I. INTRODUCTION

The nuclear mass region with proton number $Z \approx 60$ and neutron number $N \approx 90$ is receiving much attention at present, both experimental and theoretically, because it is a region where nuclear structure collective effects of different natures overlap [1]. Particularly interesting in this context is the interplay between quadrupole transitional properties in $N \approx 90$ isotones and octupole deformation manifestations in nuclei with proton $Z \approx 56$ and neutron $N \approx 88$ numbers. On one hand, isotones with $N \approx 90$ have been found as empirical realizations [2] of the critical point symmetry $X(5)$, introduced [3] to describe analytically the first-order phase transition from spherical [$U(5)$] to well-deformed [$SU(3)$] nuclei. Such critical point symmetries have recently been studied within various microscopic approaches, either relativistic or nonrelativistic (see, for example, Refs. [4–7] and references therein).

However, it is well known [1] that there is a tendency towards octupolarity around particular neutron/proton numbers, namely $N/Z = 34, 56, 88$, and 134. The emergence of octupolarity in these nuclear systems can be traced back to the structure of the corresponding single-particle spectra which exhibit maximum coupling between states of opposite parity, where the $(N + 1, l + 3, j + 3)$ intruder orbitals interact with the $(N, l, j)$ normal-parity states through the octupole component of the effective nuclear Hamiltonian. When the mixing is strong enough, the nucleus displays an octupole deformed ground state [1]. In particular, for nuclei with $Z \approx 56$ ($N \approx 88$) the coupling between the proton (neutron) single-particle states $h_{11/2}$ ($i_{13/2}$) and $d_{5/2}$ ($f_{7/2}$) has been considered as mainly responsible for mean-field ground-state octupolarity.

The search for signatures of stable octupole deformations in atomic nuclei has been actively pursued during the last decades [1,8]. As a main feature, octupole deformed even-even nuclei display particularly low-lying negative-parity $1^-$ states. In the case of stable octupole deformations, the $0^+$ and $1^-$ states represent the members of parity doublets, giving rise to alternating-parity rotational bands with enhanced $E1$ transitions among them. These fingerprints of octupole deformations have already been found in the particular regions mentioned above, but especially in the rare-earth and actinide regions [1,8].

For the sample of nuclei considered in the present study (i.e., $^{146–154}$Sm and $^{148–156}$Gd), experimental fingerprints have been obtained through the observation of octupole correlations at medium spins, as well as the crossing of the octupole and the ground-state band, pointing to the fact that reflection symmetric and asymmetric structures coexist in $^{150}$Sm [9] and $^{148}$Sm [10]. A recent study [11] has analyzed the lowest four negative-parity bands in $^{152}$Sm and has found an emerging pattern of repeating excitations, built on the $0_2^+$ level and similar to that of the ground state, suggesting a complex shape coexistence in $^{152}$Sm.

The experimental findings [9–11] mentioned above already suggest that it is timely and necessary to carry out systematic studies of the quadrupole-octupole interplay in this and other regions of the nuclear chart, starting from modern (global) relativistic [12,13] and/or nonrelativistic [13–16] nuclear energy density functionals (EDFs), with reasonable predictive power all over the nuclear chart.

Let us remark that the microscopic study of the dynamical (i.e., beyond mean field) quadrupole-octupole coupling in the considered Sm and Gd isotopes is also required to better understand the extent to which a picture of independent quadrupole and octupole excitations persists or breaks down for nuclei with neutron number $N \approx 88$. This, together with the available experimental fingerprints [9–11] for octupolarity in the region, is one of the main reasons driving our choice of the nuclei $^{146–154}$Sm and $^{148–156}$Gd as a representative sample to test the performance of the different approximations and EDFs considered in the present study.

From a theoretical perspective, many different models have been used to describe octupole correlations in atomic nuclei.
For a detailed survey the reader is referred, for example, to Ref. [1]. Calculations based on the shell-correction approach with folded Yukawa deformed potentials [17,18], as well as calculations based on Woods-Saxon potentials with various models for the microscopic and macroscopic terms [19,20], predicted a significant stabilization of octupole deformation effects in various nuclear mass regions. Pioneer Skyrme-HF + BCS calculations including the octupole constraint and restoring parity symmetry were carried out in Ref. [21]. Subsequent calculations in Ref. [22] included both quadrupole and octupole constraints at the same time but at the mean-field level only. However, microscopic studies of octupole correlations with Skyrme and Gogny EDFs, both at the mean-field level and beyond with different levels of complexity, have already been reported (see Refs. [23–33] and references therein) for several regions of the nuclear chart. Theoretical studies in the Sm region include mean-field-based calculations with the collective Hamiltonian and the Gogny force [33], the IBM study with sp$df$ bosons of Ref. [34] or the collective models using a coherent coupling between quadrupole and octupole modes [35], and new parametrizations of the quadrupole and octupole modes [36]. Nonaxial pearlike shapes in this region were considered, for example, in Refs. [37]. Additionally, the isotopes 146–156Sm have been investigated very recently within the constrained reflection-asymmetric relativistic mean-field (RMF) approach [38] based on the parametrization PK1 [39] for the RMF Lagrangian together with a constant gap BCS approximation for pairing correlations.

In the present work, we investigate the interplay between octupole and quadrupole degrees of freedom in the sample of nuclei 146–154Sm and 148–156Gd. We use three different levels of approximation. First, the constrained (reflection-asymmetric) Hartree-Fock-Bogoliubov (HFB) framework is used as a starting point providing energy contour plots in terms of the (axially symmetric) quadrupole $Q_{20} = \langle \Phi | \hat{Q}_{20} | \Phi \rangle$ and octupole $Q_{30} = \langle \Phi | \hat{Q}_{30} | \Phi \rangle$ moments (where $| \Phi \rangle$ is the corresponding HFB intrinsic wave function). Within this mean-field framework we pay attention to the shape changes in the considered nuclei and their relation with the underlying single-particle spectrum [1,32,40]. As is discussed later, the $(Q_{20}, Q_{30})$ mean-field potential energy surfaces (MFPES) obtained for the nuclei 146–154Sm and 148–156Gd are, in most of the cases, very soft along the $Q_{30}$ direction, indicating that the (static) mean-field picture is not enough and that a (dynamical) beyond-mean-field treatment is required. Therefore, both the minimization of the energies obtained after parity projection of the intrinsic states [21,30,33] and quadrupole-octupole configuration mixing calculations in the spirit of the generator coordinate method (GCM) [41] are subsequently carried out. The analysis of the two sets of results makes it possible to disentangle the role played in the dynamics of the considered nuclei by the restoration of the broken reflection symmetry and the fluctuations in the $(Q_{20}, Q_{30})$ collective coordinates. Similar calculations with the Skyrme functional where carried out in Ref. [26] for a lead isotope.

To the best of our knowledge, the hierarchy of approximations [i.e., reflection-asymmetric HFB, parity projection, and $(Q_{20}, Q_{30})$-GCM] considered in the present work belong, at least for the case of the Gogny-EDF, to the class of unique and state-of-the-art tools for the microscopic description of quadrupole-octupole correlations in atomic nuclei. Let us also stress that the two-dimensional GCM (2D-GCM) framework used in the present study represents an extension of the treatment of octupolarity reported in Refs. [32,33], where a 1D collective Hamiltonian based on several approximations and parameters extracted from $Q_{30}$-constrained HFB calculations was considered. Here, however, the octupole and quadrupole degrees of freedom are explored simultaneously and the kernels involved in the solution of the corresponding Hill-Wheeler equation [41] are computed without assuming a Gaussian behavior of the norm overlap or a (second-order) expansion over the nonlocality of the Hamiltonian kernel. Therefore, the present study for the selected set of Sm and Gd nuclei, to the best of our knowledge the first of this kind for the case of the Gogny-EDF, may also be regarded as a proof of principle concerning the feasibility of the calculations to be discussed later. Pioneer calculations along the same lines considered in the present study, but based on the Skyrme-EDF, have been carried out in Refs. [26,42].

In addition to the standard Gogny-D1S [15] parametrization, which is taken as a reference, the D1M parametrization [43] is also considered. The functional Gogny-D1S has a longstanding tradition and it has been able to describe many low-energy experimental data all over the nuclear chart with reasonable predictive power at both the mean-field level and beyond (see, for example, Refs. [15,27–31,44–54] and references therein). However, the D1M parametrization [43] that was tailored to provide a better description of masses is now proving its merits in nuclear structure studies not only in even-even nuclei [40,43,54–58], but also in odd nuclei in the framework of the equal filling approximation (EFA) [54,56–58]. In this paper the results of both D1S and D1M are compared to verify the robustness of our predictions with respect to the particular version of the interaction and to test the performance of D1M in the present context of quadrupole-octupole coupling.

The paper is organized as follows. In Secs. II, III, and IV we briefly describe the theoretical formalisms used in the present work and, subsequently, the results obtained with them. Mean-field calculations are discussed in Sec. II. Parity projection and configuration mixing results are presented in Secs. III and IV, respectively. In particular, in Sec. IV special attention is paid to beyond-mean-field properties in the considered nuclei—dynamical octupole and dipole moments, correlation energies, reduced transition probabilities $B(E1)$ and $B(E2)$, as well as energy splittings—and their comparison with available experimental data. Finally, Sec. V is devoted to the concluding remarks and work perspectives.

II. MEAN-FIELD SYSTEMATICS

The aim of the present work is the study of the quadrupole-octupole dynamics in selected Sm and Gd isotopes with neutron number $84 \leq N \leq 92$. Three different levels of approximation are considered: the HFB method with constraints in the relevant degrees of freedom, parity projection...
(with minimization of the energy after projection), and the GCM with \( Q_{20} \) and \( Q_{30} \) as collective coordinates. For a detailed survey on the three techniques, the reader is referred to Ref. [41]. The Gogny EDF is used consistently in the three methods both with the D1S and D1M parametrizations.

First, \((Q_{20}, Q_{30})\)-constrained HFB calculations are performed for the nuclei \(^{146-154}\text{Sm}\) and \(^{148-156}\text{Gd}\) to obtain a set of states \(|\Phi(Q)\rangle\) labeled by their corresponding multipole moments \(Q = (Q_{20}, Q_{30})\). The \(K = 0\) quadrupole \(Q_{20}\) and octupole \(Q_{30}\) moments are given by the average values

\[
Q_{20} = \langle \Phi | z^2 - \frac{1}{2}(x^2 + y^2) | \Phi \rangle \tag{1}
\]

and

\[
Q_{30} = \langle \Phi | z^3 - \frac{1}{2}(x^2 + y^2)z | \Phi \rangle. \tag{2}
\]

Axial and time reversal are self-consistent symmetries in the mean-field calculations. As a consequence of the axial symmetry imposed on the HFB wave functions \(|\Phi\rangle\), the mean values of the multipole operators \(\hat{Q}_{2\mu}\) and \(\hat{Q}_{3\mu}\) with \(\mu \neq 0\) are zero by construction. Aside from the constraints on the quadrupole and octupole moments, a constraint on the center-of-mass operator is used to place it at the origin of coordinates to prevent spurious effects associated with center-of-mass motion. The HFB quasiparticle operators \((\hat{a}_k^\dagger, \hat{a}_k)\) [41] have been expanded in an axially symmetric harmonic-oscillator (HO) basis \((\hat{c}_l^\dagger, \hat{c}_l)\) containing 13 major shells as to grant convergence for all the observable quantities. For the solution of the HFB equation, an approximate second-order gradient method [59] is used.

The MFPEs have been computed in a grid with \(Q_{20}\) in the range from \(-30\) to \(30\) in steps of \(0.6\) b and the octupole moment \(Q_{30}\) in the range from \(0\) b\(^3/2\) to \(3.75\) b\(^3/2\) in steps of \(0.25\) b\(^3/2\). Negative values of the octupole moment are not computed explicitly as the corresponding wave function can be obtained from the positive \(Q_{30}\) one by applying the parity operator. As the Gogny EDF is invariant under parity (see Refs. [44,45] for a discussion of the meaning of symmetry invariance for density dependent “forces”) the energy has the property \(E_{\text{HFB}}(Q_{20}, Q_{30}) = E_{\text{HFB}}(Q_{20}, -Q_{30})\) and therefore is an even function of the octupole moment. For this reason, in the graphical representation of the PES only positive values of \(Q_{30}\) are considered.

The MFPEs obtained for the nucleus \(^{150}\text{Sm}\), with the parametrizations D1S and D1M of the Gogny-EDF, are shown in Fig. 1 as an illustrative example of our mean-field results. For the sake of presentation, quadrupole and octupole moments have been constrained in the plots to the ranges \(-10b \leq Q_{20} \leq 20b\) and \(0b^{3/2} \leq Q_{30} \leq 3.75b^{3/2}\), respectively. The similitude between the D1S and D1M results in the \(Q_{20}\) and \(Q_{30}\) directions is remarkable. In previous calculations in other regions and looking at different physical effects [40,54,56–58] we have already noticed the same similitude between the D1S and D1M results. Focusing on the MFPEs, the absolute minimum is located in the prolate side at a finite value of the octupole moment. The minimum is very shallow along the \(Q_{30}\) direction. Another minimum is observed in the oblate side, but this time centered at \(Q_{30} = 0\). For the other nuclei considered the energies look similar and therefore they are not shown. The most relevant mean-field quantities for the ground states are summarized in Tables I and II. To better understand the quadrupole deformation properties of the studied nuclei, the reflection symmetric (i.e., \(Q_{30} = 0\)) mean-field potential energy curves (MFPECs) are depicted for all the considered nuclei in Fig. 2. A transition from weakly deformed ground states in the \(N = 84\) nuclei \(^{146}\text{Sm}\) and \(^{148}\text{Gd}\) to well (quadrupole) deformed ground states in \(^{152-154}\text{Sm}\) and \(^{154-156}\text{Gd}\) (prolate moments \(6.6b \leq Q_{20} \leq 7.8b\)) is observed. In most of the isotopes except the lightest ones an additional minimum is observed in the oblate side. This minimum may become a saddle point (see Ref. [6] for examples) once the \(\gamma\) degree of freedom is considered. Nevertheless, the simultaneous consideration of triaxial quadrupole and octupole moments lies outside of the scope of the present study. Investigation along these lines is in progress and will be reported elsewhere.

From Tables I and II, we observe the onset of an octupole deformed regime at the \(N = 88\) nuclei \(^{150}\text{Sm}\) and \(^{152}\text{Gd}\). These nuclei mark the borders of another shape transition from octupole deformed ground states in \(^{148}\text{Sm}\) and \(^{150}\text{Gd}\) to quadrupole deformed and reflection symmetric ground states in \(^{152}\text{Sm}\) and \(^{154}\text{Gd}\). Consistent with the breakdown of the left-right symmetry in their ground states, the \(^{148,150}\text{Sm}\) and \(^{150,152}\text{Gd}\) isotopes exhibit a nonzero (static) dipole moment \(D_0\). It is computed as the ground-state average value of the dipole operator

\[
\hat{D}_0 = \frac{N}{A} \hat{\varepsilon}_{\text{prot}} - \frac{Z}{A} \hat{\varepsilon}_{\text{neut}} \tag{3}
\]
along the symmetry z axis. The values of \( D_0 \) tend to be smaller for D1M than for D1S. This is not surprising owing to the delicate balance between single-particle orbital properties that enter in the definition of the dipole moment [29]. Another

quantity of interest is the mean-field octupole correlation energy \( E^{\text{MF}}_{\text{corr}} = E^{\Omega}_{\text{HFB}} - E^{\Omega}_{\text{MF}} \) corresponding to the energy gain by allowing octupole deformation. For example, the values obtained for \(^{150}\text{Sm} \) and \(^{152}\text{Gd} \) are 204 and 43 keV (105 and 6 keV) for the functional D1S (D1M), respectively. These very low values are a clear indication of the softness of the octupole minima in those nuclei. Because the minima are also soft along the \( Q_{20} \) direction, both the quadrupole and octupole degrees of freedom have to be considered at the same time in a dynamical treatment of the problem [9–11].

In Tables I and III, the proton \( E_p(Z) \) and neutron \( E_p(N) \) pairing energies are also listed. They are computed in the usual way as \( E_p(\tau) = -1/2T[\Delta(\tau)\kappa^*(\tau)] \) in terms of the pairing field \( \Delta \) and the pairing tensor \( \kappa \) for each isospin \( \tau = Z, N \). Moving along isochainic chains, the smallest neutron pairing energy corresponds to the \( N = 88 \) nuclei \(^{150}\text{Sm} \) and \(^{152}\text{Gd} \), which are precisely the ones providing the largest values of the mean-field octupole correlation energy \( E^{\text{MF}}_{\text{corr}} \). The significant lowering of the neutron pairing energies in these nuclei is a consequence of the low-level density typical of deformed (quadrupole or octupole) minima, the Jahn-Teller effect. However, proton pairing energies tend to decrease as a function of the neutron number. In general, the proton and neutron pairing energies for the two Gogny-EDFs considered follow the same trend, the only relevant difference being in their absolute values that tend to be slightly larger for D1M.

Before concluding this section, we turn our attention to single-particle properties. The appearance of quadrupole and/or octupole deformation effects is strongly linked to the position of the Fermi energy in the single-particle spectrum [1,32,40,55,61]. Therefore, the evolution of the single-

\[
\begin{array}{ccccccc}
\text{Nucleus} & E_p(Z) & E_p(N) & D_0 & Q_{20} & Q_{30} & E_p(Z) & E_p(N) & D_0 & Q_{20} & Q_{30} \\
154\text{Sm} & -15.22 & -4.27 & 0.00 & 0.66 & 0.00 & -16.11 & -5.35 & 0.00 & 0.00 & 0.00 \\
152\text{Gd} & -14.22 & -3.63 & 0.19 & 3.60 & 0.75 & -15.43 & -5.03 & 0.05 & 3.00 & 0.25 \\
152\text{Gd} & -12.69 & -3.02 & 0.27 & 4.80 & 1.00 & -13.18 & -4.76 & 0.15 & 4.80 & 0.50 \\
154\text{Gd} & -7.63 & -6.26 & 0.00 & 7.20 & 0.00 & -9.25 & -6.88 & 0.00 & 6.60 & 0.00 \\
156\text{Gd} & -7.18 & -4.86 & 0.00 & 7.80 & 0.00 & -7.66 & -6.20 & 0.00 & 7.80 & 0.00 \\
\end{array}
\]

\[\text{TABLE II.} \text{ The same as Table I but for the isotopes} \ 148-156\text{Gd.}\]
neutron spectrum for the \( Q_{30} \) values corresponding to the minimum at around 2 MeV. A \( j = 7/2 \) is formed at an energy of around \(-4 \) MeV; one with \( j = 5/2 \) is located at around \(-6 \) MeV and finally another one with \( j = 3/2 \) shows up at an energy of \(-8 \) MeV. The same grouping of levels can also be observed in the SPEs for protons at similar values of the octupole moment. These quasi-\( j \) orbitals are the consequence of the relationship between classical closed periodic orbits for specific octupole deformed shapes and the corresponding quantum orbitals that have to show an integer ratio between the radial and angular frequencies (see Ref. [61], Vol II, p. 587, for a general discussion and also Ref. [29] for specific examples in rare-earth nuclei).

### III. Parity Projection

Although the HFB framework discussed in the previous section is a valuable starting point, it produces MFPECS with very soft minima along the \( Q_{30} \) direction in the nuclei considered. This suggests the important role played by both types of dynamical correlations: the one associated with symmetry restoration and the other to configuration mixing. Symmetry restoration is considered in this section while configuration mixing is presented in the next section.

There are two spatial symmetries broken in the present calculations. One is rotational symmetry with the quadrupole moment as the relevant parameter and the other is reflection symmetry (parity) with the octupole moment as the relevant quantity. From the discussion of the mean-field results it is clear that the softest mode is the octupole moment and therefore the most relevant symmetry to be restored is parity. Obviously, it would be desirable to restore also the rotational symmetry as well as particle number. This combined symmetry restoration is feasible but, when combined with the configuration mixing of the next section, becomes a very demanding computational task not considered in this paper.

The quantum interference typical of the GCM framework could be directly used to restore the parity symmetry by choosing appropriate weights for the configurations with multipole moments \( (Q_{20}, Q_{30}) \) and \( (Q_{20}, -Q_{30}) \) [33]. However, to disentangle the relative contribution of the parity restoration correlations as compared with the ones of the GCM configuration mixing, we have carried out explicit parity projection calculations.

To restore parity symmetry [21,30] we build positive \((\pi = +1)\) and negative \((\pi = -1)\) parity-projected states \( |\Phi^\pi(Q_{20}, Q_{30})\rangle = \hat{P}^\pi |\Phi(Q_{20}, Q_{30})\rangle \) by applying the parity projector \( \hat{P}^\pi \) to the intrinsic configuration. The parity projector is a linear combination of the identity and the parity operator \( \hat{\Pi} \) given by

\[
\hat{P}^\pi = \frac{1}{2}(1 + \pi \hat{\Pi}).
\]

The projected energies, used to construct parity-projected potential energy surfaces (to be called PPPES in what follows), are labeled with the multipole moments \( Q = (Q_{20}, Q_{30}) \) of the intrinsic state and read [63]

\[
E_\pi(Q) = \frac{\langle \Phi(Q)\hat{H}[\rho(\vec{r})]\Phi(Q)\rangle}{\langle \Phi(Q)\Phi(Q)\rangle} + \pi \frac{\langle \Phi(Q)\hat{H}[\theta(\vec{r})]\Phi(Q)\rangle}{\langle \Phi(Q)\Phi(Q)\rangle} + \frac{\pi}{2}
\]

\[
\frac{\langle \Phi(Q)\hat{I}\Phi(Q)\rangle}{\langle \Phi(Q)\Phi(Q)\rangle}.
\tag{5}
\]

The parity-projected mean value of proton and neutron number, \( \langle Z \rangle \) and \( \langle N \rangle \), respectively, usually differ from the nucleus’ proton \( Z_0 \) and neutron \( N_0 \) numbers. To correct the energy for this deviation we have replaced \( \hat{H} \) by \( \hat{H} - \lambda_Z (\hat{Z} - Z_0) - \lambda_N (\hat{N} - N_0) \), where \( \lambda_Z \) and \( \lambda_N \) are chemical potentials for protons and neutrons, respectively [30,64,65].

In the case of the Gogny-EDF, as well as for Skyrme-like EDFs, the definite expression for the projected energy (5) depends on the prescription used for the density-dependent part of the functional. In this work, we resort to the so-called \textit{mixed density} prescription that amounts to consider the standard intrinsic density

\[
\rho(\vec{r}) = \frac{\langle \Phi(Q)\hat{\rho}(\vec{r})\Phi(Q)\rangle}{\langle \Phi(Q)\Phi(Q)\rangle}
\tag{6}
\]

and the density

\[
\theta(\vec{r}) = \frac{\langle \Phi(Q)\hat{\rho}(\vec{r})\Phi(Q)\rangle}{\langle \Phi(Q)\Phi(Q)\rangle}
\tag{7}
\]

in the evaluation of the first and second terms in Eq. (5), respectively. The \textit{mixed density} prescription has been widely and successfully used in the context of projection and/or configuration mixing techniques (see, for example, [13,44,45,66–68] and references therein). In fact, this is the only prescription that guarantees various consistency requirements within the EDF framework [44,63,69]. Even though this prescription has some drawbacks, as put into evidence recently [69–71], the use of
FIG. 3. (Color online) Single-particle energies (see text for details) in $^{150}$Sm are plotted as a function of the quadrupole moment $Q_{20}$ (in barns) up to the value corresponding to the ground-state minimum. From there on, the plot continues with the representation of the SPEs as a function of the octupole moment $Q_{30}$. In the part of the plot where the SPEs are plotted versus $Q_{20}$, solid (dashed) curves stand for positive (negative) parity levels. The thick (red) dashed line in each plot represents the chemical potential. In the part of the plot where the SPEs are plotted versus $Q_{30}$, some levels around the Fermi level are labeled with twice their $J_z$ value. Panels (a) and (b) [(c) and (d)] correspond to results obtained with D1S [D1M] EDFs. Panels (a) and (c) [(b) and (d)] correspond to protons [neutrons].

Alternative expressions, obtained by considering explicitly the $Q_{30} = 0$ limit [30], are required for a sound numerical evaluation of those quantities. Note, however (see Fig. 5), that the negative-parity projected energy increases rapidly while approaching the $Q_{30} = 0$ configuration, and therefore it does not play a significant role in the subsequent discussion of the corresponding PPPESs. As a consequence, we have omitted this quantity along the $Q_{30} = 0$ axis.

As in the mean-field case, the results with D1S and D1M show a striking similarity and therefore only the D1S results are discussed. The comparison between the MFPESs in Fig. 1 and the PPPESs in Fig. 4 clearly illustrates the topological changes induced by the restoration of the reflection symmetry. In general, the quadrupole moments $Q_{20}$ corresponding to the absolute minima of the PPPESs, remain quite close to the ones obtained at the HFB level (see Tables I and II), and other prescriptions, like the one based on the projected density, are pathologically ill defined when applied to the restoration of spatial symmetries [72].
increasing their values as more neutrons are added for each of the Sm and Gd chains. However, the situation is quite different along the $Q_{30}$ direction. To obtain a more quantitative understanding of the evolution of the PPPESs, we have plotted in Fig. 5 the parity-projected energy curves for self-consistent $Q_{20}$ values, as a function of the octupole moment $Q_{30}$ for the nucleus $^{150}$Sm. The corresponding HFB energy curves are also included for comparison. For $^{150}$Sm, and all the other nuclei considered in the present study, the negative-parity curves always show a well developed minimum at $Q_{30}$ values in the range 1.50–1.75 b$^{3/2}$. However, and regardless of the particular version of the Gogny-EDF employed, the $\pi = +1$ curves always display a characteristic pocket $[1,23,30]$ with a minimum at $Q_{30} = 0.50–0.75$b$^{3/2}$. In the spirit of the variation after projection procedure, the configuration yielding the minimum of the positive (negative)-parity-projected energy as a function of $Q_{30}$ and $Q_{30}$ is to be associated with the positive (negative)-parity state. As a consequence of this “minimization after projection” the intrinsic states for each parity have different deformations. The positive-parity ground state gains an amount of energy $E_{\text{corr}}^{\text{parproj}}$ given by

$$E_{\text{corr}}^{\text{parproj}} = E_{\text{HFB}}^{\text{g.s.}} - E_{\pi = +1}^{\text{g.s.}},$$

where, $E_{\pi = +1}^{\text{g.s.}}$ corresponds to the absolute minima of the positive-parity PPPESs and $E_{\text{HFB}}^{\text{g.s.}}$ to the HFB ground-state energies, that is, the absolute minima of the MFPEs. Regardless of the Gogny-EDF employed, they are always smaller than 900 keV in each of the considered nuclei. This correlation energy has to be compared to the correlation energy gained by configuration mixing (see also Fig. 10 below).

### IV. GENERATOR COORDINATE METHOD

According to the discussions in previous sections, it can be concluded that not only the plain HFB results of Sec. II, but even the parity-projection ones, may not be sufficient to decide whether, as suggested in Ref. [38], there exists a transition to an octupole deformed regime in the considered nuclei in addition to the transitional behavior along the $Q_{20}$ direction $[5,6]$. Within this context, $(Q_{20}, Q_{30})$-GCM calculations are needed to verify the stability of the quadrupole and/or octupole deformation effects encountered in both the MFPEs and the PPPESs for the considered Sm and Gd nuclei. One should also keep in mind that in the framework of such a dynamical 2D-GCM treatment, not only the mean-field energy surface but also the underlying collective inertia plays a role.

The superposition of HFB states

$$|\Psi_\sigma^\pi\rangle = \int dQ f_\sigma^\pi(Q)|\Phi(Q)\rangle$$

is used to define the GCM wave functions $|\Psi_\sigma^\pi\rangle$. In the integration domain both positive and negative octupole moments $Q_{30}$ are included. The GCM amplitudes $f_\sigma^\pi(Q)$ are the solutions of the Hill-Wheeler (HW) equation $[41]$, 

$$\int dQ \left[ H(Q, Q') - E_{\sigma}^\pi N(Q, Q') \right] f_\sigma^\pi(Q') = 0.$$ 

The GCM Hamiltonian $H(Q, Q')$ and norm $N(Q, Q')$ kernels are given by

$$H(Q, Q') = \langle \Phi(Q)|\hat{H}|\Phi(Q')\rangle,$$

$$N(Q, Q') = \langle \Phi(Q)|\Phi(Q')\rangle,$$

FIG. 4. Positive $\pi = +1$ (top panels) and negative $\pi = -1$ (bottom panels) parity-projected potential energy surfaces (PPPES) computed with the Gogny-D1S (left panels) and Gogny-D1M (right panels) EDFs for the nucleus $^{150}$Sm. See caption of Fig. 1 for the contour-line patterns.
to the spatial parity operation in the correlated wave functions built up from them. The inclusion of octupole correlations immediately restores the reflection symmetry spontaneously broken at the mean-field level and grants the use of a parity label \( \pi \) for the GCM quantities.

The collective wave functions of Eq. (13) can be used to express overlaps of operators between GCM wave functions in a more convenient way

\[
|\Psi_\sigma^\pi \rangle \langle \hat{O} | \Psi_\sigma^\pi \rangle = \int dQ dQ' G_{\sigma}^\pi(Q) \mathcal{O}(Q, Q') G_{\sigma}^\pi(Q'), \tag{14}
\]

with the kernels

\[
\mathcal{O}(Q, Q') = \int dQ'' dQ'' N_{\pi}^{-1}(Q'') \langle Q'' | \hat{O} | Q' \rangle N_{\pi}(Q'; Q') \tag{15}
\]
given in terms of the operational square root of the overlap kernel that is defined by the property

\[
N(Q; Q') = \int dQ'' N_{\pi}^{-1}(Q''; Q') N_{\pi}(Q'; Q''). \tag{16}
\]

The solution of Eq. (10) allows the calculation of physical observables like the energy splitting between positive- and negative-parity states as well as \( B(E1) \) and \( B(E3) \) transition probabilities. In the present study time-reversal symmetry is preserved and therefore only excited states with an average angular momentum zero can be accounted for. Genuine 1\(^-\) and 3\(^-\) states, however, will require to consider cranking HFB states [31,41], a calculation that is out of the scope of the present work. We assume here that the cranking rotational energy of the 1\(^-\) and 3\(^-\) states is much smaller than the excitation energy of the negative-parity bandhead and therefore it can be neglected. For the reduced transition probabilities \( B(E1, 1^- \to 0^+) \) and \( B(E3, 3^- \to 0^+) \) the rotational model approximation for \( K = 0 \) bands has been used,

\[
B(E\lambda, \lambda^- \to 0^+) = \frac{e^2}{4\pi} \left| \langle \Psi_{\sigma=1}^{\pi=-1} | \hat{O}_\lambda | \Psi_{\sigma=1}^{\pi=1} \rangle \right|^2, \tag{17}
\]

where \( \sigma \) corresponds to the first GCM excited state of negative parity. The electromagnetic transition operators \( \hat{O}_1 \) and \( \hat{O}_3 \) represent the dipole moment operator of Eq. (3) and the proton component \( \hat{O}_{30, \text{prot}} \) of the octupole operator, respectively. The evaluation of the overlap is carried out using Eq. (14).

In Fig. 6 the collective probability amplitude \( |G_{\sigma}^\pi(Q_{20}, Q_{30})|^2 \) of Eq. (13), obtained from the solution of the HW equation (10) are plotted. As a typical example, results for the 146\(^{150}\),154\(^{150}\)Sm isotopes and the Gogny-D1S EDF are presented. For other nuclei and Gogny parametrizations, the results look very similar. The left panels in Fig. 6 correspond to the ground-state wave functions (i.e., \( \sigma = 1 \) and \( \pi = +1 \)), while the right panels correspond to the lowest-lying \( \pi = -1 \) states \( \sigma = 3 \) for 146\(^{150}\)Sm and \( \sigma = 2 \) for the others.

The ground-state collective probability amplitude \( |G_{\sigma=1}^{\pi=1}(Q_{20}, Q_{30})|^2 \) reaches a global maximum at \( Q_{30} = 0 \) pointing to the octupole-soft character of the ground states in 146-154\(^{150}\)Sm. The spreading along the octupole direction is large for 150\(^{154}\)Sm, indicating octupole softness in these nuclei. For the negative-parity collective wave functions the
maximum is always located at a nonzero value of $Q_{30}$ as could be anticipated from the parity-projection results. For $^{150,154}$Sm the wave function spreads out farther along $Q_{30}$ than in previous cases in agreement with the octupole softness of their ground states.

To have a more quantitative characterization of the collective wave functions we have computed mean values of relevant operators [see Eq. (14)]. The first is the average of the quadrupole moment defined as

$$\langle \tilde{Q}_{20} \rangle_{\pi} = \langle \Psi_{\pi} ^{\sigma} | \tilde{Q}_{20} | \Psi_{\pi} ^{\sigma} \rangle. \quad (18)$$

For negative-parity operators like the octupole or the dipole moment, the above averages are zero by construction and therefore a meaningful averaged quantity has to be defined as

$$\tilde{O}_{\pi} ^{\sigma} = \int dQ dQ' G_{\pi} ^{\sigma} (Q) \mathcal{O} (Q, Q') G_{\pi} ^{\sigma} (Q'), \quad (19)$$

where a restriction to positive values of the octupole moment has been made. The average quadrupole $\tilde{Q}_{20} ^{(+)}$ and octupole $\tilde{Q}_{30} ^{(+)}$ moments for the ground state ($\sigma = 1$) are listed in Tables III and IV. The $\tilde{Q}_{20} ^{(+)}$ moments follow a trend similar to the one found within the HFB approximation, increasing their values as more neutrons are added in a given isotopic chain. However, the isotopic trend predicted for $\tilde{Q}_{30} ^{(+)}$ is quite different than the one predicted at the mean-field level. As discussed in Sec. II, at the Gogny-HFB level only the $N = 86$ and 88 isotones $^{148,150}$Sm and $^{150,152}$Gd display nonvanishing (static) octupole moments (see Tables I and II). Nevertheless, after both projection onto $\pi = +1$ and dynamical $(Q_{20}, Q_{30})$ fluctuations are considered at the 2D-GCM level, the octupole deformation effects predicted for $^{148,150}$Sm and $^{150,152}$Gd are reduced to more than half of their mean-field values. At variance with the HFB results, the nuclei $^{146,152,154}$Sm and $^{148,154,156}$Gd exhibit dynamical ground-state octupole moments $\tilde{Q}_{30} ^{(+)} \approx 0.40–0.50 b^{3/2}$. We conclude that, regardless of the particular version of the Gogny-EDF employed, our 2D-GCM calculations suggest a dynamical shape/phase transition from weakly ($^{146}$Sm and $^{148}$Gd) to well quadrupole deformed ($^{154}$Sm and $^{156}$Gd) ground states, as well as a transition to an octupole vibrational regime in the considered Sm and Gd nuclei.
negative-parity 2D-GCM states in the isotopes 146–154Sm. Results are given for both Gogny-D1S and Gogny-D1M EDFs.

\[ D_{\pi} \]

the lowest-lying region of the nuclear chart.

of the HFB approximation to predict dipole moments in this category, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking 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should be further investigated within the framework of cranking calculations, should be further investigated within the framework of cranking calculations, should be further investigate...
therefore the dynamical octupole correlation energies should be considered in improved versions of them.

A rough estimate of the contribution of the \((Q_{20}, Q_{30})\) fluctuations to the correlation energies can be obtained by subtracting to the total correlation energy the parity-projected one. Those contributions range between 0.94 and 1.41 MeV for Sm isotopes and between 0.94 and 1.56 MeV for Gd isotopes. The oscillations are slightly larger than for the total correlation energy.

To determine the contributions of each degree of freedom in the results obtained we have also performed 1D GCM calculations along each of the degrees of freedom. First, the octupole moment has been used as a generating coordinate. For each octupole moment considered, the quadrupole moment corresponds to the minimum energy. The octupole moments of the generating wave functions are taken in the range \(-7b_3/2 \leq Q_{30} \leq 7b_3/2\) and with a mesh size \(\delta Q_{30} = 0.25b_3/2\).

The 1D-GCM ansatz is

\[
\Psi_{\sigma, 1D-Q3} = \int dQ_{30} f_{\sigma, 1D-Q3}(Q_{30}) |\Phi(Q_{30})\rangle
\]

given in terms of the HFB states \(|\Phi(Q_{30})\rangle\). Note that no quadrupole constraint is imposed in these calculations. From the 1D-Q3 ground-state energies we can compute the 1D octupole correlation energy,

\[
E_{corr}^{1D-Q3} = E_{HFB}^{\pi=\pm 1} - E_{\pi=1, 1D-Q3}^{\pm 1}
\]

FIG. 7. (Color online) The dynamical dipole moments provided by the GCM calculations for the nuclei \(^{146-154}\text{Sm}\) and \(^{148-156}\text{Gd}\) are shown, as functions of the neutron number, in panels (a) and (b). Experimental dipole moments are taken from Ref. [1]. Results are shown for both Gogny-D1S and Gogny-D1M EDFs.

FIG. 8. Predicted energy splittings between the lowest lying \(\pi = +1\) and \(\pi = -1\) 2D-GCM states in \(^{146-154}\text{Sm}\) and \(^{148-156}\text{Gd}\) are compared with the experimental \(0^+ - 1^-\) and \(0^+ - 3^-\) splittings [74]. Results are shown for the D1S parametrization of the Gogny force as D1M ones are rather similar.

FIG. 9. Theoretical and experimental transition rates \(B(E1, 1^- \rightarrow 0^+)^{\pm 1}\) [panels (a) and (b)] and \(B(E3, 3^- \rightarrow 0^+)^{\pm 3}\) [panels (c) and (d)] for the nuclei \(^{146-154}\text{Sm}\) and \(^{148-156}\text{Gd}\). Results are shown for the Gogny-EDFs D1S and D1M. Experimental results for \(B(E1, 1^- \rightarrow 0^+)\) rates are extracted from Ref. [1], while the experimental \(B(E3, 3^- \rightarrow 0^+)\) rates are taken from Ref. [73].

FIG. 10. (Color online) The 2D-GCM correlation energies for the nuclei \(^{146-154}\text{Sm}\) (a) and \(^{148-156}\text{Gd}\) (b) are shown as functions of the neutron number. The correlation energies stemming from the restoration of reflection symmetry are also included. Results are shown for both Gogny-D1S and Gogny-D1M EDFs. For more details, see main text.
This quantity is displayed in panels (a) to (d) of Fig. 11 for the considered Sm and Gd nuclei. It has to be mentioned that this type of calculations have been carried out for all possible even-even nuclei with several parametrizations of the Gogny EDFs. For more details, see main text.

In a second step, GCM calculations with the quadrupole degree of freedom ($Q_{20} = 0$, that is, reflection symmetry is preserved) as a generating coordinate have been performed. The $Q_{20}$ values used are in the interval $-30b \leq Q_{20} \leq 30b$ with $\delta Q_{20} = 0.6b$. The GCM wave functions

$$|\Psi_{\sigma, 1D\text{-}Q_{2}}\rangle = \int dQ_{20} f_{\sigma, 1D\text{-}Q_{2}}(Q_{20})|\Phi(Q_{20})\rangle$$

(23)

are defined in terms of the states $|\Phi(Q_{20})\rangle$. The corresponding correlation energy

$$E_{\text{corr}}^{1D\text{-}Q^{2}} = E_{\text{HFB}}^{s,g} - E_{\sigma, 1D\text{-}Q=2}$$

(24)

is displayed in panels (a) to (d) of Fig. 11.

In panels (a) to (d) of Fig. 11, we compare the sum $E_{\text{corr}}^{1D\text{-}Q^{2}+1D\text{-}Q^{3}} = E_{\text{corr}}^{1D\text{-}Q^{3}} + E_{\text{corr}}^{1D\text{-}Q^{2}}$ with the correlation energies $E_{\text{corr}}^{2D\text{-GCM}}$ of Eq. (20). For the particular set of Sm and Gd nuclei considered in the present study and regardless of the Gogny-EDF employed, the correlation energies provided by the full 2D-GCM are very well reproduced by the sum of the ones obtained in the framework of the 1D-GCM approximations (21) and (23). Obviously, this is far from being a general statement and further explorations in other regions of the nuclear chart, specially those showing shape coexistence already at $Q_{30} = 0$ are required. Nevertheless, the kind of decoupling observed in our results may be potentially relevant to incorporate correlation energies stemming from parity restoration and octupole fluctuations in large-scale calculations of nuclear masses based on the Gogny-EDF (see, for example, Ref. [53]), as well as in future fitting protocols beyond the most recent D1M parametrization [43] of the Gogny EDF.

V. CONCLUSIONS

Calculations have been carried out using the GCM method and with the multipole moments $Q_{20}$ and $Q_{30}$ as generating coordinates for several Sm and Gd isotopes and with different parametrizations of the Gogny force. The results from different parametrizations are very close to each other, indicating again that the D1M parametrization of the Gogny force performs as well as D1S in spectroscopic calculation. The comparison with experimental data is fairly good both for excitation energies and electromagnetic transition probabilities reassuring the predictive power of the Gogny class of EDFs. Comparison of the 2D GCM results with the outcome of previous 1D collective Schrödinger equation calculations in the same region points to a decoupling of the dynamics of the quadrupole and octupole degrees of freedom. This conclusion is reinforced by the comparison of the 2D correlation energies with the sum of correlation energies along each of the degrees of freedom. Correlation energies show a smooth behavior with neutron number with differences between different isotopes as large as 200 keV. Although these differences are small, they can be relevant for theories aiming at providing accurate mass tables for applications requiring accurate reaction rates that depend on their energetic balance.

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