the \( A + BC \) type to the main topological features of the corresponding potential energy surface. Most of these models extend the original considerations of Polanyi about the steric requirements imposed on the dynamics by the PES.

The familiar line-of-centers model\textsuperscript{86} has been often invoked to explain the rise in \( \sigma_R(E_T) \) characteristic of reactions with a threshold; in fact, a modified line-of-centers
model which includes the dependence of the barrier height on the relative orientation of the colliding partners was applied to the H$_3$ system by Levine and Bernstein, who calculated the excitation function H + D$_2$ ($v = j = 0$) → HD + D and compared their results with the trajectory calculations by Blais and Truhlar. The agreement is very good at low energies, but the model calculations yield a slightly larger cross section than the QCT for the highest collision energy compared (1.30 eV). In a recent work on D + H$_2$, we have observed a similar deviation between the model calculations and the QCT results for translational energies beyond approximately 0.8 eV. The deviation grows with increasing collision energy and has been attributed by Levine to recrossing of trajectories from the products to the reactants valley. The recrossing mechanism would thus be responsible for the leveling off in the excitation function of D + H$_2$ obtained in trajectory calculations. A postthreshold rise similar to the one described is observed in our calculations (see Table I) for all the cases studied, the threshold being dependent on the particular $v, j$ case. The modified “line-of-centers” model can also account reasonably well for the evolution of the opacity function with growing collision energy: increase of $P(b)$ (for all $b$) and of the “cut-off” $b$ value (the maximum impact parameter for which reaction takes place) (see Figs. 9–11). The model gives a simple expression for the “cone of acceptance” (i.e., the range of orientations that can lead to reaction), but does not include rotation or reorientation effects during the collision.

Due to the symmetry of the PES of this system, the energy barrier to reaction is placed in the middle of the way from the reactants’ to the products’ valley. It is therefore interesting to consider the effects of vibration on the cross section, since in this case, the simple rationalizations mentioned in the introduction for reactions with an “early” and a “late” barrier do not apply.

The opacity functions of Figs. 9–11 as well as those from former trajectory calculations$^3$ for the H$_3$ system show that vibrational excitation of the molecule enhances the reactivity for each impact parameter and enlarges the range of impact parameters that lead to reaction. In their trajectory study of H + H$_2$($v$), Barg, Mayne, and Toennies discuss both effects and indicate that vibrational excitation results in an increase of the zero point energy, which, for a given impact parameter, widens the range of configurations of the three atoms that can lead to reaction. They further stress the fact that vibrational energy is perpendicular to the reactant channel, and once the saddle point has been reached, it should be more effective than translation in promoting reaction. The authors also suggest that reorientation effects tending to align the molecular axis with the direction of the incoming atom could be important near threshold. The fact that larger impact parameters lead to reaction with increasing $v$ is attributed by the authors to the larger amplitude of the vibrational motion that increases the anisotropy and thus the orienting character of the potential.

Levine$^{2,9}$ and co-workers have also analyzed the enhancement of the cross section for this reaction caused by vibrational excitation and have traced it back to the steric requirements imposed by the PES. The main effect of vibration would be to lower the angle-dependent barrier to reaction. In the spirit of the modified line-of-centers model commented above, a lowering of the angle-dependent barrier $E_0(\gamma)$ leads to an increase in the cross section for any given initial orientation (angle of attack) and to a wider range of initial orientations that can contribute to reaction. This opening up of the cone of acceptance upon vibrational excitation predicted by the model and verified by trajectory calculations of Schechter et al. for D + H$_3$($v$) and H + D$_2$($v$), results both in a larger $P(b)$ at each $b$ and in a larger range of reactive impact parameters with growing vibrational excitation of the molecule as indeed observed (see Figs. 9–11).

Schechter et al. also mention trajectory computations which would show that translational and vibrational excitations produce a similar enhancement in the cross section for this reaction. This may be the case at some energies, but away enough from threshold vibration is more efficient than translation in promoting the reaction as shown in the work of Barg, Mayne, and Toennies$^9$ and in Fig. 7 of the present...
TABLE I. Total reaction cross sections $\sigma_T^r$ (in $\text{Å}^2$) for the $\text{D} + \text{H}_2(\nu) \rightarrow \text{HD} + \text{D}$ reaction as a function of collision energy and of the initial rotational and vibrational quantum numbers of the $\text{H}_2$ molecule. Values in parentheses represent the 68% statistical confidence level.

<table>
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<td>1.014 (0.030)</td>
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<td>0.870 (0.050)</td>
<td>1.672 (0.070)</td>
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<td>0.351 (0.020)</td>
<td>1.220 (0.060)</td>
<td>2.064 (0.058)</td>
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</tr>
<tr>
<td>0</td>
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<td>0.100 (0.020)</td>
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<td>1.219 (0.060)</td>
<td>2.188 (0.073)</td>
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<td>0.445 (0.014)</td>
<td>1.400 (0.060)</td>
<td>2.472 (0.060)</td>
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<td>0.625 (0.019)</td>
<td>1.692 (0.044)</td>
<td>2.608 (0.076)</td>
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<tr>
<td>0</td>
<td>11</td>
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<td>0.908 (0.026)</td>
<td>2.000 (0.071)</td>
<td>2.794 (0.102)</td>
<td></td>
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<td>0</td>
<td>12</td>
<td>0.030 (0.010)</td>
<td>0.590 (0.040)</td>
<td>1.260 (0.060)</td>
<td>2.299 (0.062)</td>
<td>3.249 (0.095)</td>
</tr>
</tbody>
</table>

work.

The mentioned line-of-centers model could also help to understand the different efficiency of vibration and translation in promoting the reaction. The application of the model to the opacity functions of Figs. 9-11 would yield values of the translational threshold $E_T^0(\gamma = 0)$ and of the hard-sphere diameter $D$ that decrease and increase, respectively, with growing $\nu$. In fact, the actual potential barrier is higher for larger internuclear distances (larger $D$), but vibrational energy is used to surmount the barrier. The net effect is that the translational threshold gets smaller with vibrational excitation, but does not disappear even for $\nu = 2$. It is the persistence of this translational threshold which makes the cross section smaller for the higher vibrational levels at the same total energy and low $E_T$ (see Fig. 7). The rotational excitation of the $\text{H}_2$ molecule does not modify this effect. At higher collision energies, vibrational excitation, which implies as indicated lower $E_T^0(\gamma = 0)$ and higher $D$, would lead to larger $\sigma_T^r$.

A very interesting effect also pointed out by Levine and co-workers and related to the vibrational excitation in this reaction is the appearance, upon vibrational stretching of the molecule, of a well in the potential for a collinear configuration, best seen in a $V(R,\gamma)$ representation (where $R$ is the distance of the attacking atom to the center of mass of the molecule and $\gamma$ the angle of attack). Levine and Wu suggested that this well should give rise to resonances in the reaction dynamics. These resonances, though present in 3D quantum mechanical calculations for the lowest partial waves, do not show up in the recent exact QM calculations at least in the integral cross section. Results initially interpreted as giving evidence of the mentioned resonances are being now reconsidered.

The effects of rotational excitation on the total reaction...
cross section for reactions of an atom with a diatomic molecule have also deserved much attention. For the \( \text{H} + \text{H}_2(j) \) system, the fact that rotational excitation can inhibit reactivity was already noticed in the pioneering QCT calculations by Karplus, Porter, and Sharma\(^\text{26} \) who found that the threshold in the translational excitation function increased with growing \( j \). They interpreted this fact as due to the decrease of the "orienting effect" (which would drive the system to a collinear configuration) of the surface at higher \( j \). Polanyi and co-workers\(^\text{91} \) gave a qualitative explanation of the minimum in the rotational excitation function \( \sigma_R(E_R) \), present in this and other systems, in terms of two competing effects: the "orientation" effect (responsible for the decrease and present at low \( j \)) and the "energy" effect, which would cause the increase in \( \sigma_R(E_R) \) observed for high values of \( j \), i.e., higher values of the total energy.\(^\text{6} \) The orientation effect mentioned has indeed been shown in pictorial representations of trajectories.\(^\text{22} \)

Simplifying models like the modified line of centers one commented on before do not account for any reorientation of the colliding partners during the collision. It was thus necessary to develop more complex treatments in order to unveil the key features of the influence of rotational excitation on reactivity. These models imply the solution of the classical equations of motion with some dimensionality reducing approximations.

In particular, Loesch\(^\text{13,14} \) proposed a rotational sliding mass model for reactions of the \( \text{A} + \text{BC}(j) \) type, where \( \text{BC} \) is treated as a rigid rotor and only collisions with zero impact parameter are considered. This model was successfully tested against trajectory calculations on different surfaces and made possible, in the reactions analyzed, to establish a relationship between the shape of \( \sigma_R(E_R) \) and the anisotropic attributes (steric restrictions) of the potential energy surface. The approaching molecules experience torques caused by the mentioned anisotropy of the potential which can direct them, either away from or toward the favored geometry for reaction, thus defining a dynamical cone of acceptance distinct from the static one. In that respect, both the decline and the rise in \( \sigma_R(E_R) \) would be at least in some cases the result of a more general orientation effect. In a later treat-
sudden" (CIOS) approximation, which in addition to the approximation forcing \( \frac{dy}{dt} = 0 \) (where \( y \) is the orientation angle) during the collision. They performed total cross section calculations on a model system (not intended to fit any particular real system) and found that CCS was in very good qualitative agreement with the exact QCT calculations carried under the same conditions for all the mass combinations and translational energies they tried. The CIOS approximation, which by definition forbids the mixing of \( \gamma \) motion and motion along the reaction coordinate, was unable to reproduce the minima observed in \( \sigma_R (E_R) \) (i.e., the orientation effect) and could only account for the increase in \( \sigma_R (E_R) \) associated with the "energy" effect.

Levine and co-workers\(^{20-22}\) have also attributed the effects of rotation on total cross sections to dynamical reorientation of the reagents on the way to the barrier. They use the \( \gamma \), conserving approximation, the \( V(R, y) \) potential and discuss the reorientation in terms of the "physical" and the "chemical" shape of the molecule, as seen by the approaching atom. The physical shape is given by the equipotential contours which determine how close the atom can get to the molecule at a given collision energy. Usually, a closer approach is possible from certain directions, and in that case, the \( ABC \) system is said to be "oblate" if \( A \) can get closer to \( BC \) when \( y = 0 \) as compared with \( y = 90^\circ \), (cos \( y = \hat{R}_{BC} \hat{R}_{AB,BC} \)) and "prolate" for the opposite case. The chemical shape is defined by the location of the barrier to reaction. They show that for systems with an oblate physical shape (as is the case for \( H + H_2 \)) in the absence of molecular rotation, the forces outside the barrier tend to steer the reagents into the cone of acceptance; initial rotation would hinder this steering, leading thus to a decline in \( \sigma_R (E_R) \). The enhancement of the total cross section with rotational excitation is attributed to the anisotropy in the location of the chemical barrier.\(^{22}\)

Although the reducing dimensionality models just commented on differ in the details of their formulation and have often been tested against distinct reactions, they all share the central idea that dynamical reorientation caused by the anisotropy of the potential in the course of the reactive encounter is responsible for most of the observed effects of rotational excitation on reactivity.

In the spirit of these models, the more stringent the steric hindrances for a process and the closer the collision energy to the threshold for reaction, the more marked should be the effect of rotation on reactivity.

This is in qualitative agreement with the results of the present and previous calculations (see Table I and Figs. 2–6).

However, to the best of our knowledge, no numerical model results have been reported that reproduce the minimum in \( \sigma_R (E_R) \) for this concrete reaction on its well known potential energy surface.

B. Differential cross section and energy distribution among the reaction products

The dependence of the (c.m.) solid angle differential cross section on the translational, rotational, and vibrational energies of the reactants is depicted in Figs. 12–14. In most of the cases studied, the HD product is scattered predomi-

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**FIG. 11.** The same as Fig. 8 for the \( D + H_2 (v,j = 12) \rightarrow HD \) (all) + H.
nantly in the backward hemisphere with respect to the direction of the incoming D atom. Many of the angular distributions shown have a maximum at 180°. An increase in the collision energy (with \( v \) and \( j \) fixed) leads to wider and more forward angular distributions. The same effect is observed with growing vibrational quantum number for a given \( E_T \) and \( j \). The differential cross sections for the \( j = 4 \) case [which corresponds approximately to the minimum in \( \sigma_R(j) \) present at low \( E_T \)] are shown in Fig. 13. Such a moderate increase in the rotational energy does not greatly change the shape of the angular distributions for the higher collision energies, but has a noticeable effect for the lower values (\( E_T < 0.65 \)). A comparison of Figs. 12 and 13 and of the corresponding opacity functions (Figs. 9 and 10) shows that the initial decrease in \( \sigma_R(j) \) happens mainly for collisions with low impact parameters, which seem to correlate

with backward scattered HD product. A comparison between Figs. 9–11 and 12–14 also shows a relationship between forward scattering and collisions with high impact parameter. In general, the forward character of the angular distribution increases markedly in the cases where \( P(b) \) extends beyond \( b = 1.2 \) Å. Maxima of the angular distributions at c.m. angles clearly distinct from 180° are obtained just for values of the total energy higher than 2 eV.

Some of the present angular distributions can be compared to other theoretical calculations for \( D + H_2(v = 0,1) \rightarrow HD + H \) already mentioned in the discussion of the total cross section. The agreement with existing QCT results is very good. 34,42,75 Our differential cross sections from Fig. 12 show the same trend as the recent QM exact results by Zhang and Miller 59 (for \( v = 0,1; j = 0 \)) and by Zhao et al. 69 (for \( v = 0; j = 0,1 \)) except for the forward peak at the highest translational energies, which is unseen in our results, and for the already commented absolute value of the reaction cross section. A more detailed comparison between QCT and exact

FIG. 12. The solid angle differential cross section summed over all \( v' \) and \( f \) final states for the \( D + H_2(vj = 0) \rightarrow HD + H \) at several translational energies: small dashes, 0.25 eV; dotted line, \( E_T = 0.35 \) eV; dots, \( E_T = 0.45 \) eV; dashed line, \( E_T = 0.65 \) eV; solid line, \( E_T = 1.00 \) eV. Lower panel, \( v = 0 \); middle, \( v = 1 \); upper, \( v = 2 \). Uncertainties, not shown for clarity, are similar to those of Fig. 1(b) (see text).

FIG. 13. The solid angle differential cross section for the \( D + H_2(vj = 4) \rightarrow HD + H \) reaction. Symbols are the same as in Fig. 12.
which are predicted to be narrower than those from the QCT. If the orientation dependence of the barrier is not contemplated, the model velocity distributions differ considerably (being broader and greater) from the experimental ones.\textsuperscript{42}

The simple arguments contained in the mentioned models can probably account for the translational energy dependence of the c.m. angular distributions of Fig. 12 of the present work, not only for \( \text{D} + \text{H}_2 (v = 0) \), but also for the reaction with \( v = 1 \) and \( v = 2 \).

The partition of the available energy among the products' degrees of freedom is represented in Figs. 15–20 and in Table II. Figures 15–17 show the dependence of the average translational \( \langle E_T \rangle \), rotational \( \langle E_R \rangle \), and vibrational \( \langle E_v \rangle \) energy of the products on the translational, rotational, and vibrational excitations of the reactants. The probability density functions of the fractions of rotation \( f_R \) and translation \( f_T \) of the products are depicted in Figs. 18–20. Table II lists the cross sections for the production of HD in a given vibrational state \( v' \).

An inspection of Figs. 15–17 reveals some interesting

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**FIG. 14.** The solid angle differential cross section for the \( \text{D} + \text{H}_2 (v, j = 12) \rightarrow \text{HD} + \text{H} \) reaction. Symbols are the same as in Fig. 12.

**FIG. 15.** Average values of the products' translational \( \langle E_T \rangle \) (circles), rotational \( \langle E_R \rangle \) (triangles), and vibrational \( \langle E_v \rangle \) (squares) energy vs the \( \text{H}_2 \) rotational energy \( E_R (\text{H}_2) \) for the \( \text{D} + \text{H}_2 (v = 0) \) reaction at several collision energies (top left-hand corner in each box). All the units in electron-volts.
features that should be stressed. Although in all the cases considered there is a certain degree of interconversion between the reactants' and products' energy modes, most of the translational excitation of the reactants appears as translational energy in the products and the same is also true for the vibrational excitation. In fact, the average translational energy of the products does not depend at all on the vibrational quantum number of \( \text{H}_2 \), and the average vibrational energy of the HD product is nearly independent of the collision energy. These general assertions need, however, some precisions. Part of the vibrational energy \( (E_v) \) of the \( \text{H}_2 \) molecule goes always to the other products modes \( (E_T' \) and \( E_R' \) ) in collisions with low \( E_T \) and low \( E_R \). In the \( v = 2 \) case, \( E_v' \) decreases somewhat with increasing \( E_T \), especially for the higher \( j \). On the other hand, the average translational energy of the reactants \( E_T' \) is higher than the collision energy for low \( E_T \) and low \( j \). This is no longer the case with growing collision energy. Increasing either the translational or the vibrational energy of the reactants leads always to an increase in the rotational energy of the products.

The initial rotation of the \( \text{H}_2 \) molecule goes to all three products' modes as is apparent from Figs. 15-17. In all cases, \( E_R \) grows linearly with \( E_R' \). At the lower collision energies, there is an \( E_R \) range, corresponding to the region around the minimum in \( \sigma_R \) (see Figs. 2 and 3) for which \( E_R' \) remains nearly constant with increasing \( E_R \) as already commented on in previous work.\(^{35}\) For higher \( j \) and for higher translational energies, both \( E_T' \) and \( E_R' \) also grow linearly with \( E_R \). In any case, the fraction of energy appearing as products' rotation is relatively low (always less than one third). This suggests that rotational excitation of \( \text{H}_2 \) is efficient for the promotion of the reaction under study as far as it can be converted to a significant extent into translational or vibrational energy in the course of the reactive encounter.
The products' translational distributions represented as $P(f'_T)$ in Figs. 18–20 are clearly asymmetric for low $E_T$ and $j$ with a definite peak at relatively low $f'_T$ and a long tail extending to higher $f'_T$. In the $v = 0$ case, an increase in the translation or rotation of the reactants makes the $P(f'_T)$ distributions broader and more symmetric. For $v = 1$ and $v = 2$, the $P(f'_T)$ distributions also become broader, especially with growing $E_T$, and the peak shifts to lower $f'_T$. The asymmetry remains here over the range of conditions studied. The distributions of rotational energy in the products $P(f'_R)$ are much more sensitive to the variation of $E_T$ and $E_R$ than to the vibrational quantum number of $H_2$. The $P(f'_R)$ distributions always widen markedly with increasing collision energy. For the lower $E_T$, these distributions broaden significantly with $j$; however, for the higher values of the initial translational energy, the shape of $P(f'_R)$ does not change much with growing $j$.

The relative populations of the HD vibrational levels that can be deduced from Table II also become broader with any increase in the energy of the reactants, irrespective of the mode $E_T, E_R, E_v$, in which this energy is localized. For the lower $E_T$ and the lower $j$, the reaction is predominantly adiabatic in the vibrational quantum number. The most populated product vibrational state shifts to higher $v'$ with increasing $j$ and to lower $v'$ with growing $E_T$.

The general good concordance, with small differences, between the cross sections for the production of a given vibrational state $\sigma_R (v_j = 0 \rightarrow v')$ given by QCT and by recent exact QM calculations was already commented on in a previous work for $v = 0$. A similar agreement is obtained between the present results and those by Zhang and Miller.
excitation in excess of the barrier height $\Delta E_T$ should give rise to a more compressed intermediate configuration, which is more repulsive and would lead to enhanced products’ translation $\Delta E'_T$. On the contrary, a corresponding increase in vibrational excitation $\Delta E_v$ would lead most often to more extended intermediate configurations, smaller repulsion, and enhanced product vibration. These effects were termed, respectively, “induced repulsive energy release” ($\Delta E_T \rightarrow \Delta E'_T$) and “induced attractive energy release” ($\Delta E_v \rightarrow \Delta E'_v$). If one takes into account the fact that with increasing collision energy more bent configurations become accessible for reaction, and that collisions with bent configurations lead more easily to rotational excitation, one can write $\Delta E_T \rightarrow \Delta E'_T + \Delta E'_R$. By the same reasoning, an excess in vibrational energy also widens the acceptance cone (see above) and consequently gives rise to an increase in rotational excitation $\Delta E_v \rightarrow \Delta E'_R$. In fact, all the qualitative trends just described are present in the results of this work (see Figs. 15–17).

IV. SUMMARY AND CONCLUSIONS

Classical trajectory calculations have been carried out to study the $D + H_2 (v_f) \rightarrow HD + H$ reaction dynamics. The influence of translational, rotational, and vibrational energies of the reactants has been investigated by running QCT trajectories on the LSTH potential energy surface in the range of collision energy from 0.25 to 1 eV, $H_2$ rotational quantum number up to 12, and vibrational quantum number $v = 0, 1, 2$. Total integral and differential cross sections, as well as the disposal of energy among the products’ degrees of freedom, have been investigated.

Both translational and vibrational excitation of the reactants produce a monotonic increase in the total reaction cross section. For values of the total energy away enough from threshold, vibration is more efficient in promoting the reaction.

For the three vibrational numbers studied, the rotational excitation functions show a minimum at the lower collision energies at $\beta \approx 4–6$. This minimum disappears with increasing translational energy and its relative depth decreases with growing $v$.

The center-of-mass angular distributions of the scattered HD are predominantly backward at low energies, with a maximum at $180^\circ$ with respect to the direction of the incoming D atom, but they broaden considerably and become more forward with increasing total energy. The distributions of energy in the different products’ modes also broaden markedly with growing energy. It is significant that translational and vibrational energies are largely adiabatic with respect to each other, while rotational energy interconverts more efficiently with the other two modes in the course of reactive collisions.

Although a detailed comparison between classical and quantum results is not the main aim of this work, it should be noted that with the level of resolution of the present QCT calculations (which implies summation at least over the products’ rotational quantum numbers), the agreement with QM exact data is fairly good with slight differences; this

FIG. 20. The same as Fig. 18 for the $D + H_2 (v = 2j) \rightarrow HD$ (all) + H reaction.
TABLE II. Total reaction cross sections (in Å²) for the D + H₂(υ') → HD(υ') + H at several collision energies (E_r). Values in parentheses are standard deviations of the last digit.

<table>
<thead>
<tr>
<th>E_r (eV)</th>
<th>υ'</th>
<th>j = 0</th>
<th>j = 4</th>
<th>j = 12</th>
<th>j = 0</th>
<th>j = 4</th>
<th>j = 12</th>
<th>j = 0</th>
<th>j = 4</th>
<th>j = 12</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.25</td>
<td>0</td>
<td>0.295(9)</td>
<td>0.078(3)</td>
<td>0.19(2)</td>
<td>0.40(3)</td>
<td>0.22(3)</td>
<td>0.35(4)</td>
<td>1</td>
<td>0.680(1)</td>
<td>0.151(5)</td>
</tr>
</tbody>
</table>

good agreement, already shown in former works for υ = 0, is demonstrated here for the υ = 1 case. Where they can be compared, our results also show a general good concordance with previous QCT calculations and lie mostly within experimental error.

It is also interesting to observe that not only classical mechanics, but also very simple models can render, sometimes in a semiquantitative way, many of the dynamical characteristics of the reaction. Particularly successful have been hard-sphere models with an angle-dependent barrier in order to rationalize the effects of translation and vibration on total cross sections and angular distributions. Hard-sphere models are not sufficient to account for the role of rotation on the reactivity and it has been necessary to develop more complex treatments that consider explicitly a dynamical reorientation of the reactants in the course of the collision.

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