Measurement of the top pair production cross section in the lepton + jets channel using a jet flavor discriminant


(CDF Collaboration)
MEASUREMENT OF THE TOP PAIR PRODUCTION CROSS . . .

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We present a new method to measure the top quark pair production cross section and the background rates with data corresponding to an integrated luminosity of 2.7 fb\(^{-1}\) from \(p\bar{p}\) collisions at \(\sqrt{s} = 1.96\) TeV collected with the CDF II Detector. We select events with a single electron or muon candidate, missing transverse energy, and at least one \(b\)-tagged jet. We perform a simultaneous fit to a jet flavor discriminant across nine samples defined by the number of jets and \(b\) tags. An advantage of this approach is that many systematic uncertainties are measured in situ and inversely scale with integrated luminosity. We measure a top cross section of \(\sigma_{\text{t\bar{t}}} = 7.64 \pm 0.57(\text{stat} + \text{syst}) \pm 0.45(\text{luminosity})\) pb.

Since its discovery in 1995 [1,2], much has been learned about the top quark through analyses of \(p\bar{p}\) collisions. Top quarks are produced in pairs through the strong interaction and each top quark decays dominantly to a \(W\) boson and a \(b\) quark, followed by the \(W\) decaying either to a pair of quarks (which form jets) or a lepton and a neutrino. This paper describes a measurement of the top-antitop pair production cross section, \(\sigma_{\text{t\bar{t}}}\), in the \(p\bar{p} \rightarrow \text{t}\bar{t} \rightarrow \ell\nu qq'\bar{b}\bar{b}\) channel at a center-of-mass energy, \(\sqrt{s} = 1.96\) TeV using a new methodology to constrain background contributions and systematic effects, resulting in an improved sensitivity.

The jets which originate from the bottom quarks in the final state provide an opportunity to select events which are more likely to have come from top quark decays than from other processes. A \(b\)-tagging algorithm takes advantage of the characteristics—largely the secondary vertex displaced from the primary vertex—that distinguish heavy flavor (HF) jets from charm and light flavor (LF) jets [3]. This algorithm allows us to reduce the backgrounds from \(W\) + jets processes, which can mimic the top decay signature, and was the basis for several previous measurements of the top cross section [4,5].

While requiring the event to have at least one \(b\)-tagged jet reduces the backgrounds, it does not eliminate them. It is important to estimate the amount of \(W\) boson production with associated jets from heavy flavor, which is theoretically difficult and a source of systematic uncertainties for measurements of the cross section as well as the mass. Here we reduce this systematic uncertainty and constrain the \(W\) + HF background by performing a fit to the data which includes regions dominated by \(W\) + jets.

Since the \(b\)-tagging algorithm can incorrectly tag light flavor jets as \(b\) jets, it is advantageous to apply an additional discriminant to \(b\)-tagged jets to further separate processes with jets from bottom, charm, and light flavor. This flavor separator is a neural network whose output, on a statistical basis, discriminates between \(b\)-quark, \(c\)-quark, and light-flavor jets. The flavor separator uses 25 variables to output a single number indicating how likely a jet is a \(b\) jet, where the invariant mass of the secondary vertex has the most separation power. The flavor separator was calibrated using data control samples [6].

In this paper, we use a flavor separator for the first time in the measurement of the \(t\bar{t}\) cross section. In order to constrain the background contributions, we perform the fit to the flavor discriminant in nine samples defined by the number of jets, \(n_{\text{jet}}\) (1, 2, 3, 4, or \(\geq 5\)), and number of \(b\)-tagged jets, \(n_{\text{tag}}\) (1 or \(\geq 2\)). Events with one or two jets are dominated by \(W + j\) events, whereas events with three or more jets are largely \(t\bar{t}\). Events with two \(b\) tags are dominated by \(Wbb\) and \(t\bar{t}\), whereas events with a single \(b\) tag are predominantly \(W + c\) and \(W + LF\). Previous methods selected events with three or more jets in order to reduce the largest background from \(W + j\) processes [4,5,7]. This new method instead constrains the background contribution of the \(W + j\) processes in the region with three or more jets by measuring the contributions in the regions with one and two jets.

We use a data sample corresponding to 2.7 fb\(^{-1}\) of integrated luminosity, collected from February 2002 through April 2008 using the CDF II detector [8], an approximately cylindrically symmetric detector located at the Tevatron collider. CDF II is a general-purpose device; the central drift chamber provides charged-particle tracking, while the silicon system provides excellent vertex and impact parameter resolution, both of which are important for identifying bottom quarks. Electromagnetic and hadronic calorimeters are located outside the tracking chambers, and provide identification of electrons and jets. At the outermost layer of the detector sit the muon drift chambers which provide muon identification.

We select events with a \(W\) candidate decaying leptonically to either an electron or muon. We require at least one jet and exactly one lepton candidate both with transverse energy \(E_T > 20\) GeV and pseudorapidity \(|\eta| < 2.0\) [9]. We require that at least one jet is \(b\)-tagged, and that there is at least 20 GeV of missing transverse energy, \(E_T\), in the event. To reduce QCD backgrounds, we require the transverse mass of the \(W\), \(m_T^W = \sqrt{2(p_T^\ell p_T^\nu - p_T^\ell p_T^\nu - p_T^\ell p_T^\nu)}\), to
be at least 10 GeV/c^2 for muons, and at least 20 GeV/c^2 for electrons. Electron samples have a larger QCD background contamination than muon samples, so there we also require the ET to satisfy $\frac{E_T}{\sqrt{E_{TC}} > -0.05 m_W^3}$ (in GeV/c^2) + 3.5, where the denominator is the square root of the amount of unclustered energy in the direction of the missing transverse energy [10].

In addition to QCD multijet processes, the final state in this analysis can be mimicked by several other processes. W + jets processes are by far the largest source of backgrounds. Single top production, di-boson production, and Z + jets processes—collectively referred to as electroweak (EW) processes—also contribute. All but the QCD multijet backgrounds are modeled with Monte Carlo simulations; the QCD backgrounds are estimated using a data-driven approach. Events that pass the selection criteria, though with the lepton candidate failing any two identification cuts, are mostly QCD multijet processes, and this sample is used to model the background from these QCD processes. The normalization of the QCD background is estimated from a fit to the missing ET distribution for each subsample, without the missing ET requirement.

Monte Carlo samples are employed to estimate acceptances for the signal and backgrounds, and to model relevant distributions used in the fits described below. All of the Monte Carlo samples employed were generated using either PYTHIA v6.216 [11] (the tt and di-boson samples), MADGRAPH [12] (the single top sample), or ALPGEN v2.10' [13] with generator-to-reconstructed-jet matching [14,15] and PYTHIA v6.326 for showering (the W + jets and Z + jets samples). The tt signal Monte Carlo sample was generated with the CTEQ5L [16] parton distribution functions (PDFs) assuming a top mass of $m_t = 175$ GeV/c^2. All samples are processed through a detailed simulation of the CDF II detector response, after which they are treated in the same manner as the data events. Each of the samples is divided based on the number of jets and b tags, and made into templates—binned distributions of the flavor separator output.

The measurement is accomplished as a fit of the flavor separator distribution performed simultaneously in the nine data subsamples. Results are obtained by maximizing a binned Poisson likelihood which incorporates templates from each of the tt, W + jets, electroweak, and QCD processes. The templates are combined after initializing them to the predicted yield for data corresponding to an integrated luminosity of 2.7 fb^{-1}, where the initialization factors are functions of cross sections, tagging efficiencies, and energy scales which are all parameters in the fit. The overall normalization of each template is floated in the fit—a single overall normalization factor is used for each process—and the primary result of the fit is a set of those normalizations: the tt cross section and relative normalizations, $K_{t}$, to the standard model expectations for W + jets, electroweak, and QCD components.

Template normalizations also include functions, $P_x(i, j, \xi)$, that parametrize the effect of a source of systematic uncertainty, x, in the subsample with $n_{tag} = i$ and $n_{jet} = j$, as a function of the relative shift, $\xi$, of quantity x, in units of the uncertainty on x. A separate function is employed for each process in each subsample for each source of systematic uncertainty; an example function is shown in Fig. 1. This leads to a total of 12 parameters in the fit—seven normalizations of the samples ($\sigma_{tt}$, $K_{WW}$, $K_{WW}$, $K_{WW}$, $K_{WW}$, $K_{WW}$, $K_{WW}$, and $K_{QCD}$), and five systematic uncertainty parameters ($\xi_{BTag}$, $\xi_{Mistag}$, $\xi_{1/FSR}$, $\xi_{Q^2}$, $\xi_{IES}$).

Systematic uncertainties in this measurement can affect both the normalizations and the shapes of the templates. The rate uncertainties are naturally included in the fit via the $P_x(i, j, \xi)$ functions, and these systematic uncertainties are reflected by the total fit error. To account for each shape uncertainty, we generate an additional set of templates with the variable in question changed, rerun the fit, and take the difference in the result as the uncertainty.

We vary the b-tagging efficiency, mistag rate, and the jet energy calibration [17] by their uncertainties for all simulated samples. Initial- and final-state radiation (ISR/FSR) are processes in which gluons are radiated before or after the collision, respectively. The uncertainty arises due to ISR/FSR leading to a larger or smaller number of jets in the event. To account for this, we make additional sets of tt templates with more or less ISR and FSR as compared to the normal settings; the different settings are constrained by studies of Drell-Yan production [18]. The systematic uncertainty associated to the choice of the renormalization and factorization scales is estimated by varying these scales between half and twice their default values, as indicated in [13]. This variation also accounts for differences in ISR/FSR in W + jets processes.

![FIG. 1](color). The function which parametrizes the effect of the jet energy scale on the 1-tag templates of the tt sample. Each jet and tag bin for each process in each subsample has a different function for each source of systematic uncertainty. The x axis is in units of the systematic shift.
The uncertainty due to the choice of the algorithm used to generate the parton shower was determined by comparing the results obtained using PYTHIA and HERWIG [19]. We account for uncertainties in our modeling of the QCD template shape by using electronlike signals associated with multiple tracks, rather than electrons that fail identification cuts, to make templates. The flavor separator has a correction factor applied to match its mistag rate to the one observed in data; to account for this uncertainty, we examine templates without this factor applied. The models describing color reconnection—i.e., the QCD cross talk between the decay products of the top quarks—are not known precisely, so we account for this uncertainty by comparing two different models. We take an uncertainty of 0.6% on the top cross section due to the PDFs, and an uncertainty of 0.5% due to the beam position and lepton identification efficiency. We take a conservative 2% uncertainty due to the PDFs on the top cross section due to the PDFs, and an uncertainty of 0.6% on the top cross section due to the PDFs, and an uncertainty of 0.5% due to the beam position and lepton identification efficiency. We take a conservative 2% uncertainty due to the PDFs on the top cross section due to the PDFs, and an uncertainty of 0.6% on the top cross section due to the PDFs, and an uncertainty of 0.5% due to the beam position and lepton identification efficiency.

The measured luminosity has an uncertainty of 5.9%.

The total normalizations of the $tt$ and $Wbb$ components in the fit are given by

$$ N_{tt}^{\text{pred}}(i, j) = \sigma_{tt} \cdot F_{tt}^{MC}(i, j) \cdot P_{FSR}(i, j, \xi_{FSR}) \cdot P_{\text{Mistag}}(i, j, \xi_{\text{Mistag}}) \cdot P_{\text{JES}}(i, j, \xi_{\text{JES}}). $$

$$ N_{Wbb}^{\text{pred}}(i, j) = K_{Wbb} \cdot \sigma_{Wbb}^{MC} \cdot L \cdot S_{\sigma_w} \cdot F_{Wbb}^{MC}(i, j) \cdot P_{\text{Mistag}}(i, j, \xi_{\text{Mistag}}) \cdot P_{\text{JES}}(i, j, \xi_{\text{JES}}) \cdot P_{\text{Q}}(j, i, \xi_{\text{Q}}). $$

where $\sigma_{tt}$ is the cross section and $K_{Wbb}$ is the relative normalization factor; $\sigma_{tt}^{MC}$ is the cross section from Monte Carlo simulations; $L = \int L \, dt$ is the integrated luminosity; $F_{tt}^{MC}(i, j)$ is the Monte Carlo prediction for the fraction of events with $i$ $b$ tags and $j$ jets, including reconstruction and selection efficiencies; $S_{\sigma_w}$ is a factor of 1.54 obtained from the ratio of the measured $W +$ jets cross section [20] to the ALPGEN-prediction cross section—this is necessary due to ALPGEN being a leading-order event generator; and $P_{x}(i, j, \xi_{x})$ are functions for each source of systematic uncertainty, $x$. Normalizations of the other five samples are obtained in a similar manner. For reference and easier comparison to other measurements, the cross sections for $K = 1$ are calculated from ALPGEN as 2744.1 pb for $W +$ LF, 31.9 pb for $Wc$, 13.1 pb for $Wcc$, and 6.8 pb for $Wbb$.

The data and best fit to the flavor separator distribution are shown in Fig. 2. The $tt$ production cross section is found to be $\sigma_{tt} = 7.64 \pm 0.57$ pb, and relative normalization factors are $K_{Wbb} = 1.39 \pm 0.28$, $K_{Wcc} = 0.83 \pm 0.90$, $K_{Wc} = 1.66 \pm 0.32$, $K_{W +$ LF} = 0.98 \pm 0.25$, $K_{EW} = 1.10 \pm 0.10$, and $K_{QCD} = 0.82 \pm 0.26$. These results include statistical and systematic uncertainties, but do not include an uncertainty due to the luminosity. The top cross section we measure is consistent with theoretical predictions [21–24], and the values of the relative normalizations are consistent with what is expected from the theoretical uncertainty of the leading-order cross sections used by the Monte Carlo simulation generators [13,14].

In order to evaluate the performance of this new method, we have compared the estimates of the systematic uncertainties on the top cross section with the previous method of background estimation [7], though as applied to the same integrated luminosity. A summary of these comparisons is shown in Table I. The total uncertainty drops from 0.84 pb to 0.73 pb.

<table>
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<th>Uncertainty</th>
<th>Previous Method</th>
<th>This Result</th>
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<tr>
<td>Statistical</td>
<td>0.36 pb</td>
<td>0.33 pb</td>
</tr>
<tr>
<td>HF $K$ Factor</td>
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<td>Inc in stat</td>
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<tr>
<td>$Q^2$</td>
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<td>0.21 pb</td>
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<tr>
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<tr>
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<td>$Z0$</td>
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<td>0.02 pb</td>
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<td>Sub-Total</td>
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<td>0.45 pb</td>
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<tr>
<td>Total</td>
<td>0.84 pb</td>
<td>0.73 pb</td>
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0.84 pb to 0.73 pb, which is a 13% improvement. However, the previous result developed a normalization to the $Z$ cross section to reduce the luminosity uncertainty dramatically, and this method can be extended in the future to include that improvement. Therefore, upon excluding the luminosity uncertainty in order to better compare the methods, the uncertainty drops from 0.72 pb to 0.57 pb for a 21% improvement.

In summary, we measured the top pair production cross section using a novel method for estimating background contributions with CDF II data corresponding to an integrated luminosity of 2.7 fb$^{-1}$. The cross section we measure, $7.64 \pm 0.57$(stat + syst) \pm 0.45(luminosity), is consistent with the standard model next-to-leading-order theoretical calculation \cite{22}, and the background contributions are consistent with other predictions \cite{7}. Compared to the previous method of background estimation, using $b$ tagging, this new method improves the precision on the top quark pair production cross section by 21%, excluding luminosity uncertainties.

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\begin{thebibliography}{99}
\bibitem{9} We use a cylindrical coordinate system with its origin in the center of the detector, where $\theta$ and $\phi$ are the polar and azimuthal angles, respectively, and pseudorapidity is $\eta = -\ln \tan(\theta/2)$. The missing $E_T$ ($\vec{E}_T$) is defined by $\vec{E}_T = -\sum_i E_T^i n'_i$, $i =$ calorimeter tower number, where $n'_i$ is a unit vector perpendicular to the beam axis and pointing at the $i$-th calorimeter tower. $\vec{E}_T$ is corrected for high-energy muons and also jet energy corrections. We define $E_T = |\vec{E}_T|$. The transverse momentum, $p_T$, is defined to be $p \sin \theta$.
\end{thebibliography}