

1 **A study on a $^{210}\text{Pb}_{\text{ex}}$ accumulation-decay model for dating**
 2 **moraine soils to trace glacier retreat time**

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14 **Abstract:** This paper reports work exploring the potential for using the natural fallout
 15 radionuclide $^{210}\text{Pb}_{\text{ex}}$ to date moraine soils for tracing glacier retreat. Based on the
 16 physical processes of $^{210}\text{Pb}_{\text{ex}}$ deposition, decay and losses due to runoff, a $^{210}\text{Pb}_{\text{ex}}$
 17 accumulation-decay model ($A_n = I \left[\frac{1-\lambda^{n+1}}{1-\lambda} - \frac{b(c^{n+1}-\lambda^{n+1})}{c-\lambda} \right]$) was developed, where
 18 $A_n = ^{210}\text{Pb}_{\text{ex}}$ inventory ($\text{Bq}\cdot\text{m}^{-2}$); $I =$ annual inventory of $^{210}\text{Pb}_{\text{ex}}$ deposition ($\text{Bq}\cdot\text{m}^{-2}$);
 19 $\lambda = ^{210}\text{Pb}$ decay coefficient (0.969); $n =$ time span (years); b and $c = ^{210}\text{Pb}_{\text{ex}}$ loss
 20 coefficients for the runoff pathway. Furthermore, ^{137}Cs was used to identify the ages
 21 of the study sites and to support the $^{210}\text{Pb}_{\text{ex}}$ model results. The model was validated
 22 with data obtained from the Hailuoguo Glacier Valley, Mt. Gongga, in 2016, where

1 nine glacier retreat moraine points were recorded from 1910–1990 along a retreat
2 length of 1750 m in the valley. $^{210}\text{Pb}_{\text{ex}}$ inventories increased from $3,669.6 \pm 218.5$
3 $\text{Bq}\cdot\text{m}^{-2}$ at the site where the glacier retreated in 1990 to $10,718.9 \pm 167.4 \text{ Bq}\cdot\text{m}^{-2}$ in
4 1910. The coefficients of $b = 0.6006$ and $c = 0.9764$ were derived from the $^{210}\text{Pb}_{\text{ex}}$
5 inventories at the nine sites with recorded glacier retreat times that were marked with
6 special stone and terrain features. The goodness-of-fit (GOF) for the model
7 predictions of glacier retreat times is 65.5%. The results obtained confirm that the
8 fallout radionuclide $^{210}\text{Pb}_{\text{ex}}$ has potential for dating moraine soils in other cryosphere
9 regions throughout the world as well as for other types of records forming
10 sedimentary landform sequences such as soils on debris flows and alluvial fans.

11 **Keywords:** $^{210}\text{Pb}_{\text{ex}}$ accumulation-decay model, ^{137}Cs , dating moraine soils, glacier
12 retreat time, Hailuogou Glacier, China.

13 1 INTRODUCTION

14 Owing to global warming, most glaciers in remote polar and high mountain
15 regions of the world have retreated rapidly, particularly over the past 100 years, but
16 only some glaciers have observational retreat data (Barry, 2006). There is an urgent
17 need for information on recent changes in glacier retreat speeds for assessing the
18 impacts of climate change and its effects on soil and water resources in polar and
19 mountainous regions (Lizaga et al., 2019a). Such information will improve
20 understanding of the impact of climate change on fragile polar and high mountain
21 ecosystems at local and global scales, thereby permitting better management and
22 conservation of soil and water resources (Lopez-Moreno et al., 2016).

1 Fallout radionuclides (FRN), such as ^{137}Cs and $^{210}\text{Pb}_{\text{ex}}$, have been widely used
2 for assessing soil loss (Walling et al., 2002; Navas et al., 2013; Chen et al., 2019),
3 tracing sediment sources (Collins et al., 2017; Palazón et al., 2015; Gaspar et al., 2019;
4 Lizaga et al., 2019b), establishing sediment budgets (Navas et al., 2014; Walling et al.,
5 2014) and dating ice and sediment deposits (Morellón et al., 2011). ^{210}Pb is an
6 environmental isotope of the ^{238}U decay series with a half-life of 22.6 years, which is
7 derived from the decay of ^{222}Rn (half-life of 3.8 days). ^{222}Rn is a decay product of
8 ^{226}Ra (half-life of 1622 years) and is widely found in natural soils and rocks.
9 Following ^{226}Ra decay to gaseous ^{222}Rn , part of the resultant ^{222}Rn decays to form
10 ^{210}Pb in soils and rocks. Another small part of ^{222}Rn enters the atmosphere, decays
11 into ^{210}Pb in the atmosphere, and is then contained in fallout back to the surface of the
12 soil in association with precipitation. This fallout is eventually absorbed by the
13 surface soil, and it is this component of the total ^{210}Pb derived from atmospheric
14 fallout that is termed unsupported or excess ^{210}Pb (Robbins, 1978). The deposition of
15 fallout ^{210}Pb from the atmosphere has been relatively constant over time because of its
16 natural origin. This is different from the deposition of ^{137}Cs which is characterised by
17 peak fallout rates in 1963, which subsequently declined to very low values by 1972 in
18 the northern hemisphere as a result of the ban on atmospheric testing of
19 thermonuclear weapons (Larsen, 1985). The Chernobyl accident increased soil
20 radioactivity levels in the northern hemisphere, especially in eastern Europe, but
21 negligible activities of Chernobyl ^{137}Cs fallout were detected in China in 1986 (Zhang,
22 2005).

1 $^{210}\text{Pb}_{\text{ex}}$ is commonly applied to assess soil redistribution (Gaspar et al., 2013;
2 Porto et al., 2018), but the radionuclide is also used for dating sediment records
3 retrieved from water bodies to reconstruct dynamic changes in sediment accumulation
4 (Morellón et al., 2011). Source models comprised of a number of requirements related
5 to the fallout rate of the radionuclide or the constant accumulation of sediments have
6 been developed (Appleby & Oldfield, 1978). For example, the constant initial
7 concentration (CIC) model (Krishnaswamy et al., 1971) was applicable when the
8 amount of $^{210}\text{Pb}_{\text{ex}}$ carried and captured by sediments per unit mass was constant and
9 the deposition rate was constant. The constant rate of supply (CRS) model assumes
10 that $^{210}\text{Pb}_{\text{ex}}$ flux is constant and accumulation rate varies with time, the flux of $^{210}\text{Pb}_{\text{ex}}$
11 entering the interface between atmosphere and water is dynamically balanced with its
12 flux entering the interface between water and sediment (Sanchez-Cabeza et al., 2000).
13 Other models were specifically developed to date fluvial deposits with $^{210}\text{Pb}_{\text{ex}}$
14 considering the continuous sedimentation occurring in floodplains (He & Walling,
15 1996).

16 For regions where lakes are nonexistent, there is a need to find alternative
17 sedimentary deposits that can fulfill suitable stability conditions so as to develop a
18 deposition model fulfilling the conditions for reconstructing the chronology of the
19 sediment deposition. Special conditions in the Hailuogou Valley located at the foot of
20 the Tibetan Plateau have prevented the preservation of lakes and therefore
21 sedimentary records deposited at their bottoms from which to reconstruct the recent
22 history of sediment accumulation generated after glacier retreat are absent.

1 In light of the situation described above, this study explored the potential for
2 using $^{210}\text{Pb}_{\text{ex}}$ to date moraine soils and trace glacier retreat over the past 100 years.
3 Based on the physical processes of $^{210}\text{Pb}_{\text{ex}}$ deposition, losses with runoff that remove
4 fine particles where $^{210}\text{Pb}_{\text{ex}}$ is fixed and decays, a preliminary $^{210}\text{Pb}_{\text{ex}}$
5 accumulation-decay model was developed. The model also considered the change of
6 erosion rate, especially water erosion (Berhe et al., 2018; Liu et al., 2019), which
7 decreased with vegetation growth in the valley following the glacier retreat. To this
8 aim, a field campaign was undertaken in the Hailuoguo Glacier Valley in 2016 at Mt.
9 Gongga (Hengduan Range, China) a benchmark site of the IAEA INT5153 Project,
10 “Assessing the Impact of Climate Change and its Effects on Soil and Water Resources
11 in Polar and Mountainous Regions.” Following the direction of glacier retreat along
12 the valley, nine sampling sites were selected based on the known chronology of
13 moraine deposits. The precise moraine position was marked by boundary stones at
14 each site over the period from 1910 to 1990 (Luo et al., 2015). Furthermore, fallout of
15 ^{137}Cs was used to identify the ages of the study sites, labeled by the ^{137}Cs peak in
16 1963 and to assess if soil mobilization by water erosion occurred at the study sites. In
17 addition, ^{137}Cs was used to support the $^{210}\text{Pb}_{\text{ex}}$ model results. The model was validated
18 using these recorded retreat times and combining the data on $^{210}\text{Pb}_{\text{ex}}$ inventories with
19 the time spans between the glacier retreat year and the sampling year for the moraine
20 soil at the nine measurement points.

1 2 MATERIALS AND METHODS

2 2.1 Study Area

3 This study was carried out in the glacier retreat area of Hailuogou Valley in
4 Mt. Gongga, which is located in the Ganzi Tibetan Autonomous Prefecture of Sichuan
5 Province, China (Figure 1). Mt. Gongga is situated in the middle of the Hengduan
6 Mountain range, which is located on the southeastern edge of the Tibet Plateau. The
7 peak of Mt. Gongga is 7553 m asl and its snow line elevation varies between 4800–
8 5200 m. Glaciers on Mt. Gongga have a total area of 255.1 km² with a total volume of
9 ~24.65 km³; the largest one, the Hailuogou Glacier, has a length of 13.1 km and a
10 corresponding area of 25.71 km². The annual mean temperature at 3000 m on Mt.
11 Gongga was 4.2°C since 1988, but in the past two decades, the temperature has
12 increased 0.35°C/decade at the Hailuogou Weather Station (Wu et al., 2013). The
13 glacier in Hailuogou valley retreated from 2830 m asl in 1936 to 3000 m asl in 2006
14 with a retreat length of 1.15 km and an average retreat speed of 19.6 m/year during
15 the period 1990–2004. The annual runoff yield of the Hailuogou ravine increased by
16 12.9% per year from $232.4 \times 10^6 \text{ m}^3$ (1994) to $684.5 \times 10^6 \text{ m}^3$ (2005). The average
17 annual precipitation is 1,974 mm (Liu et al., 2010). The valley floor is flat and the
18 river channel incises the valley floor leaving the moraine deposits in the valley largely
19 unaffected by floods. Since the end of the Little Ice Age (LIA, from mid-seventeenth
20 to early eighteenth century), the Hailuogou Glacier retreated markedly with the rising
21 of global temperature, producing a moraine channel and side moraine. Soil and
22 vegetation gradually developed on the exposed glacier soil (Zhou et al., 2013).

1 Consequently, a typical soil chronological sequence and a complete primary
2 vegetation succession sequence have developed in the Hailuogou Glacier retreat area.
3 The native succession sequence of soil and vegetation is about 2 km long from the
4 end of the glacier that exists integrally and continuously on moraine deposits with big
5 boulders and sandy sediments. At the end of the glacier, there is fresh bare sandy
6 sediment soil in micro-depressions surrounded by big boulders. As seen in the
7 photographs (Fig. 1) the soil gradually evolves to be brown soil with dark colour and
8 high content of organic matter along the transition from bare land to mature subalpine
9 conifer forests. The vegetation succession is: bare ground of moraine grass such as
10 *Astragalus mongholicus* (1990s), young alder and willow, *Hippophae rhamnoides*
11 (1980s), medium alder and willow (1970s), young *Picea-Abies* alder (1960s),
12 *Picea-Abies* (1940s) and *Picea-Abies* (1930s). After 125 years, the biomass and
13 productivity of the plant community is very high (Luo et al., 2017). The position of
14 the glacier tongue during glacier retreat and the vegetation succession at nine selected
15 sites were accurately recorded by researchers at the Experimental Station of Mt.
16 Gongga, using the existing stone marks and analysing terrain features and vegetation
17 changes along the glacier valley (Luo et al., 2012; Zhou et al., 2016).

18 **2.2 Field Sampling and Laboratory Analysis**

19 Sampling was carried out in May of 2016. Nine appropriate flat or
20 micro-depression and undisturbed sites (R1–R9) were carefully selected for sampling
21 soil profiles. The glacier retreat time at each site along the Hailoukou Valley is well
22 documented from 1910–1990 (Table 1).

1 At each site, a square sampling section (50 x 50 cm) was established. The
2 section was excavated from the top surface down to a depth of 10 cm to extract 1 cm
3 samples at regular intervals. At each site, 10 stratified samples were obtained totaling
4 90 depth interval samples collected from the nine study sites (R1 to R9).

5 Prior to analysis, all samples were air dried, disaggregated, passed through a 2
6 mm sieve, homogenised and sealed hermetically into cylindrical containers for ≥ 21
7 days to achieve equilibrium between ^{226}Ra and its daughters. The activities of ^{210}Pb ,
8 ^{226}Ra and ^{137}Cs were measured in the isotope laboratory of the Chengdu Institute of
9 Mountain Hazards and Environment at the Chinese Academy of Sciences. The
10 activities of $^{210}\text{Pb}_{\text{ex}}$ and ^{137}Cs in the samples were measured by gamma spectrometry,
11 using a high resolution, low background, low energy and hyper-pure *n*-type LOAX
12 HPGe detector (ORTEC, Oak Ridge, Tennessee, USA). Each sample weighed ≥ 500 g
13 and counting times were in excess of 80,000 s, providing a precision of approximately
14 $\pm 10\%$ at the 90% level of confidence for the gamma ray measurements. ^{137}Cs was
15 detected at 662 keV. The total ^{210}Pb activity was obtained using the 46.5 keV gamma
16 ray from ^{210}Pb and ^{226}Ra concentrations were obtained using the 351.9 keV gamma
17 ray from ^{214}Pb , a short-lived daughter of ^{226}Ra . Unsupported ^{210}Pb ($^{210}\text{Pb}_{\text{ex}}$)
18 concentrations in the samples were calculated by subtracting the ^{226}Ra -supported
19 ^{210}Pb concentrations from the total ^{210}Pb concentrations. The grain size distributions
20 (sand, silt and clay sizes) of the samples were measured using a laser-diffraction
21 granulometer (Mastersizer 2000, Malvern, UK); in this case, the samples were
22 successively pretreated with 10% H_2O_2 and 10% HCl to remove organic matter and

1 CaCO₃, respectively (Shi, et al. 2017). All samples were dispersed using an ultrasonic
2 probe for one minute before the measurements for absolute grain size distributions
3 were made.

4 **3 RESULTS**

5 **3.1 Particle size composition**

6 The particle size depth distributions of the moraine soils are shown in Figure 2.
7 The average proportions of clay (<2µm) ranged between 0.19–0.97% with a
8 corresponding mean of 0.31%, silt (2–63 µm) between 26.64% and 61.33% with a
9 mean of 44.49% and sand (63–2000 µm) between 38.46% and 73.29% with a mean of
10 55.2%. The mean median diameter (d₅₀) of the nine moraine sites ranged between 44–
11 113 µm with a mean value of 77 µm. The silt content in the recent moraine sites (R1
12 and R2) was lower than that of the older moraine soils at sites R6 through R8 which
13 were covered with dense vegetation. The silt content decreased with depth in the
14 mature moraine soil at R9. The clay content was very low in all profiles except at R6,
15 mainly because the moraine soil was in the early stages of development.

16 **3.2 Distribution of ¹³⁷Cs and ²¹⁰Pb_{ex}**

17 Little ¹³⁷Cs was detected in recent soils at R1 (1990) and R2 (1983), which
18 contain ¹³⁷Cs transported with the sediments, while almost no ¹³⁷Cs was found at R4
19 (1966) because the moraine deposit was formed shortly after the 1963 ¹³⁷Cs peak.
20 However, the older moraine soils formed before the ¹³⁷Cs peak at R7 (1930), R8
21 (1915) and R9 (1910) had the highest ¹³⁷Cs inventories ranging from 764.7 ± 29.8
22 Bq·m⁻² to 891.23 ± 54.3 Bq·m⁻² (Table 2). The depth distributions of ¹³⁷Cs (Figure 3)

1 exhibit typical profiles at R7 and R9, where the highest concentrations occurred in the
2 top layers and declined exponentially as depth increased. In these profiles, only low
3 levels of ^{137}Cs were detected in the layers below 8 cm depth. Despite the fact that
4 random initial fallout might affect spatial variability of ^{137}Cs inventories (Owens &
5 Walling, 1996), the value of $850.6 \text{ Bq}\cdot\text{m}^{-2}$, which is the average of two points, was
6 considered to be the local ^{137}Cs reference inventory because it is in agreement with
7 reference inventory values predicted for China by Qi et al. (2006). The ^{137}Cs
8 inventory at R8 was less than that of R7 and R9, and the highest ^{137}Cs concentration
9 occurred in the middle layer at 4–6cm depth, indicating that both erosion and
10 deposition have taken place since 1963 at this site (Figure 3). The ^{137}Cs inventory
11 increased from $105.2 \pm 17.4 \text{ Bq}\cdot\text{m}^{-2}$ at R3 (1972) to $588.2 \pm 39.8 \text{ Bq}\cdot\text{m}^{-2}$ at R6 (1945)
12 and the ^{137}Cs depth distribution curves gradually became typical, because little ^{137}Cs
13 was produced by atomic weapon testing after the 1960s (Sutherland, 1991). The ^{137}Cs
14 inventories in soil formed before the ^{137}Cs peak at sites R5, R6 and R8 were lower
15 than the local reference inventory since part of the ^{137}Cs fallout was removed by water
16 erosion (Liu et al., 2018) resulting from rainfall and snow melt (Table 2, Figure3).

17 The depth distributions for $^{210}\text{Pb}_{\text{ex}}$ at the nine sites are shown in Figure 4. In
18 general, the $^{210}\text{Pb}_{\text{ex}}$ depth distribution curves in soils at the nine sites have similar
19 shapes, with the highest concentration of $^{210}\text{Pb}_{\text{ex}}$ occurring in the top layers, except in
20 the case of R4 and R8, and then declining exponentially as depth increased. Little
21 $^{210}\text{Pb}_{\text{ex}}$ was detected in the layer below a depth of 8 cm. Despite the fact that little
22 ^{137}Cs was detected in the soil at R1 (1990), there was a considerable amount of $^{210}\text{Pb}_{\text{ex}}$

1 with an inventory of $3,669.6 \pm 218.5 \text{ Bq}\cdot\text{m}^{-2}$ at R1 site. Across the sampling sites, the
2 variation of the $^{210}\text{Pb}_{\text{ex}}$ inventories with time had a similar pattern as ^{137}Cs , increasing
3 with the span of time between the glacier retreat and the sampling year, reaching its
4 highest value of $10,718.9 \pm 167.4 \text{ Bq}\cdot\text{m}^{-2}$ at site R9 (Table 2, Figure5).

5 **4 DISCUSSION**

6 **4.1 Temporal variations of ^{137}Cs and $^{210}\text{Pb}_{\text{ex}}$ inventories**

7 Since the sources of ^{137}Cs and $^{210}\text{Pb}_{\text{ex}}$ are different, there is a difference in the
8 total ^{137}Cs and $^{210}\text{Pb}_{\text{ex}}$ inventory curves at the nine moraine sites on a temporal scale.
9 In general, both radionuclides gradually increased with time. Apart from sites R1–R4
10 where moraine soils formed after the 1963 ^{137}Cs peak, the inventories of ^{137}Cs at R5
11 and R6, prior to the ^{137}Cs peak (Owens et al., 1997), were significantly lower than
12 those at R7 and R9 because older sites from R7–R9 experienced increased ^{137}Cs
13 fallout during the nuclear weapon test period and presumably had more dense
14 vegetation cover protecting the soil surface at that time. On the contrary, the increase
15 of $^{210}\text{Pb}_{\text{ex}}$ inventories without obvious inflection point over the nine moraine sites is
16 attributed to the fallout process of $^{210}\text{Pb}_{\text{ex}}$, which exhibits a continuous and stable
17 fallout rate on a temporal scale. However, the $^{210}\text{Pb}_{\text{ex}}$ inventory values at R3 (1972)
18 and R6 (1945) were irregularly lower. This implies that severe erosion occurred
19 during the period of soil and vegetation development since the glacier retreated from
20 these two specific sites likely due to runoff though soil disturbance by wildlife can not
21 be totally discarded.

1 4.2 Proposal of a new $^{210}\text{Pb}_{\text{ex}}$ accumulation-decay model

2 Existing theoretical $^{210}\text{Pb}_{\text{ex}}$ models make this approach convenient for wider
3 adoption, including for example, the mass balance model for $^{210}\text{Pb}_{\text{ex}}$ -based estimates
4 of soil loss (Walling & He, 1999, 2002), which is based on the physical processes of
5 the fallout redistribution after its deposition on the soil surface. For dating lake
6 deposits, existing models consider both the ^{210}Pb contained in the sediments
7 accumulated in the lake plus the ^{210}Pb atmospheric flux.

8 However, when lake records are not available the use of other kinds of
9 deposits such as moraine soils can be made. Hence, for recent moraine soils, there is
10 no input of sediments; only that of the atmospheric ^{210}Pb fallout.

11 Considering this assumption we propose the following accumulation-decay
12 model:

$$13 \quad A_n = I + \lambda I + \lambda^2 I + \lambda^3 I + \dots + \lambda^{n-1} I + \lambda^n I \quad [1]$$

14 where: $A_n(\text{Bq} \cdot \text{m}^{-2})$ is the $^{210}\text{Pb}_{\text{ex}}$ inventory after n years since glacier retreat; I (Bq
15 $\cdot \text{m}^{-2}$) is the annual inventory of $^{210}\text{Pb}_{\text{ex}}$ fallout from the atmosphere; λ is the decay
16 constant of ^{210}Pb ($\lambda = 0.969$); n is the time span between the sampling and glacier
17 retreat (in years).

18 The change in the $^{210}\text{Pb}_{\text{ex}}$ inventory in soil can be described by equation [1],
19 assuming that the deposited fallout of $^{210}\text{Pb}_{\text{ex}}$ from the atmosphere is totally absorbed
20 by the soil and that there is no loss with runoff resulting from rainfall or snow melt.
21 The mass balance model is not applicable in situations where the $^{210}\text{Pb}_{\text{ex}}$ fails to reach
22 a steady state equivalent to four decay periods (around 100 years).

1 Furthermore, the likely loss of ^{222}Rn by exhalation (Du & Walling, 2012),
2 especially in coarse textured soils has to be considered. Then, assuming equilibrium
3 the supported ^{210}Pb will be less than that estimated from ^{226}Ra . However, as soils
4 develop and became enriched in organic matter, the importance of such an effect
5 would decline with time. In addition, the mass balance places emphasis on changes in
6 the relative magnitude of the inventory over time rather than on its absolute
7 magnitude.

8 However, under natural conditions, following ^{210}Pb deposition on the ground
9 due to precipitation, part of the $^{210}\text{Pb}_{\text{ex}}$ fallout is lost through runoff, which transports
10 fine soil particles as well as snow melt. As the development of soil and vegetation
11 continues, the proportion of $^{210}\text{Pb}_{\text{ex}}$ lost (θ) with runoff will decrease with time, and
12 this can be expressed by the following power-exponential function, describing the
13 shape of the curve presented in Figure 5:

$$14 \qquad \qquad \qquad \theta_i = bc^i \qquad \qquad \qquad [2]$$

15 where, θ is the proportion of $^{210}\text{Pb}_{\text{ex}}$ lost with runoff; b and c are $^{210}\text{Pb}_{\text{ex}}$ runoff loss
16 coefficients, respectively, i is the time spans. b is the initial loss coefficient of $^{210}\text{Pb}_{\text{ex}}$,
17 which is related to the erodibility of moraine soil after glacier retreated, its value is
18 between 0 and 1. For sandy moraine soils without vegetation cover, the stronger the
19 rainfall erosion intensity is, the closer the value b approaches to 1. c is a parameter
20 related to the rate of vegetation restoration, usually between 0.9 and 1. When c is 1, it
21 means that the bare moraine soils have no vegetation restoration over time, the
22 smaller the value of c , the faster the rate of vegetation restoration. In this study area,

1 the simulation value of coefficient c is 0.9764, it means when i is 100 years, the
2 proportion of $^{210}\text{Pb}_{\text{ex}}$ lost with runoff (θ_{100}) is 0.055.

3 Considering losses of $^{210}\text{Pb}_{\text{ex}}$ fallout with runoff transporting fine particles in
4 which $^{210}\text{Pb}_{\text{ex}}$ is fixed, the accumulation and decay model is described as:

$$5 \quad A_n = I(1 - bc^n) + \lambda I(1 - bc^{n-1}) + \lambda^2 I(1 - bc^{n-2}) + \dots + \lambda^{n-1} I(1 - bc) +$$
$$6 \quad \lambda^n I(1 - b) \quad [3]$$

7 and equation [3] can be re-expressed as:

$$8 \quad A_n = I \left[\frac{1 - \lambda^{n+1}}{1 - \lambda} - \frac{b(c^{n+1} - \lambda^{n+1})}{c - \lambda} \right] \quad [4]$$

9 The application of the model in a region requires independent information on
10 the date of the moraine deposit after glacier retreat, in order to calibrate the model and
11 calculate the coefficients b and c .

12 **4.3 Testing the $^{210}\text{Pb}_{\text{ex}}$ accumulation-decay model using data from Hailuogou** 13 **Valley**

14 The R9 site where the glacier retreated in 1910 is covered by dense conifer
15 forests and has well-developed brown soil with a thick layer of litter in the sampling
16 year 2016. It also had the highest $^{210}\text{Pb}_{\text{ex}}$ inventory of $10,718.9 \pm 167.4 \text{ Bq} \cdot \text{m}^{-2}$ and
17 perfect depth distribution curves. The 106-year time span between when the moraine
18 was deposited and the sampling year is five times that of the ^{210}Pb decay half-life
19 (22.6 years). Therefore, the inventory of $10,718.9 \text{ Bq} \cdot \text{m}^{-2}$ was taken to represent the
20 reference inventory in the study area and the annual inventory of $^{210}\text{Pb}_{\text{ex}}$ fallout (I)
21 was derived as $344.5 \text{ Bq} \cdot \text{m}^{-2}$ on this basis. The $^{210}\text{Pb}_{\text{ex}}$ runoff loss coefficients b and c
22 can be derived from the annual inventory of $^{210}\text{Pb}_{\text{ex}}$ fallout (I) and $^{210}\text{Pb}_{\text{ex}}$ inventories

1 (A_n) for a number of time spans (n) using the solver tool in Microsoft Excel. The
2 coefficients of b and c were derived as 0.6006 and 0.9764, respectively, from the
3 $^{210}\text{Pb}_{\text{ex}}$ inventories (A_n) and the time spans (n) for the nine sites. The goodness-of-fit
4 (GOF) model was tested using the calculated relative difference between actual and
5 modelled values (Motha et al., 2003) as in equation [5]:

$$6 \quad \text{GOF} = \left\{ 1 - \frac{\sum_1^m \left(\frac{|A_n - A_n'|}{A_n} \right) \right\} * 100 \quad [5]$$

7 where A_n' is the modelled value of $^{210}\text{Pb}_{\text{ex}}$ inventory and m is the sample size
8 involved in the parametric simulation of the model. In this case, the nine sites
9 generated a GOF of 65.5%. However, by excluding sites R3 and R6, where the $^{210}\text{Pb}_{\text{ex}}$
10 inventory values are irregularly low because of severe erosion since the glacier
11 retreated from these sites, the GOF reached 90% with values of the coefficients b and
12 c of 0.6011 and 0.9756, respectively.

13 These results show the potential for dating moraine deposits after glacier
14 retreat despite some of the moraine deposits deviating from the curve fit, suggesting
15 that more research is needed to improve the adjustment of the model (Table 3, Figure
16 5).

17 **5 Conclusions**

18 Both ^{137}Cs and $^{210}\text{Pb}_{\text{ex}}$ fallout inventories in moraine soils increase as time
19 increases due to glacier retreat in the Hailuogou Valley. The $^{210}\text{Pb}_{\text{ex}}$ inventories
20 increased from $3,669.6 \pm 218.5 \text{ Bq}\cdot\text{m}^{-2}$ at the site where glacier retreated in 1990 to
21 $10,718.9 \pm 167.4 \text{ Bq}\cdot\text{m}^{-2}$ at the site in 1910; however, little ^{137}Cs fallout was detected
22 in the soils where the glacier retreated after the 1960s because of limited nuclear

1 weapon testing in the world since that time. Based on the physical processes of fallout
2 deposition, decay and losses with runoff, a $^{210}\text{Pb}_{\text{ex}}$ accumulation-decay model was
3 developed for assessing the time of glacier retreat by dating moraine soils over the
4 past 100 years.

5 The calculated glacier retreat times for seven of the nine sampled sites are in
6 good agreement with actual measured times, thereby showing the potential for using
7 the $^{210}\text{Pb}_{\text{ex}}$ technique for dating moraine soils in other cryosphere regions. A careful
8 selection of the sampling sites is important for model results and for reproducibility of
9 b and c coefficients, therefore stable soils with no signs of erosion and not receiving
10 runoff from adjacent areas should be selected.

11 Further research is needed to test the broader applicability of the approach
12 reported here and to validate the model for additional sites including determination of
13 the runoff loss coefficients b and c under different environmental conditions and
14 settings. A similar approach could be applied to other types of recently developed
15 sedimentary soils forming a landform sequence as in the case of moraines, such as
16 soils on debris flows and alluvial fans that, after their occurrence, stabilise and are not
17 later covered by further sediment deposits.

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30 **Figure captions**

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3 **Fig. 1.** Location of the research area in the Hailuogou Glacier Valley and sampling sites

4 **Fig. 2.** Particle size depth distributions of moraine soils at the nine sampling sites

5 **Fig. 3.** ^{137}Cs depth distributions in the soils at each of the moraine sampling sites

6 **Fig. 4.** $^{210}\text{Pb}_{\text{ex}}$ depth distributions in the soils at the nine moraine sampling sites

7 **Fig. 5.** Exponential relationship between $^{210}\text{Pb}_{\text{ex}}$ inventories and the span times between the
8 ages of the moraine deposited after glacier retreat and the sampling year

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Table 1. Locations and glacier retreat times for the sampling sites

Sites	Retreat time	Latitude north	Longitude east	Altitude (m)	Distance from 2017's glacier toe (m)
R1	1990	29°34'05"	101°59'23"	2950	350
R2	1983	29°34'07"	101°59'44"	2938	510
R3	1972	29°34'13"	101°59'49"	2935	810
R4	1966	29°34'16"	101°59'54"	2945	1030
R5	1958	29°34'21"	102°00'03"	2925	1213
R6	1945	29°34'28.2"	102°00'18.5"	2934	1570
R7	1930	29°34'30.9"	102°00'23.7"	2913	1770
R8	1915	29°34'33.8"	102°00'28"	2890	2016
R9	1910	29°34'35.2"	102°00'32.4"	2832	2100

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Table 2. ^{137}Cs and $^{210}\text{Pb}_{\text{ex}}$ inventories in soils at the nine moraine sampling sites.

Sites (glacier retreat time)	R1 (1990)	R2 (1983)	R3 (1972)	R4 (1966)	R5 (1958)	R6 (1945)	R7 (1930)	R8 (1915)	R9 (1910)
^{137}Cs inventory (Bq/m ²)	17.28	30.63	105.07	9.29	151.77	588.24	891.23	764.73	818.91
Errors	15.3	25.1	17.4	8.5	46.3	39.8	54.3	29.8	50.1
$^{210}\text{Pb}_{\text{ex}}$ inventory (Bq/m ²)	3669.6	4180.4	2026.9	8341.2	6966.7	4710.7	8704.2	7359.2	10718.9
Errors	218.5	216	327.1	232	244.5	147.1	143.6	67.3	167.4

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1 **Table 3.** The actual and modelled span times (n) between the age of the moraine deposit
2 formed after glacier retreat and the sampling year.

sites	R1	R2	R3	R4	R5	R6	R7	R8	R9
Actual span times (year)	26	33	44	50	58	71	86	101	106
Modelled span times (year)	26.2	30.5	13.6	79.1	58.7	35.1	86	63.8	169.8

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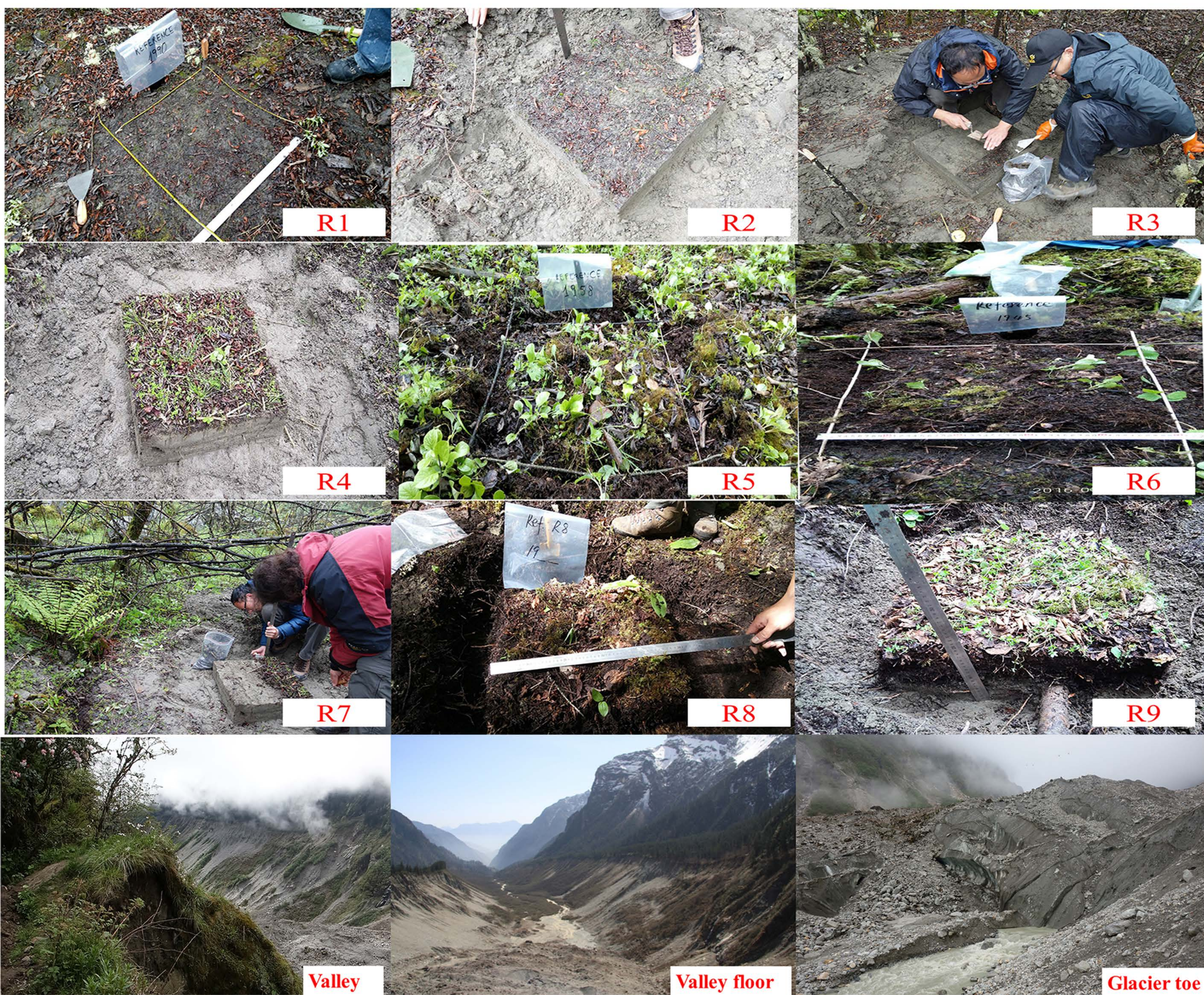
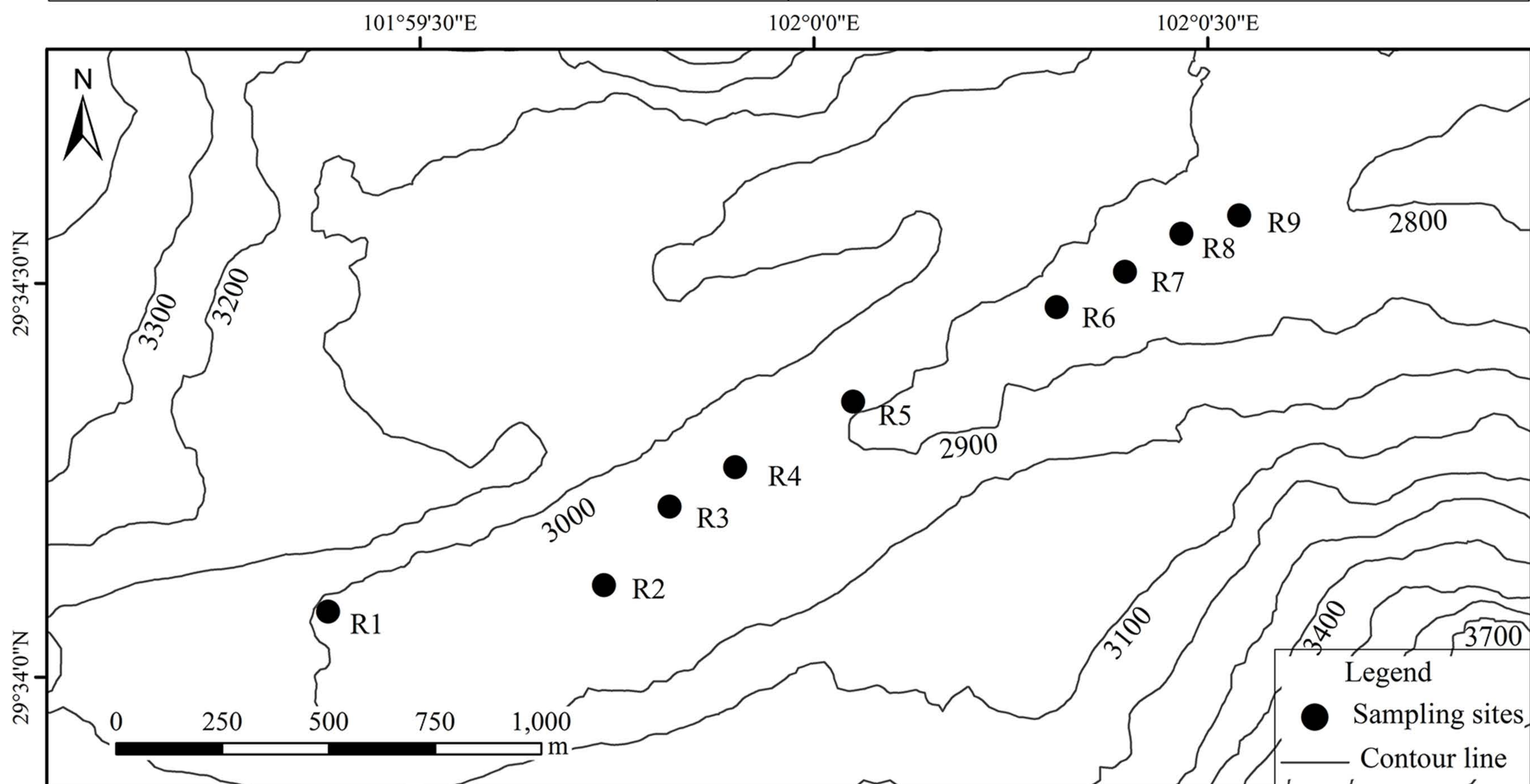
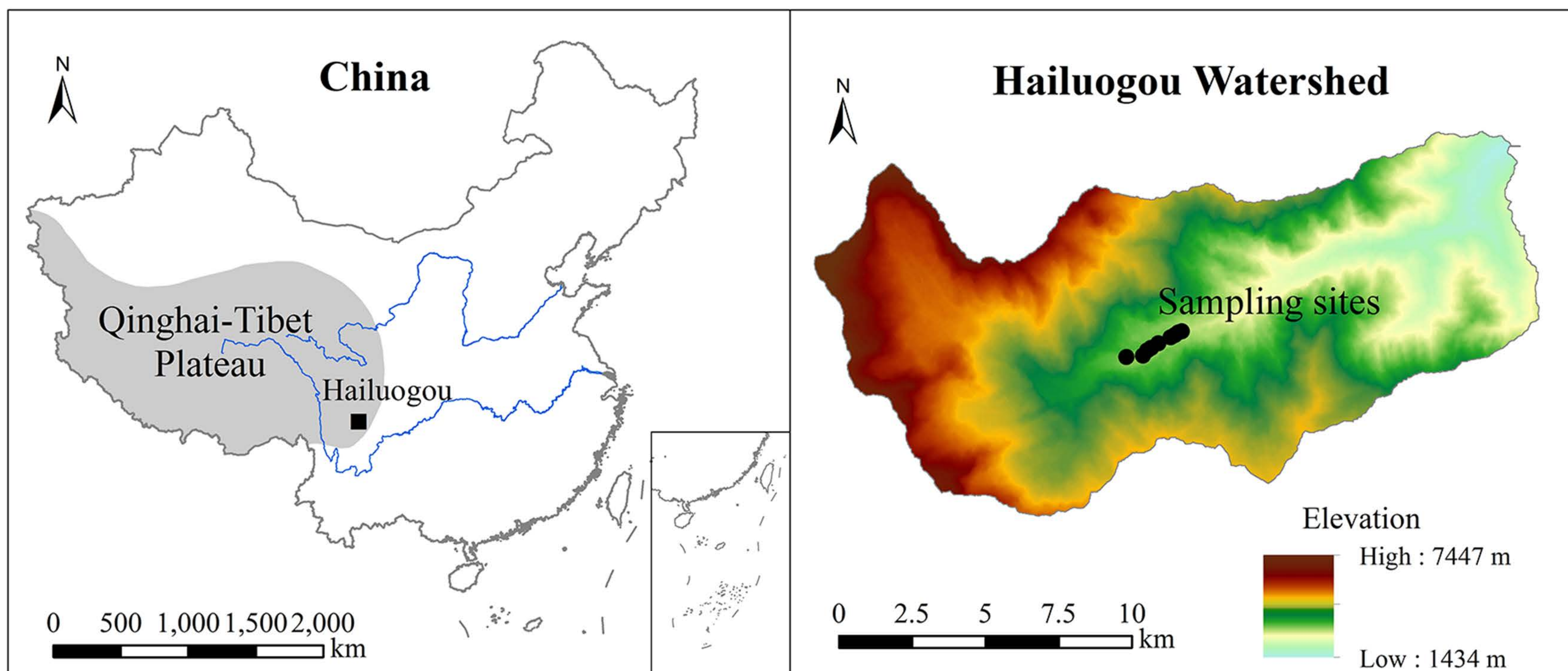
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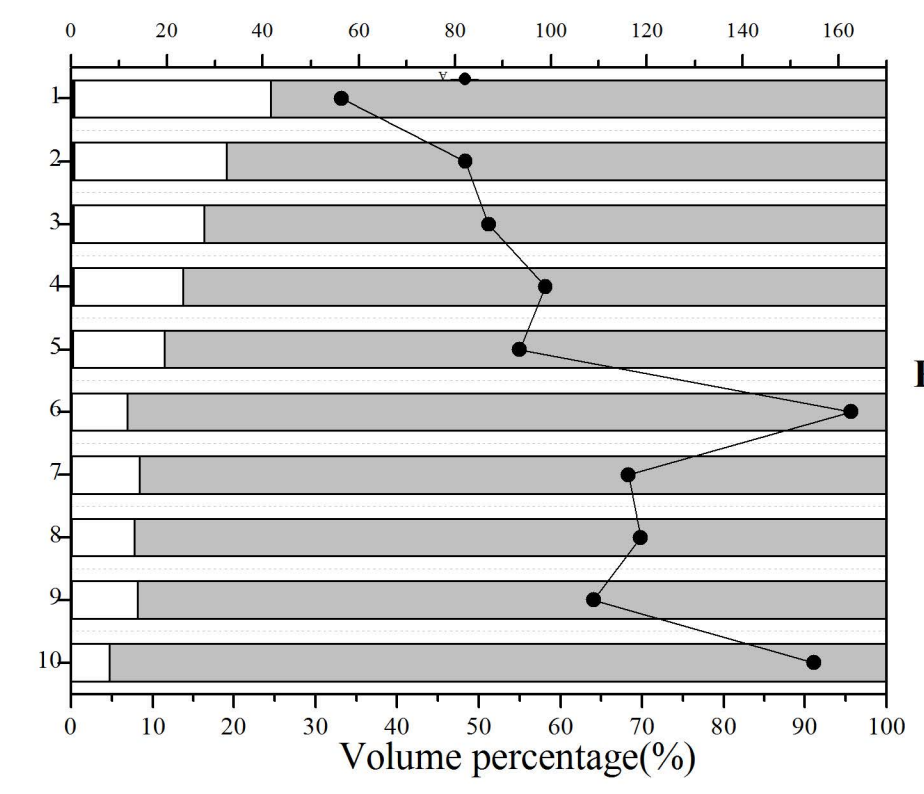
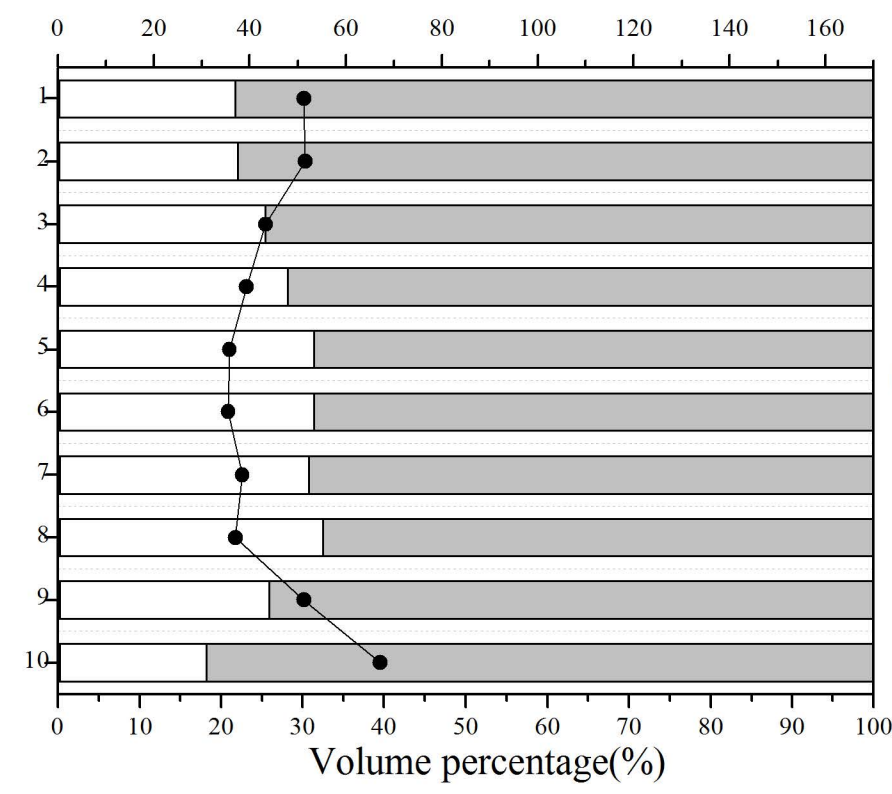
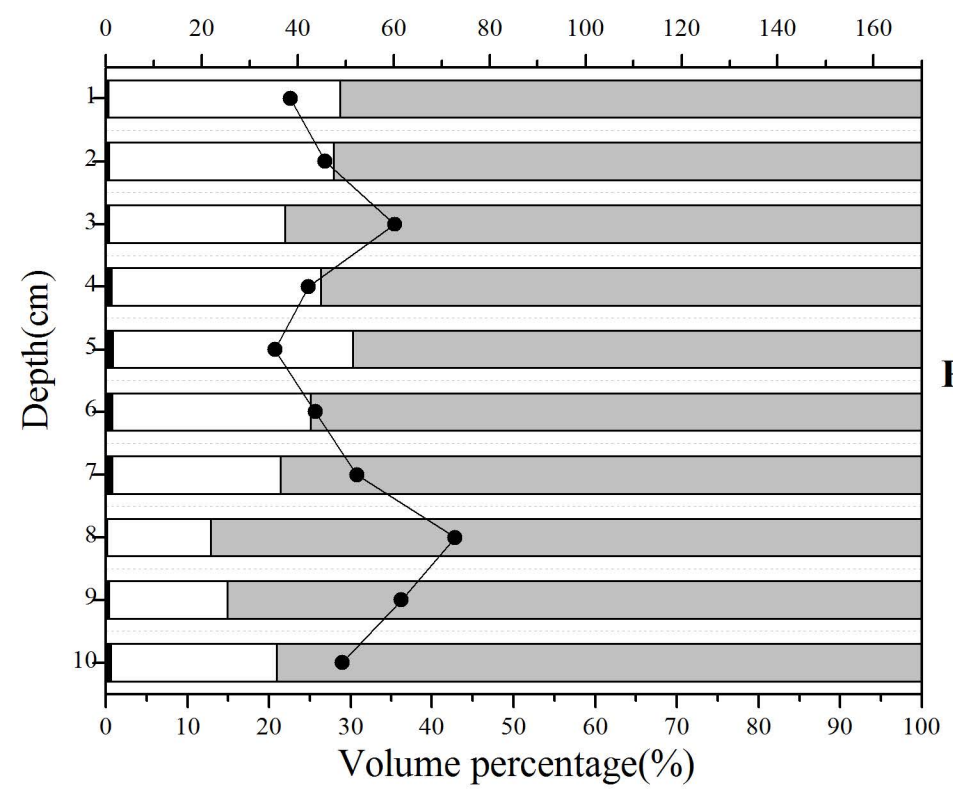
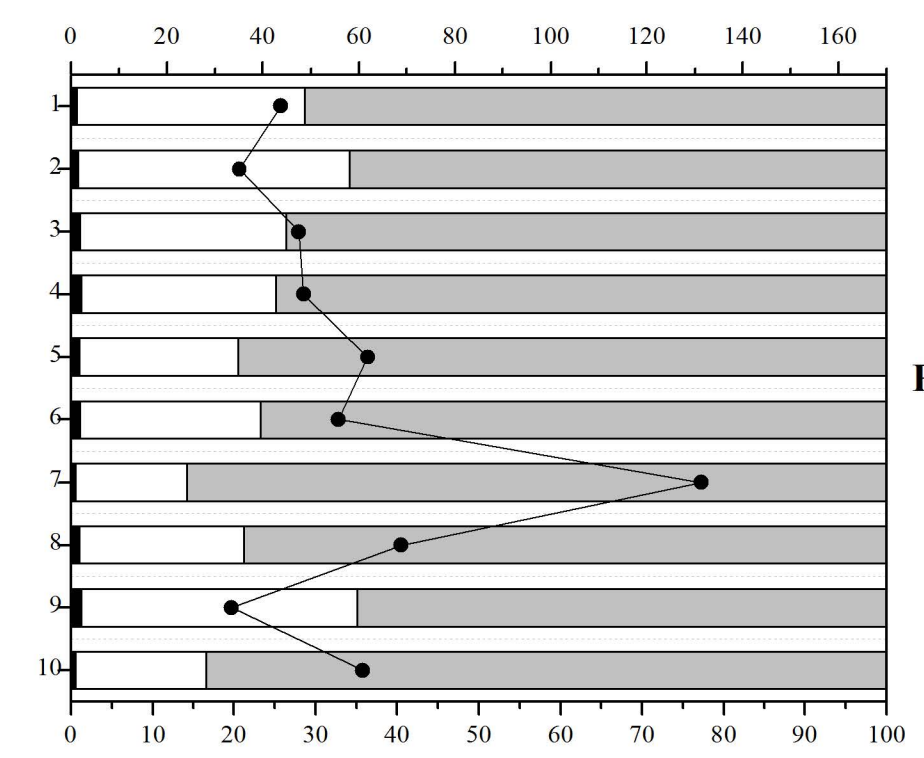
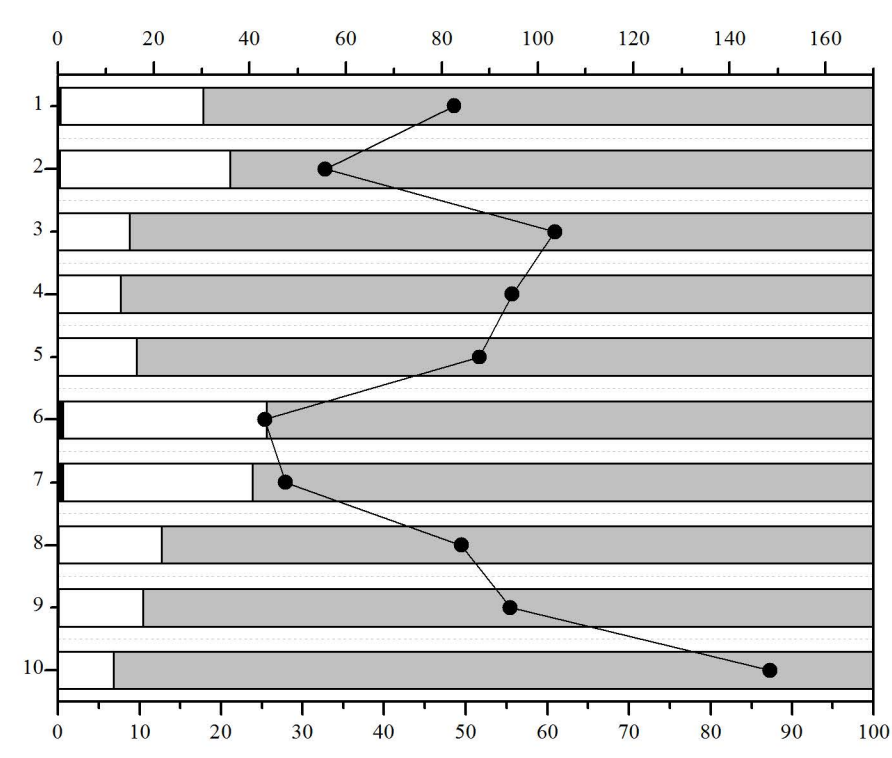
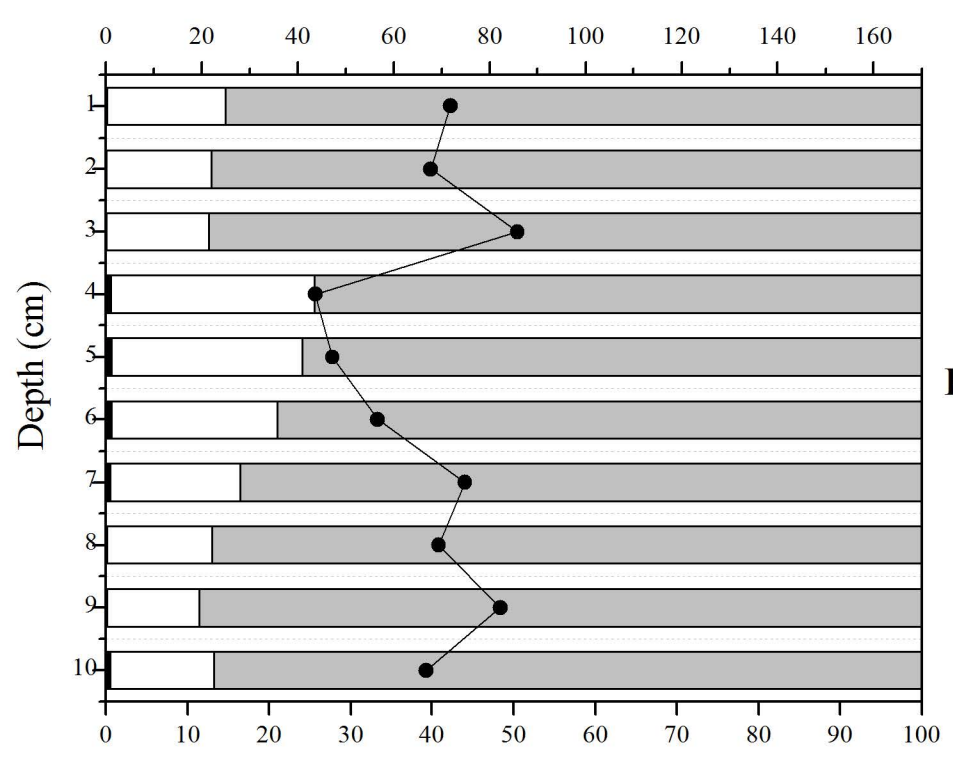
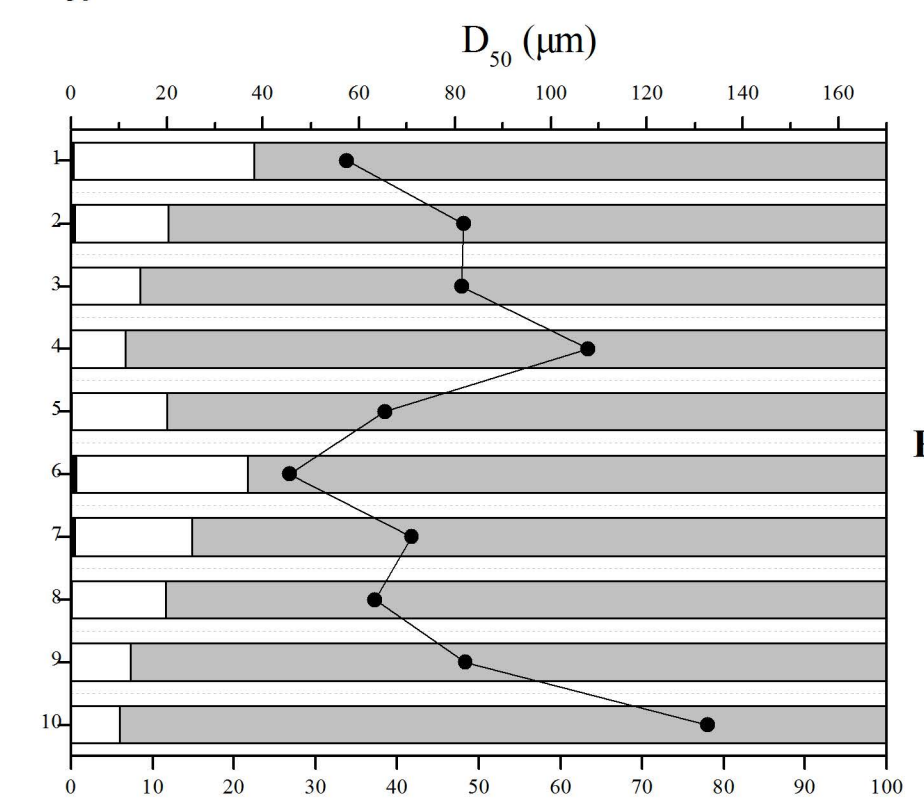
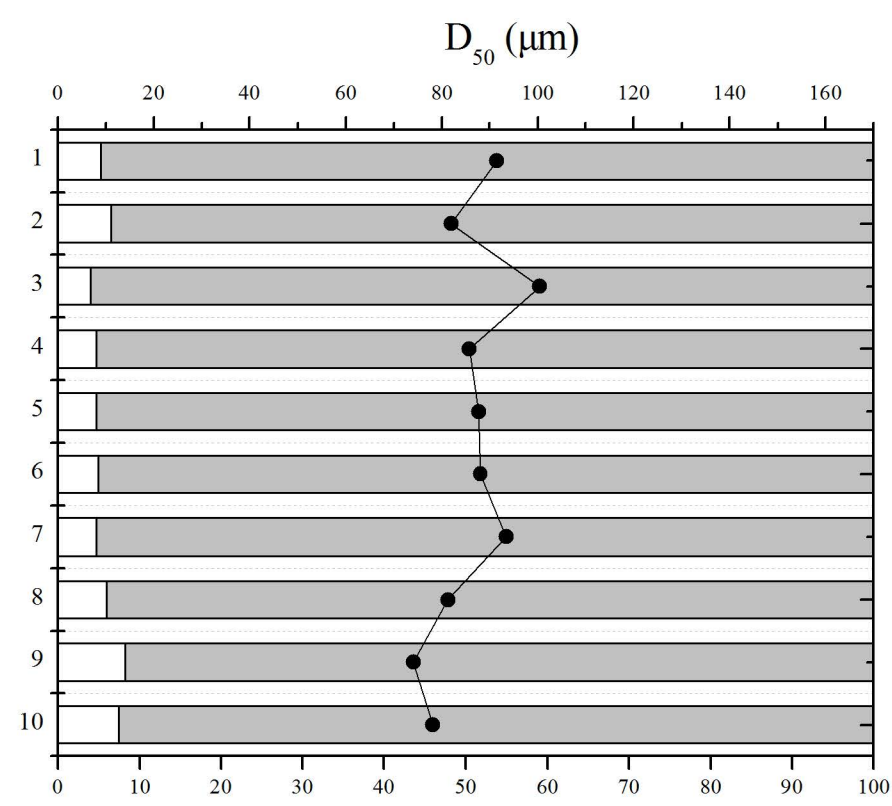
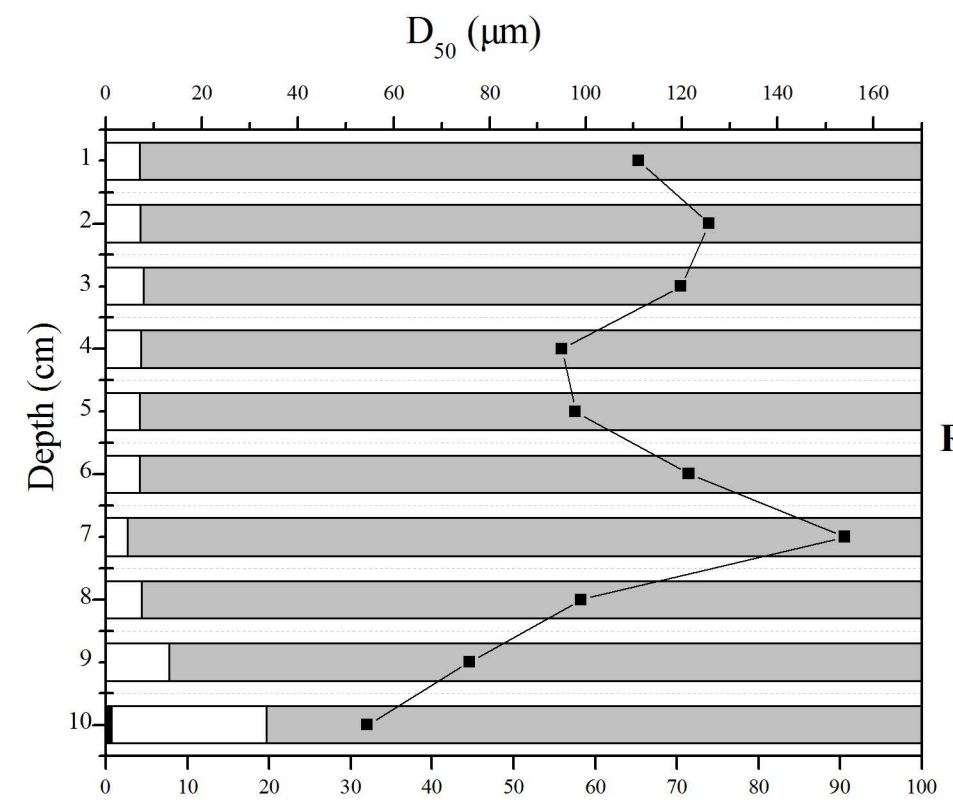
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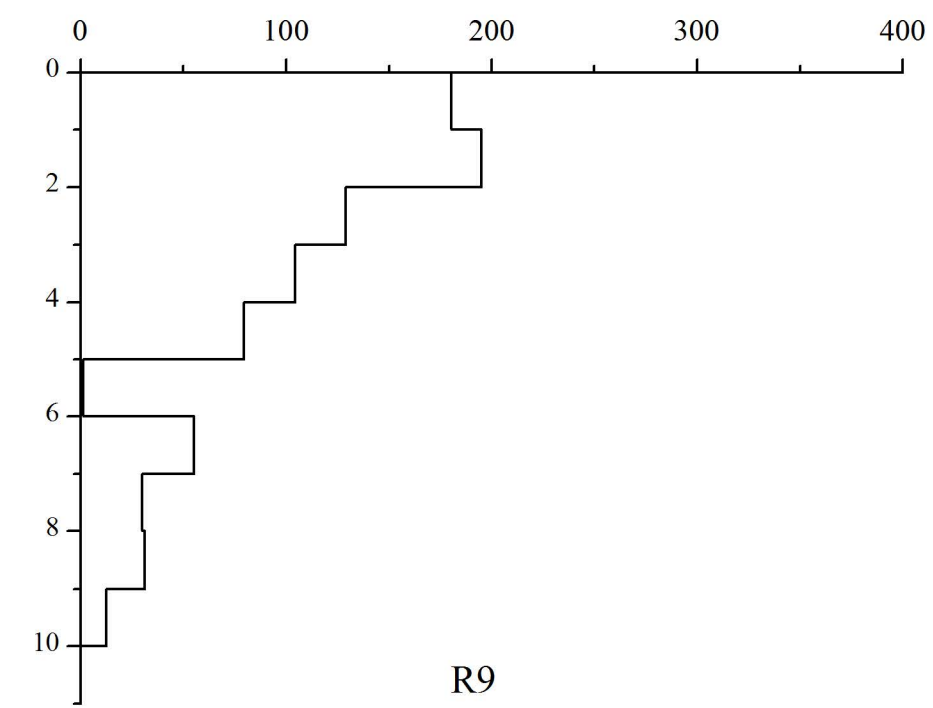
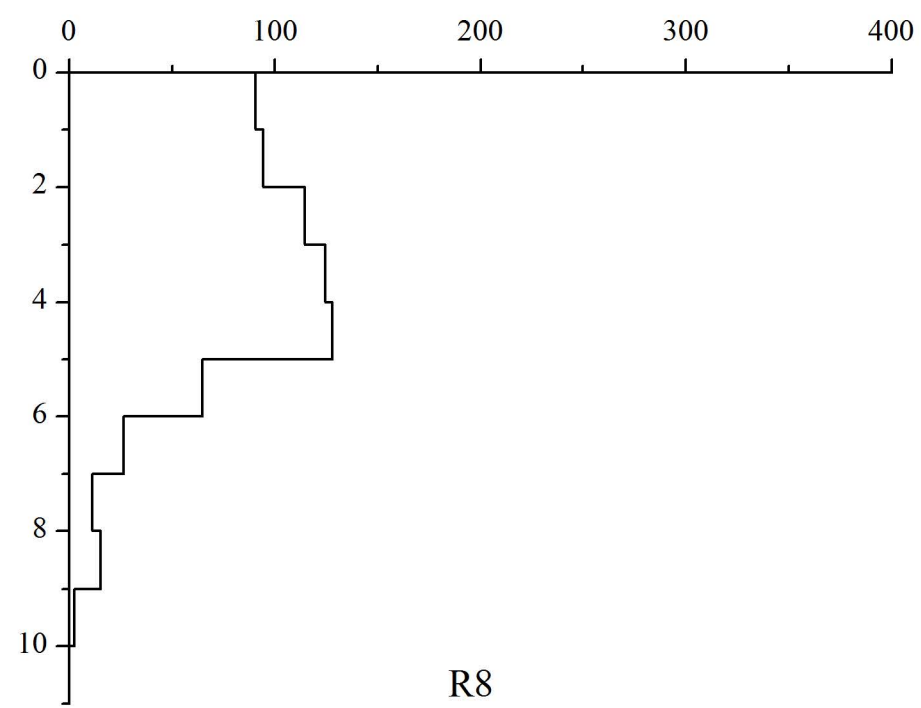
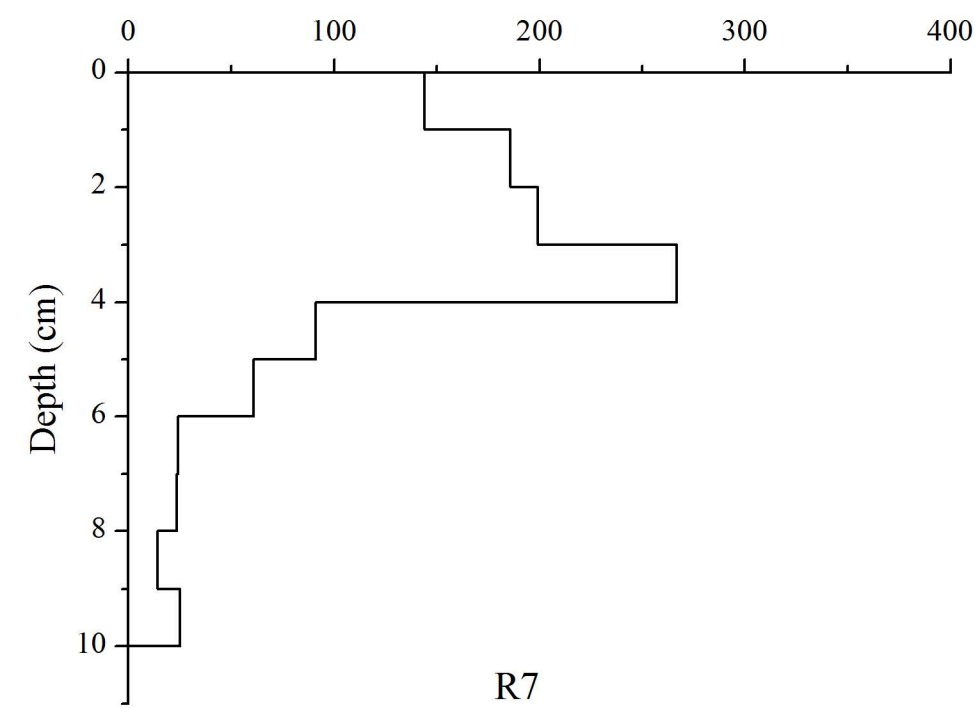
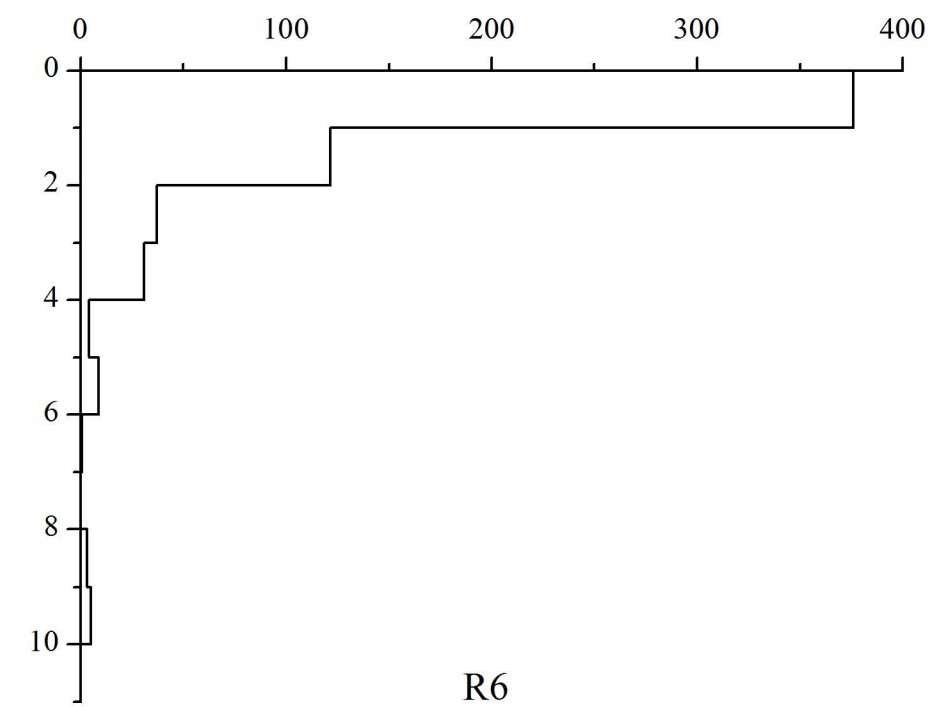
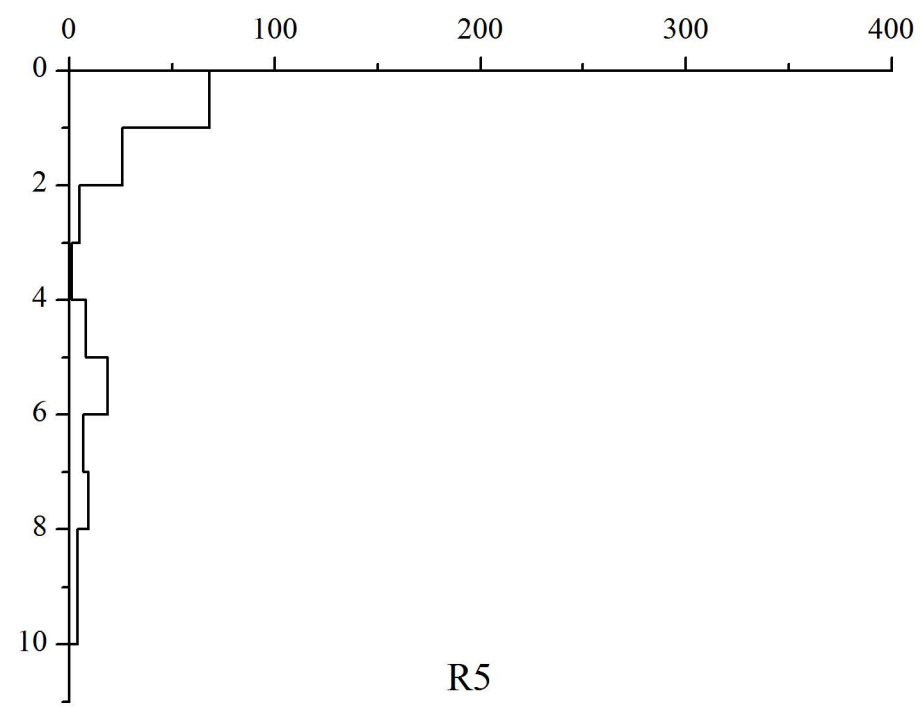
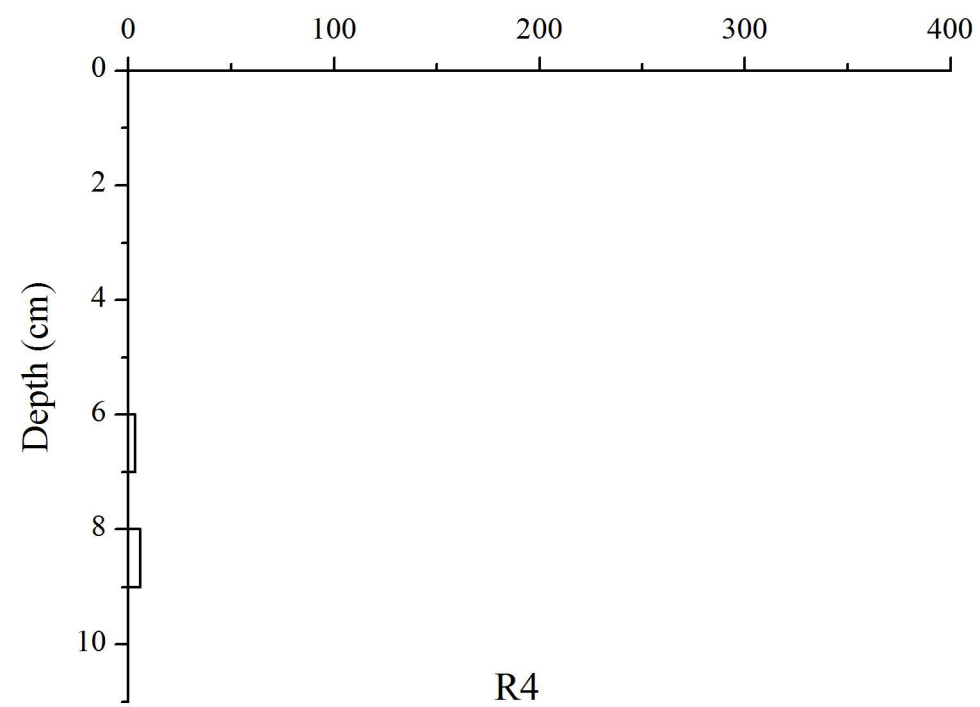
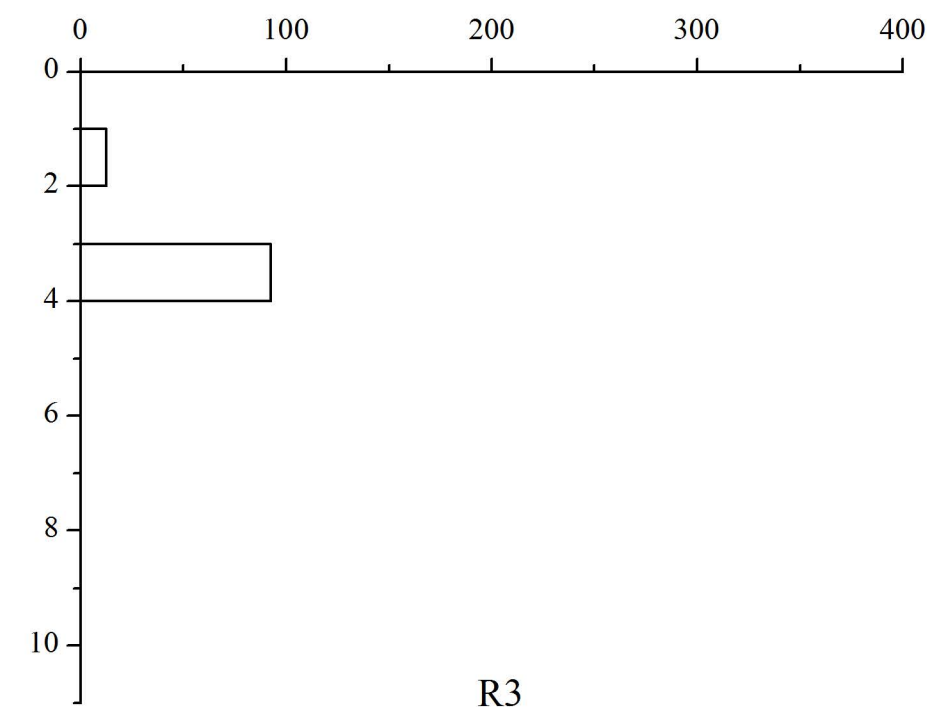
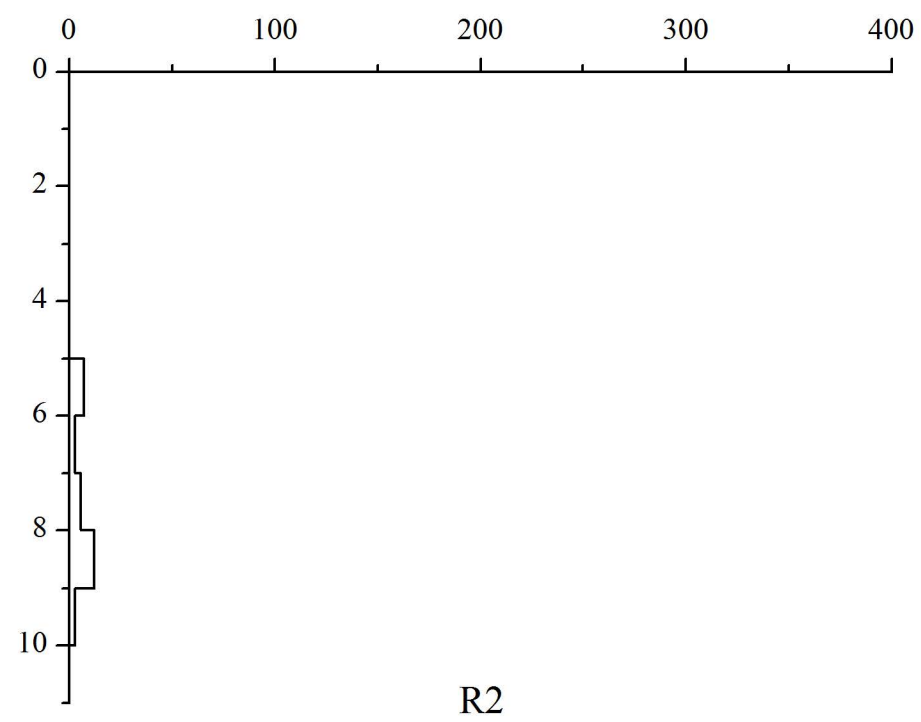
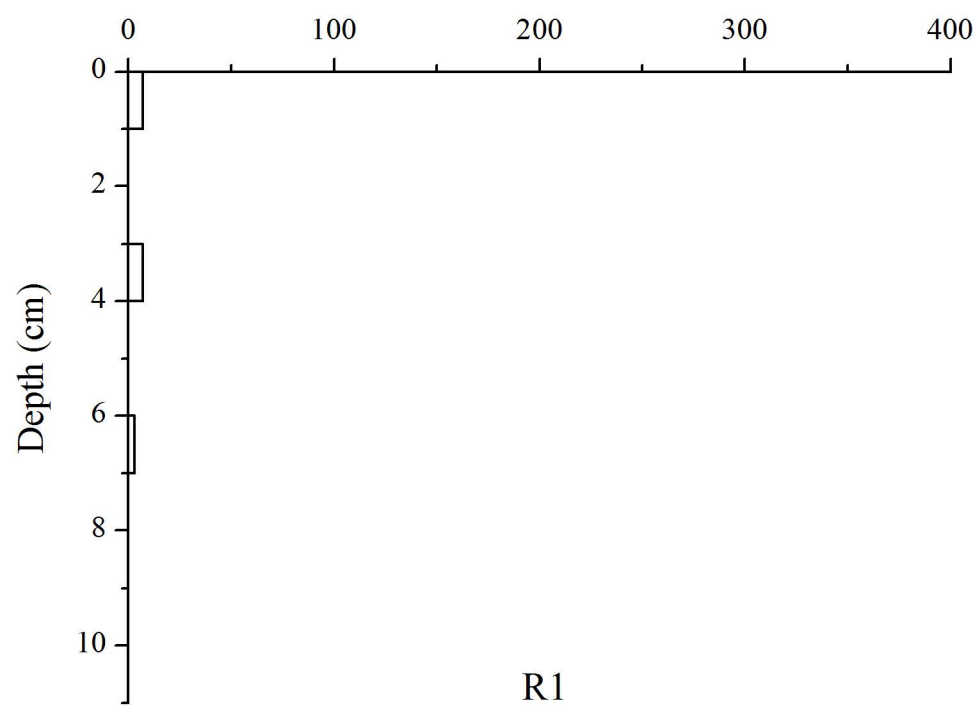
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sand
 silt
 clay
 D_{50}



^{137}Cs Mass activity (Bq/kg)



The $^{210}\text{Pb}_{\text{ex}}$ Accumulation-decay Model

