# Rotation and pulsation in Ap stars: first light results from TESS sectors 1 and 2 

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#### Abstract

We present the first results from the Transiting Exoplanet Survey Satellite (TESS) on the rotational and pulsational variability of magnetic chemically peculiar A-type stars. We analyse TESS 2-min cadence data from sectors 1 and 2 on a sample of 83 stars. Five new rapidly oscillating Ap (roAp) stars are announced. One of these pulsates with periods around 4.7 min , making it the shortest period roAp star known to date. Four out of the five new roAp stars are multiperiodic. Three of these and the singly periodic one show the presence of rotational mode splitting. Individual frequencies are provided in all cases. In addition, seven previously known roAp stars are analysed. Additional modes of oscillation are found in some stars, while in others we are able to distinguish the true pulsations from possible aliases present in the ground-based data. We find that the pulsation amplitude in the TESS filter is typically a factor of 6 smaller than that in the $B$ filter, which is usually used for ground-based observations. For four roAp stars we set constraints on the inclination angle and magnetic obliquity, through the application of the oblique pulsator model. We also confirm the absence of roAp-type pulsations down to amplitude limits of 6 and $13 \mu \mathrm{mag}$, respectively, in two of the best characterized nonoscillating Ap (noAp) stars. We announce 27 new rotational variables along with their rotation periods, and provide different rotation periods for seven other stars. Finally, we discuss how these results challenge state-of-the-art pulsation models for roAp stars.


Key words: stars: chemically peculiar - stars: individual - stars: oscillations - stars: magnetic fields - stars: variables.

## 1 INTRODUCTION

Ap stars are chemically peculiar stars with enhanced abundances of $\mathrm{Si}, \mathrm{Cr}, \mathrm{Sr}$, or Eu , permeated by relatively strong magnetic fields (Preston 1974). That makes them test beds for the modelling of the physical processes responsible for element segregation in stars, such as gravitational settling and radiative levitation. They are relatively

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slow rotators and their magnetic field axis is usually found to be inclined with respect to the rotation axis. Moreover, as a result of element segregation in the presence of magnetic fields, some of the chemical elements are unevenly distributed at the surface (e.g. Kochukhov 2011). As a consequence of the magnetic field being inclined to the rotation axis (Stibbs 1950), many of these stars show light, spectral, and magnetic field variations over a period of rotation, and are commonly known as $\alpha^{2}$ Canum Venaticorum variables (hereafter, $\alpha^{2} \mathrm{CVn}$ stars) (Samus et al. 2017). Still, for some stars, no such rotational variations are detected indicating
that either the rotation period is too long to be measured within the observational time span, or the star has a very particular configuration, such as a rotation axis pointing towards the observer or a very small magnetic obliquity and no chemical spots away from the magnetic poles.
Some of the Ap stars exhibit high radial-order acoustic pulsations. First discovered by Kurtz (1978, 1982), they are known as the rapidly oscillating Ap stars (hereafter, roAp stars). A number of searches for new pulsators of this class have been made since, through both ground-based surveys (Martinez \& Kurtz 1991; Holdsworth et al. 2014a; Paunzen et al. 2015; Joshi et al. 2016) and space-based data (Balona et al. 2010, 2011; Kurtz et al. 2011; Holdsworth et al. 2014b; Smalley et al. 2015; Bowman et al. 2018). At the time of launch of the NASA Transiting Exoplanet Survey Satellite (TESS) mission (Ricker et al. 2014), 61 roAp stars had been discovered (Smalley et al. 2015; Joshi et al. 2016). They are found on the main sequence, among the cooler Ap stars, with temperatures ranging from about 6000 to 9000 K and have large-scale magnetic fields with strengths of a few kG (see Mathys 2017, for definitions of the different types of magnetic field measurements performed in Ap stars and their typical values). The survey nature of the TESS satellite opens a new window of opportunity for finding additional members of this rare and unique class of pulsating star. In turn, these observations will set strong constraints on the modelling of key aspects of the stellar physics, such as the macroscopic and microscopic processes that define the distribution of elements in the stellar atmospheres and interiors.

Of particular interest for constraining structural models of Ap stars, as well as their magnetic fields, are pulsators exhibiting multiple modes (the multiperiodic roAp stars). In the absence of a strong magnetic field, and assuming all modes within a given frequency range were to be observed, the oscillation spectrum of an roAp star would be expected to show a regular pattern of alternating even and odd degree modes, as asymptotically predicted for high radial-order acoustic oscillations (Shibahashi 1979; Tassoul 1980). However, in classical pulsators mode selection is usually present (see Aerts, Christensen-Dalsgaard \& Kurtz 2010, for a discussion) and not all modes in that pattern are necessarily visible. In addition, because of the strong magnetic field, the waves in the outer layers of roAp stars become magnetoacoustic in nature with a consequent change in the mode oscillation frequencies. Theory predicts that the oscillation spectra of these stars may still exhibit an almost equidistant set of peaks, whose separation is only a few $\mu \mathrm{Hz}$ larger than that expected in the absence of the magnetic field, but that they may also show a few modes at frequencies that do not follow that equidistant pattern predicted by the asymptotic analysis. These significant anomalies in the mode frequencies occur when the coupling between the acoustic and magnetic waves is strongest (Cunha \& Gough 2000; Cunha 2001, 2006; Saio \& Gautschy 2004; Saio 2005). Indeed, some known multiperiodic roAp stars do show such frequency anomalies (e.g. Kurtz et al. 2005; Gruberbauer et al. 2008; Huber et al. 2008). By revisiting most known roAp stars, TESS will discover additional pulsation modes, revealing many of these stars to be multiperiodic, in addition to the multiperiodic roAp stars that the satellite will discover for the first time. Likewise, rotationally split frequency multiplets discovered by TESS in previously known or in new roAp stars will provide stringent constraints on the rotational inclination and magnetic obliquity of these stars.

The excitation mechanism responsible for the oscillations observed in roAp stars is still a matter of debate. Currently the most widely accepted theory proposes that these oscillations are driven
by an opacity mechanism in the hydrogen ionization layers in stars where the strong magnetic field is capable of suppressing envelope convection, at least in some region around the magnetic poles (Balmforth et al. 2001). Based on this theory, Cunha (2002) determined the the maximum extent of the region of pulsational instability for roAp stars in the HR diagram (hereafter, the theoretical instability strip), derived by assuming that envelope convection in these stars is suppressed at all latitudes (see Aerts et al. 2010 for a general discussion of the classical instability strip).
A few problems have been identified by confronting the theoretical results with observations. Among these problems is the existence of some roAp stars that pulsate with frequencies higher than those predicted by the models (Cunha et al. 2013; Holdsworth et al. 2018); this is one of the most interesting challenges for the theory. Cunha et al. (2013) have shown some evidence that these very high frequencies may be excited by an entirely different mechanism, associated with the turbulent pressure, but a thorough test of this possibility still needs to be performed. In fact, a similar mechanism seems to be responsible for the excitation of high radialorder acoustic modes in some $\delta$ Scuti stars (Antoci et al. 2014).
Another important open problem concerns the region of pulsational instability for the roAp stars in the HR diagram. Inspection of the effective temperatures known prior to the launch of TESS indicates the existence of roAp stars that are cooler than the red (i.e., cooler) edge of the theoretical instability strip. Likewise, roAp stars have not yet been found close to the blue (i.e., hotter) edge of the theoretical instability strip. Moreover, many stars with properties very similar to the roAp stars have been searched for pulsations without success. Those stars are commonly known as non-oscillating Ap stars (hereafter, noAp stars). TESS allows us, for the first time, to test whether these apparent disagreements between theory and observations are a consequence of an observational bias, resulting from selection effects on the samples observed so far, or from a lower intrinsic amplitude of the pulsational variability in hotter stars.
In this work we present the analysis of TESS data on Ap stars, from the 27-d data sets for sectors 1 and 2 (see Ricker et al. 2014 for an explanation of the TESS observing strategy), observed in 2-min cadence. In Section 2 we describe the sample of stars under study, and describe the data analysis techniques employed. In Section 3 we present the results of our analysis, including the determination of rotation periods and pulsational variability. Sections 4 and 5 present detailed TESS results on the newly discovered roAp stars and previously known roAp stars, respectively. Section 6 makes a comparison between pulsation amplitudes as seen by TESS and Johnson $B$ observations. In Section 7 we discuss the results on two well-characterized noAp stars, and in Section 8 we summarize our main results and conclude.

## 2 ANALYSIS

In this work we have used data from sectors 1 and 2 of the TESS mission. We present the analysis of 83 stars with spectral types from late B to early F, of which 80 have previously been identified as peculiar, or suspected peculiar, with enhanced $\mathrm{Sr}, \mathrm{Cr}, \mathrm{Eu}$, and/or Si. The 80 chemically peculiar stars are a subset of the nearly 1400 targets proposed for observation with the 2-min cadence of TESS during the nominal mission, in the context of the roAp programme of the TESS Asteroseismic Science Consortium (TASC). The targets proposed for observation included (1) 56 previously known roAp stars; (2) 13 well-characterized noAp stars; (3) 40 stars observed by the KELT survey (Pepper, Stassun \& Gaudi 2018) and found
to show evidence for pulsations in the frequency range from 700 to $3000 \mu \mathrm{~Hz}$; and (4) 1273 additional stars from the Michigan Spectral Catalogues (Houk \& Cowley 1975; Houk 1978, 1982; Houk \& Smith-Moore 1988; Houk \& Swift 1999) with an Ap spectral classification. In particular, the current subset of 80 Ap stars comprises 7 previously known roAp stars, 2 noAp stars, and 71 Ap stars selected from the Michigan Spectral Catalogues. The three additional stars in the sample of 83 stars reported here, namely, TIC 152808505, TIC 350146296, and TIC 407661867, have not been classified as chemically peculiar in the literature and were not part of the targets selected in the context of the roAp programme. Nevertheless, they were observed with the 2-min cadence by TESS and included in our present sample because hints of high-frequency pulsations have been found in their light curves in the context of a systematic search for pulsations in over 5000 stars with $T_{\text {eff }}>$ 6000 K observed with the TESS 2-min cadence. Of the 83 stars in our sample, 77 are listed in the General Catalogue of Ap and Am stars (Renson \& Manfroid 2009).

### 2.1 Properties of the sample

The properties of our sample are given in Table 1. Two effective temperatures, $T_{\text {eff }}$, are provided, one obtained from the TESS Input Catalogue (TIC) ${ }^{1}$ and the other derived using the Infrared Flux Method (IRFM; Blackwell \& Shallis 1977).

To calculate the effective temperature through the Infrared Flux Method, the stellar spectral energy distributions (SEDs) were obtained using literature broad-band photometry: 2MASS (Skrutskie et al. 2006), Tycho $B$ and $V$ (Høg et al. 2000), APASS9 $B, V, g^{\prime}$, $r^{\prime}$ and $i^{\prime}$ (Henden et al. 2015), USNO-B1 $R$ (Monet et al. 2003), and WISE (Cutri \& et al. 2012). The photometry was converted to fluxes, and the best-fitting Kurucz (1993) model flux distribution was obtained using a weighted Levenberg-Marquardt (Levenberg 1944; Marquard 1963) non-linear least-squares fitting procedure, as implemented in Press et al. (1992). The fitted flux distributions were then numerically integrated to determine the stellar bolometric fluxes. Interstellar reddening was assumed to be zero. The IRFM was then used to determine $T_{\text {eff }}$ values and their uncertainties from the three individual 2MASS photometry bands. The final values given in Table 1 are the weighted mean and uncertainty of the three 2MASS values.

The luminosities for our sample of stars were computed by taking the Gaia DR2 parallaxes (Gaia Collaboration 2018a,b), when available, and the Hipparcos parallaxes (van Leeuwen 2008), otherwise. In both cases we considered the uncertainties quoted in the respective catalogues, but for the Gaia data we inflated the formal errors by 30 per cent, as suggested in the catalogue for stars of magnitude $G<12$. We note also that Gaia DR2 parallaxes do not account for stellar multiplicity, which could, in some cases, influence the luminosities derived. For the bolometric correction we considered the expression of Flower (1996) (where we used the corrected version of the coefficients, published in table 1 of Torres 2010), and assumed an error of 0.13 mag . This error was estimated by computing the bolometric corrections for six roAp stars for which a detailed bolometric flux computation is available (Bruntt et al. 2008, 2010; Perraut et al. 2011, 2013, 2015, 2016) and comparing them with the values predicted by the Flower (1996) expression. The root mean square of the difference between the two bolometric correction values was then adopted as the error for
all stars. As the six stars used in this error estimate have effective temperatures lower than $\sim 9100 \mathrm{~K}$, hence, do not cover the full temperature range in our sample, we have, in addition, computed bolometric corrections using the calibration proposed by Netopil et al. (2008). The latter was derived on the basis of peculiar stars and is valid in the range $7500 \mathrm{~K}<T_{\text {eff }}<19000 \mathrm{~K}$. We found a maximum absolute difference of 0.12 mag between the bolometric corrections from Flower (1996) and Netopil et al. (2008) in our sample, which is comparable to the error assumed. Finally, we considered the $V$ magnitude from the TIC catalogue and assumed an uncertainty of 0.02 mag , corresponding to the typical spread in results seen in literature. The luminosities and associated errors computed from these data are given in the 8th and 9th columns of Table 1. No extinction was considered in that calculation. In addition, we computed the luminosity corrected for extinction (10th column in the same table), by considering the extinction published by Gontcharov \& Mosenkov (2018). We find that the root mean square of the difference between the logarithmic luminosity values derived with and without accounting for extinction is 0.1 .

Fig. 1 shows the position in the HR diagram of all stars in our sample. Here we have used the effective temperatures and luminosities derived in this work, as listed in columns 6-9 of Table 1.

### 2.2 Data analysis strategy

In this work we have used the PDC_SAP fluxes from the FITS data files retrieved from the Mikulski Archive for Space Telescopes (MAST). ${ }^{2}$ Ten different teams were involved in the analysis of the data. One of these teams, hereafter, the reference team, analysed the data on all stars, in search for both rotational and pulsational variability, so that homogeneous results could be provided. Two other teams analysed the full sample in search for rotational variability. The other seven teams analysed subsamples of the target list for rotational and/or pulsational variability. The distribution of the targets was done in such a way that the rotational variability of each star was inspected by a minimum of three teams and the pulsational variability by a minimum of two. The results from the teams other than the reference team were used to (1) identify apparent inconsistencies and (2) in the case of rotational variability, compute the standard deviation of the periods derived by the different teams. When inconsistencies were found, the teams were asked to revisit their analysis. The most common inconsistency was the derivation of rotational frequencies corresponding to different harmonic values. In those cases, inspection of the light curve and, when available, of the pulsational multiplets, allowed for the identification of the true rotation period. Rotation periods and pulsation frequencies were only considered after these inconsistencies had been understood and removed and only when at least two teams had confirmed a detection.

For the reference team, the data analysis procedure involved the following steps. The extracted fluxes were converted to magnitudes, with the time stamps being corrected for the zero-point offset. Obvious outliers from the light curves were removed by hand in each case (less than 1 per cent in most cases). Where possible, the data from both sectors were combined to increase the time base and reduce the noise level in the amplitude spectra.

For all stars, the data were first analysed at low frequencies $(0-0.12 \mathrm{mHz})$ in the search for rotational modulation. Both a visual

[^0][^1]Table 1. Properties of the 83 stars analysed in this work. Columns show, from left to right: (1) TIC identification number; (2) Henry Draper (HD) Catalogue identification number; (3) spectral type according to Renson \& Manfroid (2009), except where noted otherwise; (4) TIC visual magnitude; (5) TIC effective temperature; (6) effective temperature from the infrared flux method; (7) error on effective temperature from the infrared flux method; (8) luminosity assuming no extinction; (9) error on luminosity assuming no extinction; and (10) luminosity assuming extinction from Gontcharov \& Mosenkov (2018). Entries with ' $\mathrm{N} / \mathrm{A}$ ' indicate that data are not available for that star.

| TIC | HD | Spectral Type | V | $\begin{gathered} T_{\text {eff }}^{\mathrm{TIC}} \\ (\mathrm{~K}) \end{gathered}$ | $\begin{aligned} & T_{\mathrm{eff}}^{\mathrm{IRF}} \\ & (\mathrm{~K}) \end{aligned}$ | $\begin{gathered} \Delta T_{\text {eff }}^{\mathrm{IRF}} \\ (\mathrm{~K}) \end{gathered}$ | $\log \left(L / \mathrm{L}_{\odot}\right)^{\mathrm{noAv}}$ | $\Delta \log \left(L / L_{\odot}\right)^{\mathrm{noAv}}$ | $\log \left(L / L_{\odot}\right)^{\text {Av }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12359289 | 225119 | B9 SiCr | 8.210 | N/A | 10911 | 189 | 2.46 | 0.07 | N/A |
| 12393823 | 225264 | A1 Si Sr | 8.280 | 9433 | 9374 | 186 | 1.35 | 0.06 | 1.44 |
| 12968953 | 217704 | A5 Sr | 10.169 | 7972 | 7881 | 162 | 1.33 | 0.09 | N/A |
| 24693528 | 14944 | A0 Eu | 9.706 | 7522 | 7401 | 153 | 2.05 | 0.07 | N/A |
| 31870361 | 22488 | A3 Sr Eu Cr | 7.510 | 7219 | 6911 | 157 | 1.45 | 0.05 | 1.52 |
| 32035258 | 24188 | A 0 Si | 6.260 | N/A | 13136 | 220 | 2.17 | 0.05 | 2.25 |
| 38586082 | 27463 | A 0 Eu Cr | 6.340 | 8669 | 8594 | 176 | 1.57 | 0.05 | 1.63 |
| 38586127 | 27472 | F0 Eu Cr Sr | 9.956 | 7309 | 7391 | 155 | 1.14 | 0.05 | 1.23 |
| 41259805 | 43226 | A0 Sr Eu | 8.970 | 8034 | 8293 | 172 | 1.08 | 0.05 | 1.23 |
| 52368859 | 10081 | A0 Sr Eu | 9.620 | 9076 | 8726 | 239 | 1.87 | 0.06 | N/A |
| 69855370 | 213637 | F1 Eu Sr | 9.647 | 6587 | 6433 | 148 | 0.69 | 0.05 | 0.77 |
| 89545031 | 223640 | B9 Si Sr Cr | 5.170 | N/A | 13161 | 207 | 2.21 | 0.06 | 2.26 |
| 92705248 | 200623 | A2 SrEuCr | 9.070 | 8808 | 8889 | 199 | 1.16 | 0.07 | 1.25 |
| 115150623 | 201018 | A2 CrEuSr | 8.640 | 9080 | 9891 | 198 | 1.32 | 0.06 | 1.43 |
| 116881415 | 3135 | F3 Si Cr | 9.600 | 7137 | 6765 | 147 | 1.08 | 0.06 | 1.15 |
| 118114352 | 3772 | A9 Si | 10.001 | 6789 | 6869 | 150 | 1.01 | 0.05 | 1.07 |
| 129636548 | 203585 | A0 Si | 5.760 | N/A | 10725 | 185 | 1.91 | 0.05 | 1.95 |
| 139191168 | 217522 | A5 Sr Eu Cr | 7.540 | 6918 | 6888 | 151 | 0.89 | 0.05 | 0.95 |
| 141028198 | 35361 | A2 CrEu | 9.869 | 8192 | 7444 | 157 | 1.74 | 0.06 | N/A |
| 141610473 | 41613 | A3 Eu Cr | 9.672 | 7183 | 6910 | 149 | 1.28 | 0.06 | N/A |
| 144276313 | 221760 | A2 Sr CrEu | 4.690 | 8495 | 8498 | 264 | 1.80 | 0.06 | 1.85 |
| 152086729 | 224962 | F0 Sr | 10.160 | 6768 | 6801 | 147 | 1.38 | 0.06 | N/A |
| 152808505 | 216641 | F3IV/V ${ }^{\text {a }}$ | 8.280 | 6430 | 6640 | 160 | 0.95 | 0.05 | 1.04 |
| 159834975 | 203006 | A2 CrEuSr | 4.800 | 8790 | 9057 | 218 | 1.48 | 0.06 | 1.53 |
| 167695608 |  | F0p $\mathrm{SrEu}(\mathrm{Cr})^{\text {b }}$ | 11.513 | 7185 | 7460 | 157 | 1.10 | 0.06 | N/A |
| 167751145 | 52280 | A0 Sr Cr Eu | 9.816 | 7621 | 7772 | 177 | 1.30 | 0.06 | 1.42 |
| 182909257 | 6783 | B8 Si | 7.960 | N/A | 11511 | 197 | 1.86 | 0.06 | 2.00 |
| 183802606 | 8700 | A0 SiCrFe | 9.569 | 8754 | 8982 | 179 | 1.77 | 0.06 | N/A |
| 183802904 | 8783 | A2 SrEuCr | 7.800 | 8648 | 8346 | 181 | 1.78 | 0.06 | 1.89 |
| 206461701 | 209364 | A5 Sr Eu Cr | 10.028 | 7144 | 6962 | 150 | 1.42 | 0.06 | N/A |
| 206648435 | 215983 | A0 Sr Eu Cr | 9.660 | 8184 | 8395 | 169 | 1.24 | 0.06 | 1.33 |
| 207208753 | 20505 | A2 CrSr | 9.816 | 9310 | 8418 | 169 | 1.45 | 0.06 | N/A |
| 211404370 | 203932 | A5 Sr Eu | 8.812 | 7544 | 7366 | 157 | 0.92 | 0.20 | N/A |
| 219340705 | 222349 | F Sr | 9.217 | 6222 | 6231 | 153 | 0.39 | 0.05 | 0.45 |
| 231844926 | 10840 | B9 Si | 6.790 | N/A | 10471 | 185 | 1.90 | 0.05 | 1.98 |
| 232066526 | 11090 | A Sr | 10.782 | 8750 | 8587 | 171 | 1.32 | 0.06 | N/A |
| 234346165 | 16504 | B8 Si | 9.050 | 9480 | 10315 | 175 | 2.14 | 0.06 | N/A |
| 235007556 | 221006 | A0 Si | 5.660 | N/A | 13863 | 237 | 2.24 | 0.05 | 2.30 |
| 237336864 | 218495 | A2 Eu Sr | 9.378 | 8283 | 7941 | 162 | 0.92 | 0.05 | 1.04 |
| 262613883 | 63728 | A0 Eu Cr Si | 9.356 | 9359 | 8847 | 176 | 1.39 | 0.06 | 1.57 |
| 262956098 | 3988 | A 0 CrEuSr | 8.340 | 7691 | 7646 | 166 | 1.67 | 0.06 | 1.82 |
| 266905315 | 225234 | A3 Sr | 8.872 | 8343 | 7993 | 163 | 1.00 | 0.05 | 1.13 |
| 270304671 | 209605 | F0 Sr Eu | 9.576 | 8044 | 7943 | 163 | 1.24 | 0.06 | 1.33 |
| 271503787 | 2883 | F4 Sr | 9.380 | 6359 | 6423 | 149 | 0.64 | 0.06 | 0.75 |
| 277688819 | 208217 | A 0 SrEuCr | 7.200 | 8368 | 8318 | 172 | 1.13 | 0.06 | 1.21 |
| 277748932 | 208759 | A0 SrEuCr | 9.984 | 8955 | 8308 | 165 | 1.34 | 0.06 | N/A |
| 278804454 | 212385 | A3 Sr Eu Cr | 6.850 | 8672 | 8806 | 175 | 1.50 | 0.06 | 1.56 |
| 279091054 | 50861 | A3 Sr Eu | 9.746 | 7372 | 7493 | 164 | 1.20 | 0.06 | 1.32 |
| 279573219 | 54118 | A 0 Si | 5.140 | N/A | 10848 | 182 | 1.88 | 0.06 | 2.00 |
| 280051011 | 18610 | A2 CrEuSr | 8.170 | 8628 | 8371 | 178 | 1.50 | 0.05 | 1.64 |
| 281668790 | 3980 | A7 Sr Eu Cr | 5.720 | 8747 | 7448 | 159 | 1.26 | 0.05 | 1.32 |
| 304096024 | 11346 | A2 Sr Eu Cr | 9.898 | 8098 | 7339 | 153 | 1.69 | 0.06 | N/A |
| 306573201 | 66195 | A0 Sr Eu Cr | 8.660 | N/A | 8892 | 194 | 1.39 | 0.06 | 1.56 |
| 306893839 | 68561 | B9 Si | 8.020 | N/A | 11290 | 207 | 2.34 | 0.06 | N/A |
| 307031171 | 69578 | F6III Sr ${ }^{\text {c }}$ | 9.560 | 6720 | 5905 | 148 | 1.18 | 0.06 | 1.35 |
| 307288162 | 71006 | A0 Si | 9.243 | N/A | 12403 | 213 | 2.34 | 0.07 | N/A |
| 307642246 | 72634 | A 0 Eu Cr Sr | 7.280 | 8947 | 9348 | 191 | 2.13 | 0.11 | 2.31 |
| 308085294 | 74388 | B8 Si | 6.990 | N/A | 12165 | 223 | 2.48 | 0.06 | 2.66 |
| 309148260 | 69862 | A2 Sr Eu Cr | 10.112 | 8134 | 7485 | 156 | 1.45 | 0.06 | N/A |
| 316913639 | 222638 | A0 Sr Eu Cr | 8.650 | 9714 | 9961 | 195 | 1.51 | 0.06 | 1.64 |

Table 1 - continued

| TIC | HD | Spectral Type | V | $\begin{gathered} T_{\text {eff }}^{\text {TIC }} \\ (\mathrm{K}) \end{gathered}$ | $\begin{gathered} T_{\mathrm{eff}}^{\mathrm{RF}} \\ (\mathrm{~K}) \end{gathered}$ | $\Delta T_{\mathrm{eff}}^{\mathrm{IRF}}$ <br> (K) | $\log \left(L / L_{\odot}\right)^{\text {noAv }}$ | $\Delta \log \left(L / L_{\odot}\right)^{\text {noAv }}$ | $\log \left(L / L_{\odot}\right)^{\text {Av }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 327597288 | 206653 | B9 Si | 7.210 | N/A | 11384 | 205 | 2.00 | 0.06 | 2.13 |
| 336731635 | 214985 | A0 Si | 11.103 | 9439 | 11631 | 199 | 2.18 | 0.18 | N/A |
| 348717688 | 19918 | A5 SrEuCr | 9.350 | 8074 | 7484 | 159 | 1.10 | 0.05 | 1.22 |
| 348898673 | 54399 | A2 Sr CrEu | 9.725 | 7506 | 7466 | 156 | 1.70 | 0.06 | N/A |
| 349409844 | 58448 | B8 Si | 6.920 | N/A | 11536 | 204 | 1.77 | 0.05 | 1.88 |
| 350146296 | 63087 | A7IV ${ }^{\text {c }}$ | 9.408 | 7690 | 7450 | 160 | 0.82 | 0.05 | N/A |
| 350146577 | 63204 | B9 Si | 8.307 | 9737 | 11389 | 200 | 1.86 | 0.05 | 2.03 |
| 350272314 | 222925 | F8 Sr Eu | 9.020 | 5579 | 5723 | 136 | 1.63 | 0.05 | N/A |
| 350519062 | 38719 | A 0 CrSrEu | 7.510 | 8937 | 8967 | 186 | 1.62 | 0.05 | 1.75 |
| 358467700 | 65712 | A 0 SiCr | 9.340 | 8768 | 8941 | 178 | 1.46 | 0.05 | N/A |
| 364424408 | 30374 | A 0 Sr Eu Cr | 10.052 | 7608 | 8420 | 167 | 1.50 | 0.06 | N/A |
| 372913684 | 65987 | B9 Si Sr | 7.620 | N/A | 10796 | 186 | 2.33 | 0.06 | 2.49 |
| 382512330 | 64369 | B9 Si | 8.839 | 9042 | 9701 | 214 | 1.71 | 0.06 | N/A |
| 389531041 | 206193 | F5 Sr | 9.920 | 6513 | 6495 | 152 | 1.16 | 0.06 | 1.25 |
| 389922504 | 40277 | A1 Sr CrEu | 8.350 | N/A | 9123 | 188 | 1.22 | 0.05 | 1.36 |
| 391927730 | 56981 | F0 Sr | 9.589 | 6984 | 6817 | 155 | 0.78 | 0.05 | 0.95 |
| 392761412 | 207259 | A 0 Eu Sr Cr | 8.830 | 8036 | 7901 | 163 | 1.33 | 0.06 | 1.47 |
| 394045029 | 211333 | F6IV Sr ${ }^{\text {c }}$ | 8.550 | 6292 | 6349 | 141 | 1.14 | 0.05 | 1.25 |
| 394124612 | 218994 | A3 Sr | 8.570 | 7451 | 7368 | 154 | 1.42 | 0.06 | 1.52 |
| 407661867 | 37584 | A3V ${ }^{\text {c }}$ | 8.330 | 9363 | 8750 | 180 | 1.10 | 0.05 | N/A |
| 410451752 | 66318 | A 0 Eu Cr Sr | 9.652 | 9057 | 8849 | 177 | 1.48 | 0.06 | 1.63 |
| 431380369 | 20880 | A3 Sr Eu Cr | 7.953 | 8242 | 7884 | 167 | 1.40 | 0.06 | 1.51 |
| 434103853 | 221531 | F5 Sr | 8.340 | 6513 | 6436 | 156 | 0.64 | 0.05 | 0.70 |

Notes. ${ }^{\text {a }}$ Spectral type from (Houk 1978).
${ }^{\mathrm{b}}$ Spectral type from Holdsworth et al. (2014a).
${ }^{\mathrm{c}}$ Spectral type from Houk \& Cowley (1975).
inspection of the light curve and the computation of a Fourier transform were conducted. If modulation was identified, the signal and any harmonics were fitted by non-linear least-squares to the light curve to optimize the solution of the rotation frequency. In the cases where a harmonic has a higher amplitude, we used its frequency to determine the period as the frequency precision is higher for a higher amplitude signal. Phase-folded light curves were produced for every determined rotation period to ensure by visual inspection that the correct frequency (i.e. not a harmonic) was chosen.

As a by-product of this process, we also identified low-frequency variability which we assumed to be either g-mode $\gamma$ Doradus (hereafter, $\gamma$ Dor) pulsations, or low overtone p-mode pulsations as seen in $\delta$ Scuti (hereafter, $\delta$ Sct) stars. We made a note of these stars, but did not perform an in-depth analysis.

Once any low-frequency information had been extracted from the light curve, we iteratively pre-whitened the data to remove the rotation signals and low-frequency instrumental artefacts in the range $0-0.12 \mathrm{mHz}\left(0-10 \mathrm{~d}^{-1}\right)$. This was done on a star-by-star basis; the amplitude limit of the pre-whitening was determined by the noise level in the high-frequency range where rapid oscillations have been seen in other stars ( $0.7-3.6 \mathrm{mHz}$ ).

Subsequently, an amplitude spectrum was calculated to the Nyquist frequency of the data in the search for high-frequency pulsations. If variability was detected, the mode frequency was fitted with linear least-squares (where the frequency is fixed and the amplitude and phases are derived to minimize the residuals) and non-linear least-squares (where all three parameters are free) to optimize the frequency, amplitude, and phase of the fit to the data. If the star was found to be multiperiodic, these fits were performed simultaneously on all frequencies. In the cases where variability was not detected, we took the limit of the non-detection as either four times the error of the highest noise peak in the data, or the
top of the Fourier 'grass' (the approximate background peaks of the amplitude spectrum that resemble mown grass), whichever was found to be greater to be conservative.

As mentioned above, a number of additional teams analysed the sample of stars under study (typically three per star for the pulsational variability, and typically five per star for the rotational variability). Different analysis tools were used by these teams, including Period04 (Lenz \& Breger 2005), the CLEANest (Foster 1995), and Phase Dispersion Minimization (PDM) algorithms (Stellingwerf 1978) as implemented in the Peranso light curve and period analysis software (Paunzen \& Vanmunster 2016), ${ }^{3}$ the harmonic-function fitting program LCfit (Sódor 2012), and the SigSpec code (Reegen 2007). The spread in the rotation periods derived by the different teams, as measured by the standard deviations listed in Table 2, likely results not only from the different tools applied in the data analyses, but also from differences in the pre-processing of the light curve, including the filtering of outliers and bad data sections, and in the normalization of the light curves. In this respect, we note that the reference team normalized each stellar light curve to zero by removing the mean magnitude of the entire sector. Some of the other teams normalized each light curve by the maximum or minimum of the light curve, and others still, by the median of the raw electron counts.

## 3 RESULTS

A summary of the rotational and pulsational variability results obtained for the 83 stars in our sample is presented in Table 2. In the column 'Variability' we identify whether a star is found to be a variable and, when that is the case, the type(s) of variability

[^2]

Figure 1. HR diagram showing the position of the 83 stars in our sample. The thick dotted line indicates the zero-age main sequence and the continuous non-straight lines mark the evolutionary sequences for masses between 1.0 and $3.5 \mathrm{M}_{\odot}$ (from Marques, Monteiro \& Fernandes 2008, grid B). The thick, blue, continuous straight lines indicate the theoretical instability strip from Cunha (2002) and the orange-dashed lines enclosing the shaded area indicate the region where the 61 roAp stars known prior to the TESS launch were found. This region was established by adopting the effective temperatures from Joshi et al. (2016) for all stars, except TIC 363716787 , for which we adopted the value from the TIC catalogue, as the authors did not provide one, and by computing the roAp stars' luminosities from the data sources considered for the stars in the TESS sample, without considering extinction. The numbered red squares show the position of the five new roAp stars discovered in the TESS data: (1) TIC 12968953, (2) TIC 41259805, (3) TIC 152808505, (4) TIC 350146296, and (5) TIC 431380369; the numbered orange circles show the seven previously known roAp stars observed in sectors 1 and 2: (1) TIC 69855370, (2) TIC 139191168, (3) TIC 167695608, (4) TIC 211404370, (5) TIC 237336864, (6) TIC 348717688, and (7) TIC 394124612; and the black circles show the remaining stars in the sample.
presented. When the star was not previously known to exhibit a given type of variability, the variability type is prefixed by the word 'new'. Likewise, if the star was known to exhibit rotational variability, but we find evidence that the rotation period published in the literature is incorrect, we write 'new rot per' in that column. For new $\delta$ Sct and/or $\gamma$ Dor variables we further use the term 'susp.' to indicate that these are suspected variables of these types. This is to remind the reader that no detailed analysis of the low-frequency variability was performed in this work, as mentioned in Section 2, thus we cannot be certain that the variability is only due to pulsation.
As the TESS pixels are large ( 20.25 arcsec ), there is a relatively high possibility of contamination from nearby sources. This is summarized by the contamination ratio for each star as provided by the TIC. For the 83 stars we study here, the contamination ratio is below 0.1 for all but one star (TIC 410451752). This gives us confidence that the variability we report is for the target star in question, and not associated with a contaminating source. In addition to checking the contamination ratio, we searched the literature for discussion on stellar binarity or multiplicity. For most stars reported as new rotational or roAp pulsational variables,
there is no mention in the literature of multiplicity. The case of TIC 410451752, as well as cases where multiplicity may be a source of confusion, is discussed, on a star-by-star basis, in Sections 3.1.1, 4.3, and 5.7.

### 3.1 Rotational variability

We have identified 27 new rotational variables among the 83 targets and found five known rotational variables to have previously misidentified rotation periods. Of these, in three cases the published values correspond to a harmonic of the true rotation frequency. The phase-folded light curves for the five stars mentioned above are shown in Fig. 2. The double-wave nature of the light curves from TIC 307642246 , TIC 336731635 , and TIC 348898673 explains why these stars were previously identified to have half of the true rotation period. For TIC 309148260 and TIC 394124612 the reasons why the published values are so different from the ones determined now are unclear.
In addition to the rotation periods derived by the reference team and associated formal uncertainties, we provide in Table 2 the

Table 2. Variability properties of the 83 stars analysed in this work. Columns show, from left to right: (1) TIC identification number; (2) Henry Draper Catalogue identification number: (3) variability type; here the word 'new' is used to indicate stars in which the property under consideration was first discovered or measured in this work. For new $\delta$ Sct and $\gamma$ Dor variables we use 'susp.' to indicate the stars are suspected to be variables of the indicated type; (4) published rotation period, if available; (5) rotation period determined in this work; (6) formal uncertainty in the rotation period; (7) standard deviation computed from the set of rotation periods derived by the different teams (see the text for details); (8) pulsation amplitude limit for stars in which pulsational variability has not been detected; (9) references for known rotational variables; 'new rot var' means new rotational variable - all of these appear to be $\alpha^{2} \mathrm{CVn}$ stars; 'new rot per' means new rotation period.

| TIC | HD | Variability type | $P_{\text {rot }}(\text { lit })$ <br> (d) | $P_{\text {rot }}$ <br> (d) | $\Delta P_{\text {rot }}$ <br> (d) | SDV <br> (d) | Pulsation limit ( $\mu \mathrm{mag}$ ) | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12359289 | 225119 | rot var | 2.9 | 3.06395 | 0.00041 | 0.0030 | 19 | 1,2 |
| 12393823 | 225264 | new rot var |  | 1.42353 | 0.00023 | 0.00016 | 20 |  |
| 12968953 | 217704 | new roAp |  |  |  |  |  |  |
| 24693528 | 14944 | susp. new $\delta$ Sct / $\gamma$ Dor |  |  |  |  |  |  |
| 31870361 | 22488 | susp. new $\delta$ Sct / $\gamma$ Dor |  |  |  |  |  |  |
| 32035258 | 24188 | $\alpha^{2} \mathrm{CVn}$ | 2.2301 | 2.23047 | 0.00004 | 0.0013 | 7 | 3,17 |
| 38586082 | 27463 | $\alpha^{2} \mathrm{CVn}$; susp. new $\delta$ Sct | $2.833 \pm 0.010$ | 2.8349 | 0.0001 | 0.0030 |  | 18 |
| 38586127 | 27472 |  |  |  |  |  | 30 |  |
| 41259805 | 43226 | new roAp; new rot var |  | 1.71441 | 0.00011 | 0.00038 |  |  |
| 52368859 | 10081 | $\alpha^{2} \mathrm{CVn}$ | $1.57032 \pm 0.00003$ | 1.57056 | 0.00006 | 0.0023 | 40 | 5 |
| 69855370 | 213637 | roAp |  |  |  |  |  |  |
| 89545031 | 223640 | $\alpha^{2} \mathrm{CVn}$ | 3.73524 | 3.72251 | 0.00097 | 0.0047 | 30 | 4 |
| 92705248 | 200623 | $\alpha^{2} \mathrm{CVn}$ | $2.18 \pm 0.01$ | 2.1577 | 0.0002 | 0.0021 | 30 | 4,9 |
| 115150623 | 201018 | new rot var |  | 1.50048 | 0.00005 | 0.00050 | 24 |  |
| 116881415 | 3135 | susp. new $\delta$ Sct / $\gamma$ Dor |  |  |  |  |  |  |
| 118114352 | 3772 | susp. rot variable ${ }^{\text {a }}$ |  |  |  |  | 30 |  |
| 129636548 | 203585 | new rot var |  | 3.11016 | 0.00056 | 0.0052 | 8 |  |
| 139191168 | 217522 | roAp |  |  |  |  |  |  |
| 141028198 | 35361 | new rot var |  | 6.3035 | 0.0009 | 0.013 | 30 |  |
| 141610473 | 41613 | new rot var |  | 4.0954 | 0.0004 | 0.0029 | 23 |  |
| 144276313 | 221760 | $\alpha^{2} \mathrm{CVn}$; susp. new $\delta$ Sct / $\gamma$ Dor | 12.5 |  |  |  |  | 4,2 |
| 152086729 | 224962 | susp. new $\delta$ Sct / $\gamma$ Dor |  |  |  |  |  |  |
| 152808505 | 216641 | new roAp star |  | 1.876660* | 0.00895 |  |  |  |
| 159834975 | 203006 | $\alpha^{2} \mathrm{CVn}$ | 2.12204 | 2.12230 | 0.00009 | 0.0025 | 10 | 17 |
| 167695608 |  | roAp |  |  |  |  |  |  |
| 167751145 | 52280 |  |  |  |  |  | 42 |  |
| 182909257 | 6783 | new rot var |  | 3.14108 | 0.00082 | 0.0044 | 18 |  |
| 183802606 | 8700 | new rot var |  | 2.27015 | 0.00017 | 0.0022 | 25 |  |
| 183802904 | 8783 | $\alpha^{2} \mathrm{CVn}$ | $19.396 \pm 0.05$ | 19.408 | 0.017 | 0.04 | 14 | 6 |
| 206461701 | 209364 |  |  |  |  |  | 36 |  |
| 206648435 | 215983 | new rot var |  | 5.1094 | 0.0022 | 0.018 | 42 |  |
| 207208753 | 20505 | $\alpha^{2} \mathrm{CVn}$ | $2.04401 \pm 0.00005$ | 2.04334 | 0.00019 | 0.0012 | 40 | 6 |
| 211404370 | 203932 | roAp; new rot var |  | 6.442 | 0.012 | 0.083 |  |  |
| 219340705 | 222349 | new rot var |  | 5.129 | 0.036 | 0.0064 | 16 |  |
| 231844926 | 10840 | $\alpha^{2} \mathrm{CV}$ | 2.09784 | 2.0971 | 0.0001 | 0.0012 | 8 | 17 |
| 232066526 | 11090 | new rot var |  | 2.91982 | 0.00016 | 0.0082 | 46 |  |
| 234346165 | 16504 | new rot var |  | 3.3040 | 0.0003 | 0.0091 | 19 |  |
| 235007556 | 221006 | $\alpha^{2} \mathrm{CVn}$ | $2.3148 \pm 0.0004$ | 2.31206 | 0.00036 | 0.0022 | 18 | 4,11 |
| 237336864 | 218495 | roAp; new rot var |  | 4.2006 | 0.0001 | 0.0037 |  |  |
| 262613883 | 63728 | $\alpha^{2} \mathrm{CVn}$ | $1.83993 \pm 0.00004$ | 1.84015 | 0.00017 | 0.00075 | 33 | 5 |
| 262956098 | 3988 |  |  |  |  |  | 15 |  |
| 266905315 | 225234 |  |  |  |  |  | 24 |  |
| 270304671 | 209605 | $\alpha^{2} \mathrm{CVn}$ | $7.8132 \pm 0.0007$ | 7.8896 | 0.0050 | 0.061 | 38 | 6 |
| 271503787 | 2883 | new rot var |  | 6.056 | 0.013 | 0.024 | 18 |  |
| 277688819 | 208217 | $\alpha^{2} \mathrm{CVn}$; noAp | $8.44475 \pm 0.00011$ | 8.3200 | 0.0084 | 0.057 | 13 | 4,7 |
| 277748932 | 208759 | new rot var |  | 4.4501 | 0.0019 | 0.0036 | 43 |  |
| 278804454 | 212385 | $\alpha^{2} \mathrm{CVn}$ | $2.48 \pm 0.04$ | 2.5062 | 0.0002 | 0.0027 | 14 | 4,12 |
| 279091054 | 50861 |  |  |  |  |  | 30 |  |
| 279573219 | 54118 | $\alpha^{2} \mathrm{CVn}$ | 3.27533 | 3.2724 | 0.0010 | 0.00089 | 8 | 17 |
| 280051011 | 18610 |  |  |  |  |  | 15 |  |
| 281668790 | 3980 | $\alpha^{2} \mathrm{CVn}$; noAp | $3.9516 \pm 0.0003$ | 3.9517 | 0.0001 | 0.00054 | 6 | 4,13 |
| 304096024 | 11346 | new rot var |  | 7.116 | 0.006 | 0.097 | 38 |  |
| 306573201 | 66195 | new rot var |  | 4.88938 | 0.00063 | 0.0057 | 17 |  |
| 306893839 | 68561 | $\alpha^{2} \mathrm{CVn}$ | 4.2334 | 4.23415 | 0.00016 | 0.0017 | 18 | 3,17 |
| 307031171 | 69578 |  |  |  |  |  | 19 |  |
| 307288162 | 71006 | new rot var |  | 1.52073 | 0.00026 | 0.000051 | 40 |  |
| 307642246 | 72634 | $\alpha^{2} \mathrm{CVn}$; new rot per | $0.93062 \pm 0.00001$ | 1.8607 | 0.0002 | 0.00083 | 12 | 6 |
| 308085294 | 74388 | new rot var |  | 4.3063 | 0.0019 | 0.0051 | 11 |  |

Table 2 - continued

| TIC | HD | Variability type | $P_{\text {rot }}(\text { lit })$ <br> (d) | $P_{\text {rot }}$ <br> (d) | $\Delta P_{\text {rot }}$ <br> (d) | SDV <br> (d) | Pulsation limit ( $\mu \mathrm{mag}$ ) | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 309148260 | 69862 | $\alpha^{2} \mathrm{CVn}$; new rot per | $0.518885 \pm 0.000003$ | 13.3519 | 0.0107 | 0.25 | 48 | 6 |
| 316913639 | 222638 | new rot var |  | 2.34691 | 0.00026 | 0.0021 | 18 |  |
| 327597288 | 206653 | $\alpha^{2} \mathrm{CVn}$ | $1.788 \pm 0.005$ | 1.786898 | 0.000058 | 0.00094 | 13 | 4,14 |
| 336731635 | 214985 | $\alpha^{2} \mathrm{CV}$ n; new rot per | $1.3851 \pm 0.0001$ | 2.77342 | 0.00219 | 0.0019 | 70 | 8 |
| 348717688 | 19918 | roAp |  |  |  |  |  |  |
| 348898673 | 54399 | $\alpha^{2} \mathrm{CVn}$; new rot per | $2.50142 \pm 0.00008$ | 4.9910 | 0.0011 | 0.0060 | 25 | 6 |
| 349409844 | 58448 | $\alpha^{2} \mathrm{CVn}$ | $0.831 \pm 0.003$ | 0.83088 | 0.00005 | 0.00017 | 10 | 4,15 |
| 350146296 | 63087 | new roAp star |  | 2.66121 | 0.00029 | 0.0012 |  |  |
| 350146577 | 63204 | $\alpha^{2} \mathrm{CVn}$ | $1.83817 \pm 0.00002$ | 1.83764 | 0.00004 | 0.00036 | 20 | 5 |
| 350272314 | 222925 |  |  |  |  |  | 20 |  |
| 350519062 | 38719 | rot var | 4.02107 | 4.0237 | 0.0004 | 0.0034 | 9 | 10 |
| 358467700 | 65712 | $\alpha^{2} \mathrm{CVn}$ | 1.9457 | 1.94639 | 0.00054 | 0.00047 | 55 | 4 |
| 364424408 | 30374 | $\alpha^{2} \mathrm{CVn}$ | $1.55631 \pm 0.00003$ | 1.55682 | 0.00014 | 0.00059 | 50 | 6 |
| 372913684 | 65987 | $\alpha^{2} \mathrm{CVn}$ | $1.44962 \pm 0.00018$ | 1.45610 | 0.00015 | 0.00033 | 15 | 4,16 |
| 382512330 | 64369 | $\alpha^{2} \mathrm{CVn}$ | $0.89113 \pm 0.00001$ | 0.8912 | 0.0001 | 0.00012 | 25 | 5 |
| 389531041 | 206193 | roAp candidate ${ }^{\text {b }}$; new rot var |  | 6.030 | 0.022 | 0.041 |  |  |
| 389922504 | 40277 | new rot var |  | 0.849585 | 0.000008 | 0.00035 | 14 |  |
| 391927730 | 56981 | new rot var |  | 3.7843 | 0.0018 | 0.0021 | 22 |  |
| 392761412 | 207259 | $\alpha^{2} \mathrm{CVn}$ | $2.16 \pm 0.01$ | 2.1557 | 0.0002 | 0.0020 | 23 | 4,9 |
| 394045029 | 211333 |  |  |  |  |  | 17 |  |
| 394124612 | 218994 | roAp; new rot per | 1.09058 | 5.855 | 0.008 | 0.031 |  | 10 |
| 407661867 | 37584 | susp. rot variable ${ }^{\text {a }}$, roAp candidate |  |  |  |  |  |  |
| 410451752 | 66318 | new rot var |  | 0.77688 | 0.00052 | 0.00021 | 57 |  |
| 431380369 | 20880 | new roAp; new rot var |  | 5.2434 | 0.0026 | 0.042 |  |  |
| 434103853 | 221531 | new rot var |  | 3.2584 | 0.0066 | 0.0023 | 15 |  |

Notes. ${ }^{\text {a }}$ The star shows two low-frequency peaks, but it is unclear whether either of them is a rotation signal (see the text for details).
${ }^{\mathrm{b}}$ The formal significance of the pulsation detection is $4.9 \sigma$, thus marginal.
${ }^{\mathrm{c}}$ Rotation period inferred from the analysis of pulsations (see the text for details).
Ref: 1: Renson \& Manfroid (2009); 2: Catalano \& Renson (1998); 3: Paunzen \& Maitzen (1998); 4: Samus et al. (2017); 5: Bernhard et al. (2015);
6: Hümmerich, Paunzen \& Bernhard (2016); 7: Manfroid \& Mathys (1997) ; 8: Bernhard, Hümmerich \& Paunzen (2015); 9: Renson \& Catalano (2001); 10: Oelkers et al. (2018); 11: Manfroid \& Mathys (1985); 12: Renson (1978); 13: Maitzen, Weiss \& Wood (1980); 14: Hensberge et al. (1977); 15: Manfroid \& Renson (1983); 16: North (1984); 17: ESA (1997); and 18: Manfroid \& Renson (1981).
standard deviations on the rotation periods derived by all teams analysing each star. These correspond to the spread in results arising from the application of different analysis techniques. For comparison, the literature values for the rotation periods are also provided, when available.
Besides the five stars mentioned above, for which our rotation periods are strikingly different from the published results, there are a few other cases in which we found rotation periods differing significantly from those in the literature. To identify the most extreme cases, we added in quadrature the formal error and standard deviation of our rotation periods, and adopted that quantity, $\sigma_{\text {rot }}$, as a conservative measurement of the uncertainty on our results. We found that for another two stars the absolute difference between the literature value, taking into account the published uncertainties, and the value we obtained is larger than $10 \sigma_{\text {rot }}$. For those stars, namely TIC 12359289 and TIC 372913684 , we established that the rotation period derived from TESS data is significantly different from the previously published values. Moreover, while this work was under review, an independent study of magnetic O, B, and A stars (DavidUraz et al. 2019) has reported rotation periods derived from the same TESS data used in this work for 12 stars in our sample. While for nine stars the agreement is clear (with eight rotation periods agreeing within the formal errors and one within $\sigma_{\text {rot }}$ ), for the remaining three stars the rotation periods reported by David-Uraz et al. (2019) are somewhat different. In particular, for TIC 89545031 the period in that study, $P=3.7349 \pm 0.0005 \mathrm{~d}$, differs by $2.6 \sigma_{\text {rot }}$ from the period
derived in our work; for TIC 237336864 the same authors find $P=$ $4.183 \pm 0.006 \mathrm{~d}$, which differs from the period we derived by 4.8 $\sigma_{\text {rot }}$; and for TIC 279573219 their period, of $3.2759 \pm 0.0002 \mathrm{~d}$ differs from ours by $2.6 \sigma_{\text {rot }}$. In fact, these three stars have some strong low-frequency instrumental systematics, which are either not removed by the TESS science pipeline, or introduced by the TESS reduction pipeline. It is, thus, more likely that different approaches to the analysis of their light curves lead to differences in the derived periods. While the differences found are not as significant as in the cases discussed earlier in this section, they do call for caution when analysing TESS PDC SAP fluxes when strong low-frequency instrumental noise is present.
Finally, we note, for future comparison, that for TIC 118114352 and TIC 407661867 rotation periods were derived, but considered insecure, hence were not included in the table. We provide provisional values here for future reference. For TIC 118114352, the amplitude spectrum shows a peak consistent with a rotation period of 1.388 d. However, there is a second peak close to it, corresponding to a period of 1.093 d . If one is the rotation signal, then the other may be due to a pulsation mode or contamination from another star. The second star is TIC 407661867. For this star there is a peak in the amplitude spectrum corresponding to a period of 0.562 d but with other similar amplitude peaks in the vicinity and the period is short for an Ap star. The field for this star is crowded (despite the target star being the brightest), so the source of the variability is also questionable.


Figure 2. The phase-folded light curves for the five stars where we provide a new determination of the rotation period. Top left: TIC 307642246, top right: TIC 309148260, middle left: TIC 336731635 , middle right: TIC 348898673 , and bottom left: TIC 394124612 . The data have been binned $50: 1$ for clarity.

### 3.1.1 Contamination and multiplicity

We found TIC 410451752 to be a new rotationally variable star with a period of $0.77688 \pm 0.00052 \mathrm{~d}$, which we measured from the rotation frequency and its harmonic. This star has a contamination ratio of 0.8 . To ensure that we attributed this signal to the correct star, we investigated the surrounding bright objects that may have fallen in the photometric aperture. We found that one, TIC 410451777 (HD 66295), is classified as B8/9p Si by Hartoog (1976). The rotation period is known to be 2.45 d (Netopil et al. 2017), which is significantly different from what we find for TIC 410451752. The other stars in the region have no rotation period reported in the literature. We are thus confident that we attributed the rotation signal to the correct star, although we cannot say for certain.

Of the other stars for which we find new rotational variability, there are six stars with discussion in the literature pertaining to multiplicity. TIC 152808505 and TIC 394124612 are also pulsational variables, hence we discuss their cases in dedicated sections (Sections 4.3 and 5.7, respectively) below.

TIC 12393823: This star is a known spectroscopic binary with a period of $5.400945 \pm 0.000040 \mathrm{~d}$ and an eccentricity of $e$ $=0.267 \pm 0.008$ (González \& Levato 2009). This period is not associated with the rotation period we derive here ( $P=$ $1.42353 \pm 0.00023 \mathrm{~d}$ ). There is no mention of the companion to

TIC 12393823 in the literature, indicating a less luminous object. We therefore assume that the derived rotation period is for the primary component of TIC 12393823 , i.e. the A1 SiSr star.

TIC 115150623: This star is reported in the literature as an sdB +F binary (Kilkenny et al. 2015). However, this is cast into doubt when considering the Gaia parallax of $4.03 \pm 0.08$ mas. In the absence of extinction, this provides an absolute magnitude of about +1.7 , which corresponds to a mid-A star. Since the composite spectrum of an $\mathrm{sdB}+\mathrm{F}$ binary shows both signatures of the hot star and cool star, a combined apparent magnitude would be between $V=3$ and $V=5$. Finally, TIC 115150623 was classified as Ap CrEuSr by Houk (1982), which is consistent with the rotation period of $P=$ $1.50048 \pm 0.00005 \mathrm{~d}$ we found.

TIC 129636548: The multiplicity of this star has been reported many times. The Washington Double Star Catalogue (Mason et al. 2001) provides information on three components in the system, with two being of similar magnitude ( $\mathrm{AB} ; V=6.24$ and $V=6.88$ ) and a fainter third ( $\mathrm{C} ; V=10.30$ ). The AB pair has been observed to have a variable separation ( 0.8 arcsec in 1879 and 0.3 arcsec in 2014), with the AC separation being about 80 arcsec over the same period. Given the pixel size of TESS, and the photometric aperture, it is expected that all three components will be contributing to the recorded flux. Malkov et al. (2012) provide an orbital period of 464 yr for the two bright components. There is only one spectral
type provided for the entire system: A0 Si. Therefore, we cannot say which of the three stars the determined rotation period of 3.11 d is intrinsic to, but assume it is either the A or B component; given the classification and magnitude difference, component C is likely a G star, which is not expected to have the stable spots that we observed.
TIC 434103853: North \& Duquennoy (1991) first noted this star to be an SB1 system. Makarov \& Kaplan (2005) noted that the star is an astrometric binary, for which Pourbaix \& Jorissen (2000) gave a period of 1416 d and an eccentricity of 0.165 . There is no discussion of the secondary in the literature, but we estimate here a lower limit on the mass of $0.6 \mathrm{M}_{\odot}$ from the results of Pourbaix \& Jorissen (2000). Therefore, depending on the inclination, it is possible that the rotation signal we derive here ( 3.25 d ) belongs to either the primary or secondary component.

### 3.2 Pulsational variability

Five new roAp stars have been identified in our sample, in addition to the seven previously known roAp stars in TESS sectors 1 and 2. Of the five new roAp stars, three were discovered among the list of 80 Ap stars submitted for observation with the TESS 2-min cadence in these sectors. The other two roAp stars, TIC 152808505 and TIC 350146296, and the roAp candidate TIC 407661867, were discovered also among the stars observed in 2-min cadence by TESS, but are A stars not classified as peculiar in the literature. Considering that only the sample of stars previously classified as peculiar was thoroughly searched for roAp-type pulsations in this work, we deduce an incidence of the roAp phenomena of about 4 per cent among the Ap stars (corresponding to 3 in 73 stars).

The roAp stars discovered in TESS data are shown as red squares in Fig. 1. Their global parameters are within those of the 61 roAp stars known prior to the launch of TESS, bracketed by the orangedashed lines seen in the same figure. One of them is located outside the theoretical instability strip, marked by the straight blue lines. Moreover, none is close to the theoretical blue edge.

Among the stars found to exhibit pulsational variability, there are also two classified as 'roAp candidate' and a few classified as suspected $\gamma$ Dor and/or $\delta$ Sct stars. We have made a note of these in the third column of Table 2, but leave the full exploitation of the data on those pulsators to forthcoming publications. In particular, for the roAp candidate TIC 407661867, we found signals of pulsations in the range $0.7-0.74 \mathrm{mHz}$ (periods around 23 min ) which could be $\delta$ Sct in nature, but could also be roAp. However, the star has not been classified as chemically peculiar; its spectral type is A3 V in Houk \& Cowley (1975). McDonald, Zijlstra \& Boyer (2012) obtained $T_{\text {eff }}=8430 \mathrm{~K}$ for this star by comparing model atmospheres to SEDs derived through the combination of data from different sources, and a luminosity of $\log \left(L / L_{\odot}\right)=1.23$, based on the Hipparcos parallax. In this work we find a temperature of $T_{\text {eff }}=$ $8750 \pm 180 \mathrm{~K}$ and a luminosity based on Gaia data of $\log \left(L / L_{\odot}\right)$ $=1.10 \pm 0.05$. The high effective temperature of this star, along with either of the above luminosities, makes it relatively unevolved. For a star with such properties, the expected roAp frequencies are significantly higher than the ones observed (cf. fig. 4 in Cunha 2002), thus putting into question the roAp origin of the pulsations. As the star is in the TESS continuous viewing zone, we will leave the confirmation, or otherwise, of this roAp candidate to a later stage.

In the case of the roAp candidate TIC 389531041 (HD 206193), we detected a pulsation mode with a frequency of $1.21012 \pm 0.00005 \mathrm{mHz}$, in the typical range of the roAp stars. While the signal at this frequency was reported by three independent teams, its significance is only of $4.9 \sigma$, making the identification of
this star as roAp insecure. Its peculiarity is also unclear. It was classified by Renson, Gerbaldi \& Catalano (1991) as F5 Sr, but with a 'peculiarity probability note' of 'doubtful nature'. The effective temperature derived here, $T_{\text {eff }}=6495 \pm 152 \mathrm{~K}$, places the star outside the theoretical instability strip, but there are other known roAp stars with similar effective temperatures. TIC 389531041 was observed during sector 1, and will not be revisited in TESS's primary mission. Thus, unfortunately, TESS data will not allow us to test the roAp nature of this star during the nominal mission.
Finally, for 63 stars in our sample, no pulsational variability was found. For those stars, the 8th column in Table 2 provides the detection limit as defined in Section 2.2. We note, however, that these limits to pulsational variability are in the TESS photometric band, where pulsation amplitudes in roAp stars are significantly smaller than in the $B$ filter most often used in ground-based campaigns. Further discussion on the amplitude comparison between the TESS and $B$ filters is presented in Section 6, based on the analysis of previously known roAp stars.

In the following sections, we provide details of the analysis and results for 14 stars in our sample found to be of particular interest. These consist of the five new roAp stars (Section 4), seven previously known roAp stars (Section 5), and two wellcharacterized noAp stars (Section 7).

## 4 THE NEW TESS ROAP STARS

### 4.1 TIC 12968953

TIC 12968953 (HD 217704) was classified as A7 by Philip \& Stock (1972). Later, Renson et al. (1991) (see also Renson \& Manfroid 2009) identified the peculiar nature of this star, classifying it as A5 Sr. The star was among the targets of the Cape Survey for rapid oscillations in Ap stars (see e.g. Martinez 1993; Martinez \& Kurtz 1991), but no evidence was found for high-overtone pulsations at that time (Martinez \& Kurtz 1994). Its effective temperature of $7880 \pm 160 \mathrm{~K}$, derived in this work, places it on the hot side of the temperature range for the known roAp stars.

We analysed TESS sector 2 data for this star and found no indication of rotational modulation of the light curve. This null detection could be a result of a long rotation period, or a rotational inclination or magnetic obliquity near to zero. However, there is clear evidence of four pulsation modes in this star, thus making it a new roAp star. There is no evidence of multiplets in the amplitude spectrum, consistent with a lack of rotational modulation of the light curve, nor is there amplitude modulation of the modes. In Fig. 3 we show the full amplitude spectrum, a detailed view of the mode frequencies, and the amplitude spectrum after removing the mode frequencies displayed in Table 3. There is no clear separation pattern between the mode frequencies that could represent the large- or small-frequency separations. Unfortunately, the amplitudes in this star are low, so it is unlikely that ground-based $B$ observations will provide more information on the pulsations in TIC 12968953.

### 4.2 TIC 41259805

TIC 41259805 (HD 43226) was classified Ap $\operatorname{Sr}(\mathrm{Eu})$ by Houk \& Cowley (1975) and A0 SrEu by Renson et al. (1991). Its fundamental parameters were obtained by McDonald et al. (2012) by comparing model atmospheres to SEDs inferred from different data sources. They determined $T_{\text {eff }}=8054 \mathrm{~K}$, which is similar to the TIC effective temperature, and $L / L_{\odot}=13.74$, which is between the two values presented in Table 1. The effective temperature determined in this


Figure 3. Top: full amplitude spectrum of TIC 12968953 to almost the Nyquist frequency. Clearly evident are the pulsations around 1.3 mHz . Middle: zoom of the pulsation mode frequencies. Bottom: the amplitude spectrum of the residuals after removing the frequencies shown in Table 3, showing no remaining significant signals.

Table 3. Details of the pulsation modes found in TIC 12968953. The zeropoint for phases is BJD 2458367.81699.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.013$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | ---: | :---: |
|  |  | 0.071 | $1.45 \pm 0.17$ | 5.9 |
| $\nu_{1}$ | $1.25875 \pm 0.00004$ | $0.02 \pm 0.15$ | 6.4 |  |
| $\nu_{2}$ | $1.26961 \pm 0.00003$ | 0.083 | $-0.02 \pm 0.5$ |  |
| $\nu_{3}$ | $1.27047 \pm 0.00005$ | 0.064 | $2.50 \pm 0.21$ | 4.9 |
| $\nu_{4}$ | $1.33782 \pm 0.00003$ | 0.099 | $-0.47 \pm 0.12$ | 8.3 |

work, $T_{\text {eff }}=8290 \pm 170 \mathrm{~K}$, places this star among the hottest roAp stars known.

TIC 41259805 was observed during both sectors 1 and 2 , and will continue to be observed for the rest of cycle 1 apart from sector 9 . There is a clear rotation signal in this star, as shown by the amplitude spectrum in the top panel of Fig. 4, corresponding to a rotation period of $1.71441 \pm 0.00011 \mathrm{~d}$. This is the shortest measured rotation period for an roAp star. The double-wave nature of the light curve, as indicated by the presence of the strong second harmonic in the amplitude spectrum, is an indication that we see both magnetic poles of this star during the rotation cycle (under the assumption that the spots are located at the magnetic poles).


Figure 4. Top: amplitude spectrum at low frequency showing the rotation signal in TIC41259805. The rotation frequency is the highest amplitude peak. Middle: zoom of the pulsation frequencies found in this star. Bottom: the amplitude spectrum of the residuals after removing the frequencies shown in Table 4 showing no remaining significant signals.

Table 4. Details of the pulsation frequencies found in TIC 41259805. The zero-point for phases is BJD 2458353.40492.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.005$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| $v-v_{\text {rot }}$ | $2.30425 \pm 0.00002$ | 0.022 | $-1.06 \pm 0.22$ | 4.4 |
| $v$ | $2.31100 \pm 0.00001$ | 0.052 | $-1.84 \pm 0.09$ | 10.4 |

There are two clear pulsation frequencies (Table 4) in the amplitude spectrum of TIC 41259805, as shown in the middle panel of Fig. 4. These peaks are split by the rotation frequency of the star, implying a triplet with a missing sidelobe at $v+v_{\text {rot }}$. We fitted the assumed triplet with linear least-squares by forcing the sidelobe frequencies to be split by exactly the rotation frequency. The highfrequency sidelobe is present, but not statistically significant at an S/N of 1.8.

### 4.3 TIC 152808505

TIC 152808505 (HD 216641) is one of the three stars in our list not identified as peculiar in the literature. It was classified F3 IV/V by Houk (1978). Through a Bayesian method, using parallaxes and multiband photometry, Bailer-Jones (2011) derived two values


Figure 5. Top: amplitude spectrum of TIC 152808505 to almost the Nyquist frequency. Middle: zoom of the pulsation modes found in this star. Bottom: the amplitude spectrum of the residuals after removing the frequencies shown in Table 5 showing no remaining significant signals.
for its effective temperature, from two different models: $T_{\text {eff }}=$ $6710 \pm 230 \mathrm{~K}$ and $T_{\text {eff }}=6670 \pm 225 \mathrm{~K}$. These values agree with the effective temperature of $6640 \pm 160 \mathrm{~K}$ derived in this work. This effective temperature places this star among the coolest roAp stars known and outside of the theoretical instability strip.

Several sources in the literature cite TIC 152808505 as a multiple system (e.g. Turon et al. 1993; Mason et al. 2001; Fabricius et al. 2002). The two components are separated by about 0.3 arcsec and have Hipparcos magnitudes of 8.92 and 9.41. Therefore, the temperature measurements discussed above have been calculated using the combined flux of both stars.

Observed in TESS sector 1, the data for TIC 152808505 do not show low-frequency light variations that could be attributed to rotation. There are, however, clear signals of pulsation in this star (Fig. 5). We detected five significant peaks in the data, as are shown in Table 5. There are three frequencies that are split by the same frequency that we interpret as a rotationally split triplet. This allows us to infer a rotation period of $1.8766 \pm 0.0090 \mathrm{~d}$. Therefore, we find three independent modes in TIC 152808505. We assume that all three modes are in a single star of this binary pair, however we cannot say which. We also note that the mode amplitudes will be diluted due to the flux from the other component.

As discussed in Section 1, the rotation axis in Ap stars is often inclined with respect to the magnetic axis. In the simple oblique pulsator model, the pulsation axis is assumed to be coincident with the magnetic axis (Kurtz 1982; Shibahashi \& Saio 1985a,b; Dziem-

Table 5. Linear least-squares fit to the pulsations and force fitted sidelobes in TIC 152808505. The zero-point for the fit is BJD 2458340.30085, and has been chosen as such to force the sidelobe phases to be equal.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.004$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | ---: | ---: |
| $\nu_{1}$ | $1.36260 \pm 0.00005$ | 0.019 | $2.16 \pm 0.21$ | 4.8 |
| $\nu_{2}-\nu_{\text {rot }}$ | 1.37976 | 0.033 | $1.09 \pm 0.12$ | 8.3 |
| $\nu_{2}$ | $1.38593 \pm 0.00002$ | 0.055 | $0.35 \pm 0.07$ | 13.8 |
| $\nu_{2}+\nu_{\text {rot }}$ | 1.39210 | 0.020 | $1.09 \pm 0.19$ | 5.0 |
| $\nu_{3}$ | $1.39119 \pm 0.00002$ | 0.041 | $-2.84 \pm 0.10$ | 10.3 |

bowski \& Goode 1985), whereas in the 'improved' oblique pulsator model the pulsation axis generally lies in the plane defined by the rotation and magnetic axes (Bigot \& Dziembowski 2002; Bigot \& Kurtz 2011), and is not necessarily coincident with the magnetic axis. Oblique pulsation results in a changing view of the pulsation axis as the star rotates. Such a configuration allows constraints to be placed on the geometry of the star. These constraints are derived through the analysis of sidelobes to the pulsation mode that are separated by the rotation frequency of the star. For a pure dipole mode, one expects a triplet, and for a pure quadrupole mode, a quintuplet (i.e. a $2 \ell+1$ multiplet).

The triplet here shows unequal sidelobe amplitudes that is a signature of the effect of Coriolis force on the pulsations (e.g. Bigot \& Dziembowski 2002). Under the assumption that the triplet represents a dipole mode, we forced the sidelobes to be equally separated from the pulsation frequency by the assumed rotation frequency, then fitted the triplet (after removing the two other modes from the data) by linear least-squares to test the oblique pulsator model. By choosing the zero-point in time such that the phases of the first sidelobes are equal, we are able to show that the mode is slightly distorted as the central peak in the triplet has a different phase. The results of this test are shown in Table 5.

Furthermore, we are able to provide constraints on the geometry of the pulsation through the relation of Kurtz, Shibahashi \& Goode (1990):
$\tan i \tan \beta=\frac{A_{+1}^{(1)}+A_{-1}^{(1)}}{A_{0}^{(1)}}$,
where $A_{ \pm 1}^{(1)}$ are the dipole sidelobe amplitudes, $A_{0}$ is the amplitude of the central peak, $i$ is the inclination angle, and $\beta$ is the angle of obliquity. This holds true under the assumption of a pure, nondistorted, dipole pulsation ( $\ell=1, m=0$ ), with sidelobes generated from rotation alone.

For TIC 152808505, we measure $\tan i \tan \beta=0.96 \pm 0.12$. Although we cannot separate $i$ or $\beta$, we show the values that satisfy this relation in Fig. 6. The results show that $i+\beta \simeq 90^{\circ}$ implying we only see one pulsation pole.

### 4.4 TIC 350146296

TIC 350146296 (HD 63087) is another star in our sample for which references to chemical peculiarity do not exist in the literature. The only reference for this star is Houk \& Cowley (1975), who classified it as A7IV. The effective temperature derived in this work, $T_{\text {eff }}$ $=7450 \pm 160 \mathrm{~K}$, places it well within the theoretical instability strip. The analysis presented here is based on sectors 1 and 2 data; however, this star is in TESS's continuous viewing zone and will have a complete 13 -sector data set at the end of TESS cycle 1.


Figure 6. Display of the possible $i+\beta$ combinations, for the four stars where the analysis of the multiplets allows us to set constraints on the stellar pulsation geometry. The full lines and coloured regions limited by dashed lines correspond, respectively, to the values and uncertainties of $i+\beta$ for each star. In stars for which $i+\beta \leq 90^{\circ}$ only one pulsation pole is observed. Different colours show the results for different stars. The brown and purple stripes indicate regions of overlap of possible solution for TIC 350146296 and TIC 237336864.

There is clear rotational modulation in this star as demonstrated by the high amplitude harmonic series in the top panel of Fig. 7. We determine the rotation period to be $2.66121 \pm 0.00029 \mathrm{~d}$. The pulsation spectrum is rich. In order of increasing frequency, we find a doublet split by twice the rotation frequency, a singlet, a triplet, a quintuplet, and another triplet, all split by the rotation frequency. The details of the pulsations are shown in Table 6. Further to the rich amplitude spectrum, TIC 350146296 hosts the highest frequency pulsations of any known roAp star ( $3.562 \mathrm{mHz} ; P=4.68 \mathrm{~min}$ ), significantly surpassing those found in HD $134214(2.947 \mathrm{mHz}, P$ $=5.66 \mathrm{~min}$; Kreidl 1985; Gruberbauer et al. 2011).

The pulsations observed in TIC 350146296 may be above the star's acoustic cut-off frequency, $\nu_{\mathrm{ac}}$. The roAp stars with frequencies above the acoustic cut-off frequency are a challenge to theory (Cunha et al. 2013). This is because, while the strong magnetic field provides a natural way to keep the wave energy of such high-frequency pulsations within the star (Sousa \& Cunha 2008), the opacity mechanism is unable to excite them, as discussed in Section 1. We estimate a mass of $1.55 \pm 0.09 \mathrm{M}_{\odot}$ for TIC 350146296, from the mass-luminosity relation published by Eker et al. (2015). Based on that mass and on the effective temperature and luminosity listed in Table 1, we compute the cut-off frequency by scaling from the solar value using $v_{\mathrm{ac}} \propto g / \sqrt{T_{\text {eff }}}$, where $g$ is the surface gravity (e.g. Chaplin \& Miglio 2013). Taking a solar value of


Figure 7. Top: amplitude spectrum at low frequency showing the rotation signal of TIC 350146296 and its harmonics. Middle: zoom of the pulsation modes found in this star. Bottom: the amplitude spectrum of the residuals after removing the frequencies shown in Table 6 showing no remaining significant signals.

Table 6. Details of a linear least squares fit to the pulsation modes found in TIC 350146296. The zero-point for the phases, BJD 2458353.55189, was chosen to force the sidelobes of $\nu_{3}$ to be equal. The frequencies of all sidelobes have been forced to be split from the central component by integer values of the rotation frequency.

| ID | Frequency (mHz) | $\begin{gathered} \text { Amplitude } \\ (\mathrm{mmag}) \\ \pm 0.005 \end{gathered}$ | Phase <br> (rad) | S/N |
| :---: | :---: | :---: | :---: | :---: |
| $\nu_{1}-v_{\text {rot }}$ | $3.398781 \pm 0.000021$ | 0.044 | $2.35 \pm 0.12$ | 8.2 |
| $v_{1}+v_{\text {rot }}$ | $3.407455 \pm 0.000021$ | 0.036 | $2.27 \pm 0.14$ | 6.9 |
| $\nu_{2}$ | $3.442436 \pm 0.000012$ | 0.051 | $-2.10 \pm 0.10$ | 9.5 |
| $\nu_{3}-v_{\text {rot }}$ | 3.479660 | 0.095 | $2.79 \pm 0.06$ | 18.0 |
| $v_{3}$ | $3.484009 \pm 0.000009$ | 0.068 | $2.97 \pm 0.08$ | 12.8 |
| $\nu_{3}+v_{\text {rot }}$ | 3.488359 | 0.074 | $2.79 \pm 0.07$ | 13.9 |
| $\nu_{4}-2 \nu_{\text {rot }}$ | 3.514631 | 0.060 | $1.51 \pm 0.09$ | 11.4 |
| $\nu_{4}-1 v_{\text {rot }}$ | 3.518980 | 0.053 | $1.94 \pm 0.10$ | 9.9 |
| $v_{4}$ | $3.523329 \pm 0.000004$ | 0.159 | $1.44 \pm 0.03$ | 30.0 |
| $\nu_{4}+1 v_{\text {rot }}$ | 3.527678 | 0.062 | $1.39 \pm 0.08$ | 11.8 |
| $\nu_{4}+2 \nu_{\text {rot }}$ | 3.532027 | 0.045 | $1.51 \pm 0.12$ | 8.5 |
| $v_{5}-v_{\text {rot }}$ | 3.558301 | 0.043 | $2.56 \pm 0.12$ | 8.2 |
| $\nu_{5}$ | $3.562650 \pm 0.000020$ | 0.029 | $2.72 \pm 0.18$ | 5.5 |
| $\nu_{5}+v_{\text {rot }}$ | 3.566999 | 0.032 | $2.41 \pm 0.16$ | 6.1 |

Table 7. Details of the splittings between pulsation modes in TIC 350146296.

| IDs | Splitting <br> $(\mu \mathrm{Hz})$ |
| :--- | :---: |
| $\nu_{2}-\nu_{1}$ | $39.318 \pm 0.016$ |
| $\nu_{3}-\nu_{2}$ | $41.573 \pm 0.014$ |
| $\nu_{4}-\nu_{3}$ | $39.320 \pm 0.009$ |
| $\nu_{5}-\nu_{4}$ | $39.321 \pm 0.020$ |

$v_{\mathrm{ac}}^{\odot}$ $=5.106 \mathrm{mHz}$ (Jiménez 2006), we find $v_{\mathrm{ac}}=2.91 \pm 0.79 \mathrm{mHz}$, for TIC 350146296. Unfortunately, the large uncertainties in the star's global parameters prevent us from concluding whether the star is indeed pulsating above the cut-off frequency.

Since the frequencies in this star are so high, there is a nonnegligible suppression of the pulsation amplitude due to the length of the exposures. Calculated using the expression (Murphy 2014)
$\frac{A}{A_{0}}=\operatorname{sinc} \frac{\pi T_{\text {exp }}}{P_{\text {puls }}}$,
where $T_{\text {exp }}$ and $P_{\text {puls }}$ are the exposure time and pulsation period, we find that the intrinsic amplitude $\left(A_{0}\right)$ of the central component of the quintuplet is 0.217 mmag in the TESS filter. Given the non-optimum red filter of TESS, it is possible that this pulsation is detectable from the ground with $B$ observations (cf. Section 6).

With such a rich pulsation spectrum, we are also able to determine the large-frequency separation, $\Delta v$, for this star, defined as the difference in frequency of modes of the same degree and consecutive radial orders. The frequency difference between most of the modes is $39.3 \mu \mathrm{~Hz}$. This spacing may correspond to the large-frequency separation, if the modes are of the same degree, or to half of it, if they are of alternating even and odd degrees. To establish which of these is the most likely option, we consider again the mass estimated above and the global parameters given in Table 1, and scale from the Sun, to derive an estimate of the large-frequency separation for TIC 350146296. Using the scaling relation $\Delta v \propto \sqrt{\langle\rho\rangle}$, where $\langle\rho\rangle$ is the stellar mean density (e.g. Chaplin \& Miglio 2013), and adopting $135 \mu \mathrm{~Hz}$ as the solar large frequency separation (e.g. Stello et al. 2009), we estimate the large frequency separation for this star to be $87 \pm 16 \mu \mathrm{~Hz}$. This value clearly points towards the modes seen in TIC 350146296 as being alternating even and odd degrees.

This remains the case even if extinction is accounted for in the computation of the luminosity. Although no extinction value is provided for this star, we saw from Section 2.1 that the root mean square of the difference between the logarithmic luminosity values derived with and without accounting for extinction is 0.1 . If we were to assume that the logarithmic luminosity of TIC 350146296 is 0.1 larger than the value considered before, we would find a large-frequency separation of $73.5 \mu \mathrm{~Hz}$, still pointing towards the same conclusion. Interestingly, there is one spacing, between $v_{2}$ and $v_{3}$, which is slightly larger at $41.6 \mu \mathrm{~Hz}$. This may indicate that $v_{2}$ and $\nu_{4}$ correspond to modes of different degrees, a possibility that would also naturally explain the difference seen in their multiplet structures. All of the splittings are shown in Table 7.

Now that we have justified the identification of the modes as alternating even and odd degree modes, we suggest the following degree identifications for the multiplets: $v_{1}$ dipole; $v_{2}$ radial, or quadrupole; $v_{3}$ dipole; $v_{4}$ quadrupole and $v_{5}$ dipole. From this, we are able to provide constraints on the geometry of the star by applying the oblique pulsator model to the various multiplets we detect, as described in Section 4.3. For a pure, non-distorted mode,
we expect the phases of each peak in the multiplet to be the same. We find that, in the cases of the dipole triplets, there is good agreement between the phases of all of the peaks in a multiplet. This is also the case for the quadrupole mode $\left(v_{4}\right)$ where there is good agreement between all but the $\nu_{4}-v_{\text {rot }}$ phase.

Returning to the oblique pulsator model and the geometry of the star, as discussed above, we can use the relative amplitudes of the sidelobes and the pulsation peak to see the relationship between $i$ and $\beta$. Applying equation (1) to the two triplets, $\nu_{3}$ and $v_{5}$, in TIC 350146296, we find that $\tan i \tan \beta=2.50 \pm 0.22$ and $2.58 \pm 0.53$, respectively. We have also identified the doublet as the rotational sidelobes of an undetected $v_{1}$, hence a dipole triplet for these frequencies. The undetected frequency $v_{1}$ could plausibly be lost in the noise; it is possible that the dipole modes have different geometries, as was suggested for KIC 10195926 (Kurtz et al. 2011). This result will become clear with more sectors of data for this star, which is in the continuous viewing zone.

Now considering the quintuplet $\left(v_{4}\right)$, the relationship between the amplitudes of the sidelobes of a non-distorted quadrupole mode ( $\ell=2, m=0$ ) is given by Kurtz et al. (1990):
$\tan i \tan \beta=4 \frac{A_{-2}^{(2)}+A_{+2}^{(2)}}{A_{-1}^{(2)}+A_{+1}^{(2)}}$
where $A_{ \pm 1}^{(2)}$ and $A_{ \pm 2}^{(2)}$ are the amplitudes of the first and second sidelobes of the mode. With this relation we find $\tan i \tan \beta=$ $3.91 \pm 0.36$, which differs from the relation derived from the two dipole modes by $3.3 \sigma$ and $2.1 \sigma$, respectively. This difference may be a result of the magnetic field perturbing the different degree modes differently, a result of the broad TESS filter, a combination of these, or something else entirely. This star warrants a detailed study reserved for a later publication when more data are available.

Using the combined results of the dipole triplets, by taking their average $\tan i \tan \beta$ and summing the corresponding errors in quadrature, we calculate the allowed values of $i$ and $\beta$, which satisfy equation (1) and show them in Fig. 6. As we have no information on either $i$ or $\beta$, they cannot be disentangled.

### 4.5 TIC 431380369

TIC 431380369 (HD 20880) was classified as $\mathrm{ApSr}(\mathrm{EuCr})$ by Houk \& Cowley (1975). Martinez (1993) measured Strömgren and H $\beta$ indices for this star: $V=7.957 ; b-y=0.097 ; m_{1}=0.212 ; c_{1}=$ $1.005 ; \beta=2.870$, from which the parameters $\delta m_{1}=-0.009$ and $\delta c_{1}=0.095$ can be derived; neither of these indices is indicative of an Ap star. The $\mathrm{H} \beta$ index indicates an equivalent spectral type near mid-A (see Crawford 1975, 1979; Moon \& Dworetsky 1985, for calibration relations for the Strömgren and $\mathrm{H} \beta$ indices for F and A stars, respectively). The relatively high temperature of $7880 \pm 170 \mathrm{~K}$ derived in this work may explain why the Strömgren indices are essentially normal.

Observed in sector 2, the TESS data for TIC 431380369 show this star to be a rotationally modulated variable with a period of $5.2434 \pm 0.0026 \mathrm{~d}$. The light curve is significantly affected by instrumental artefacts during the last 5 days of sector 2 , which may lead one to conclude that the period is double to what we present, but the pulsation analysis discussed below provides us with confidence in our determination.

There are three frequencies that can be extracted with confidence in this star, as shown in Fig. 8 and Table 8. Analysis of these peaks shows that two are independent modes, with the third being a rotational sidelobe. The separation of the two modes, $\sim 45 \mu \mathrm{~Hz}$,


Figure 8. Top: amplitude spectrum at low frequency showing the rotation signal of TIC431380369. Middle: zoom of the pulsation modes found in this star. Bottom: the amplitude spectrum of the residuals after removing the significant frequencies given in Table 8 showing no remaining significant signals.

Table 8. Linear least-squares fit to the pulsations and force-fitted sidelobes in TIC 431380369. The zero-point for phases is BJD 2458370.481478, and has been chosen such that the phases of the sidelobes of the highest amplitude mode are equal.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.004$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\nu_{1}-v_{\text {rot }}$ | 0.81366 | 0.003 | $0.13 \pm 1.34$ | 0.8 |
| $\nu_{1}$ | $0.81587 \pm 0.00004$ | 0.018 | $-1.18 \pm 0.21$ | 4.5 |
| $\nu_{1}+v_{\text {rot }}$ | 0.81808 | 0.017 | $-0.77 \pm 0.24$ | 4.3 |
| $\nu_{2}-v_{\text {rot }}$ | 0.85829 | 0.011 | $-3.10 \pm 0.36$ | 2.8 |
| $\nu_{2}$ | $0.86050 \pm 0.00003$ | 0.034 | $-1.24 \pm 0.12$ | 8.5 |
| $\nu_{2}+v_{\text {rot }}$ | 0.86271 | 0.024 | $-3.10 \pm 0.16$ | 6.0 |

could be the large separation. In fact, an analysis similar to that described in Section 4.4 gives for this star $\Delta v=44 \pm 8 \mu \mathrm{~Hz}$, when extinction is neglected.

Given that one of the modes shows a rotational sidelobe $\left(v_{2}\right)$, we attempt to extract further sidelobes that are not clearly seen in Fig. 8 . To do this, we force fitted sidelobes at $\pm \nu_{\text {rot }}$ to the two modes with linear least-squares. We find that only the positive sidelobes are significant at the $4 \sigma$ level, as shown in Table 8.

TIC 431380369 will be observed in two more sectors. However, these are well spaced in time, which will result in a complex window
function, potentially complicating the extraction of the sidelobes and any further modes.

## 5 THE PREVIOUSLY KNOWN ROAP STARS

### 5.1 TIC 69855370

TIC 69855370 (HD 213637) was classified as A (pEuSrCr) by Houk \& Smith-Moore (1988). Martinez (1993) measured Strömgren and $\mathrm{H} \beta$ indices for this star: $V=9.611 ; b-y=0.298 ; m_{1}=0.206 ; c_{1}$ $=0.411 ; \beta=2.670$, from which the parameters $\delta m_{1}=-0.035$ and $\delta c_{1}=-0.031$ can be derived; both of these indices are indicative of an Ap star. The $\mathrm{H} \beta$ index indicates an equivalent spectral type near mid-F, so this is one of the coolest roAp stars. This is confirmed by the effective temperature derived in this work, $T_{\text {eff }}=6430 \pm 150 \mathrm{~K}$. This value is consistent with the effective temperature determined by Kochukhov (2003), based on the analysis of high-resolution spectra from the Ultraviolet and Visual Echelle Spectrograph (UVES) on the ESO Very Large Telescope (VLT), from which the author derived $T_{\text {eff }}=6400 \pm 100 \mathrm{~K}$ from the $\mathrm{H}_{\alpha}$ and $\mathrm{H}_{\beta}$ lines, and $\log g=3.6 \pm 0.2$ from the ionization equilibrium for $\mathrm{Fe}_{\mathrm{I}}$ and $\mathrm{Fe}_{\text {II }}$ lines. The author points out that stratification contributes to the uncertainty in the surface gravity determination. In any case, this star, along with a few others such as HD 101065 (Przybylski's star), sets the lower temperature boundary for the Ap phenomenon, and hence tests our understanding of these stars.

Mathys (2003) first measured the mean magnetic field modulus of TIC 69855370 to be 5.2 kG . Kochukhov (2003) also derived a mean magnetic field modulus of $B_{s}=5.5 \pm 0.1 \mathrm{kG}$ from Zeeman splitting in the Fe II 6146.26-Å line, and Elkin, Kurtz \& Mathys (2015) found $B_{s}=5.56 \pm 0.15 \mathrm{kG}$ from the partially resolved components of the Fe II $6146.26 \AA$ line. Clearly, TIC 69855370 is a strongly magnetic Ap star.

Rapid pulsations were discovered in TIC 69855370 by Martinez et al. (1998), who found two pulsation mode frequencies, $v_{1}=$ $1.41089 \pm 0.00011 \mathrm{mHz}$ and $\nu_{2}=1.45235 \pm 0.00006 \mathrm{mHz},{ }^{4}$ although with some uncertainty because of the daily aliases in their data set. Elkin et al. (2015) obtained 2.1 h of high-time resolution, high spectral resolution observations of TIC 69855370 with the UVES spectrograph on the ESO VLT and reported on the pulsational radial velocity variations at different atmospheric heights. Their 2-h observations were not long enough to resolve the two frequencies found by Martinez et al. (1998).

TIC 69855370 was, and will only be, observed during TESS sector 2. We detect no indication of rotation in this star, suggesting one of three options: a long rotation period, an unfavourable alignment (with $i$ or $\beta$ close to zero), or the absence of significant spots. The latter would be surprising, given the strong magnetic field. Kochukhov (2003) measured a projected rotational velocity $v_{\mathrm{e}} \sin i$ $=3.5 \pm 0.5 \mathrm{~km} \mathrm{~s}^{-1}$, and suggested a rotation period of 25 d . With this in mind, we favour an unfortunate geometry for the explanation of the lack of a rotation signal.

Clearly present in the TESS data are the two known pulsation mode frequencies (Fig. 9). We fitted these frequencies with nonlinear least-squares and show the results in Table $9 . \nu_{2}$ is in agreement with Martinez et al. (1998); $v_{1}$ differs from their value by $11.57 \mu \mathrm{~Hz}\left(1 \mathrm{~d}^{-1}\right)$; as they were concerned about daily aliases in

[^3]

Figure 9. Top: full amplitude spectrum of TIC 69855370 to almost the Nyquist frequency. Middle: zoom of the pulsation modes found in this star. Bottom: the amplitude spectrum of the residuals after removing the frequencies given in Table 9 showing no significant frequencies remaining.

Table 9. Details of the pulsation modes found in TIC 69855370. The zeropoint for phases is BJD 2458367.81716.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.007$ | Phase <br> $(\mathrm{rad})$ | S/N |
| :--- | :---: | :---: | :---: | :---: |
| $v_{1}$ | $1.422447 \pm 0.000014$ | 0.120 | $1.96 \pm 0.06$ | 17.1 |
| $\nu_{2}$ | $1.452371 \pm 0.000010$ | 0.172 | $1.03 \pm 0.04$ | 24.6 |

their data set, this resolves the issue; the frequencies in Table 9 do not suffer from aliasing, thanks to the high duty cycle of TESS.

We therefore derive the separation between the two pulsation frequencies of $v_{2}-v_{1}=29.924 \pm 0.017 \mu \mathrm{~Hz}$. This is plausibly the large separation, or half of that. Following the scaling applied in Section 4.4, we find for this star $\Delta v=68 \pm 13 \mu \mathrm{~Hz}$, when extinction is neglected, which is consistent with the observed separation corresponding to half of the large-frequency separation, so with the degree of the modes being of alternating parity.

### 5.2 TIC 139191168

TIC 139191168 (HD 217522) was classified as an Ap (Si)Cr star by Houk (1978) with the remark 'may be Eu rather than Si'. The Eu suggests a cooler star than Si. Martinez (1993) measured Strömgren and $\mathrm{H} \beta$ indices for this star: $V=7.525 ; b-y=0.289 ; m_{1}=0.227$;
$c_{1}=0.484 ; \beta=2.691$, from which the parameters $\delta m_{1}=-0.056$ and $\delta c_{1}=-0.015$ can be derived; both of these indices are indicative of an Ap star. The $\mathrm{H} \beta$ index indicates an equivalent spectral type near mid-F, so this is among the coolest roAp stars. Previously, Gelbmann (1998) obtained $T_{\text {eff }}=6750 \mathrm{~K}$ as part of the detailed abundance analysis of this star. Kochukhov, Bagnulo \& Barklem (2002) derived $T_{\text {eff }}=6850 \mathrm{~K}$ from the Balmer line profiles. We derive an effective temperature of $6890 \pm 150 \mathrm{~K}$, which is consistent with those.

The mean longitudinal magnetic field of TIC 139191168 was measured to be $-400 \pm 120$ G by Mathys \& Hubrig (1997). Later, Hubrig et al. (2002) measured a mean quadratic field strength of $2000 \pm 400 \mathrm{G}$, which is consistent with the mean field modulus upper limit of 1.5 kG provided by Ryabchikova, Kochukhov \& Bagnulo (2008).

Kurtz (1983) discovered pulsations with periods around 13.72 min in this star with observations made on 17 nights in 1982 through a Johnson $B$ filter. Kreidl et al. (1991) conducted a multisite observing campaign on TIC 139191168 in 1989 from four southern hemisphere observatories. They concluded that the pulsation mode amplitudes have short growth and decay times for the pulsations with frequencies near 1.2 mHz . Indeed, the highest peak near 1.2 mHz has a greater amplitude in 1989 than in 1982. They also discovered new pulsations with frequencies near 2 mHz that were completely absent from the 1982 observations, supporting the argument for rapid growth and decay for the pulsations in this star.

Medupe et al. (2015) obtained further $B$ observations of TIC 139191168 in 2008, which also showed the presence of the 2.0 mHz peaks. Importantly, they also obtained high time resolution, high spectral resolution spectra with the ESO VLT UVES spectrograph. Their study of individual lines shows the presence of both the 1.2 and 2.0 mHz peaks with amplitudes that were very sensitive to the atmospheric height of the line formation layer for individual elements and ions, largely of rare earth elements. The $\mathrm{H}_{\alpha}$ measurements barely showed the presence of the 2.0 mHz peak, whereas, for example, that frequency had a higher amplitude than the 1.2 mHz peak for the Nd II $5293 \AA$ line.

Previous observations of TIC 139191168 showed no signs of rotational light variability due to surface spots (van Heerden, Martinez \& Kilkenny 2012; Medupe et al. 2015), nor is there spectral line variability observed in this star. The longitudinal field measurements reported in the catalogue by Bagnulo et al. (2015), based on the data collected with the FOcal Reducer and low dispersion Spectrograph 1 (FORS1), indicate variability on the time scale of a few years. The rotational broadening corresponding to $v \sin i=2.5 \mathrm{~km} \mathrm{~s}^{-1}$ was derived by Ryabchikova et al. (2008). A 'mild constraint' on the $v \sin i$ of $3 \mathrm{~km} \mathrm{~s}^{-1}$ was given by Medupe et al. (2015). Consistent with these ground-based observations, we are unable to detect a signal of rotation in the TESS sector 1 data.

The TESS data do clearly show the pulsational variability in TIC 139191168 , though only around 1.2 mHz (Fig. 10). There is no signal at 2 mHz where pulsations have previously been found. This is not surprising, given that the spectroscopic studies show that the $2-\mathrm{mHz}$ frequencies are more visible higher in the atmosphere, and the TESS red filter samples more deeply in the atmosphere because of the lower opacity in the red.

As with the ground-based data, the TESS data show significant evidence of frequency and/or amplitude modulation, or short mode lifetimes. After the removal of four frequencies in TIC 139191168 (Table 10), there is still excess power in the amplitude spectrum (as shown by the bottom panel of Fig. 10). The two higher frequency peaks listed in Table 10 are separated by $\sim 9 \mu \mathrm{~Hz}$, which could


Figure 10. Top: full amplitude spectrum of TIC 139191168 to almost the Nyquist frequency. Middle: zoom of the pulsation modes found in this star. Bottom: the amplitude spectrum of the residuals after removing the frequencies shown in Table 10. There is still excess power in the spectrum, indicating further, unresolved modes or frequency modulation in this star.

Table 10. Details of the pulsation modes found in TIC 139191168. The zero-point for phases is BJD 2458339.24058.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.003$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | ---: | ---: |
|  |  |  |  |  |
| $\nu_{1}$ | $1.200877 \pm 0.000023$ | 0.031 | $-1.73 \pm 0.10$ | 10.3 |
| $\nu_{2}$ | $1.201677 \pm 0.000026$ | 0.029 | $-2.11 \pm 0.11$ | 9.7 |
| $\nu_{3}$ | $1.205792 \pm 0.000021$ | 0.032 | $0.67 \pm 0.09$ | 10.7 |
| $\nu_{4}$ | $1.215135 \pm 0.000021$ | 0.031 | $-1.59 \pm 0.10$ | 10.3 |

be the small-frequency separation, i.e. the separation between the almost degenerate frequencies of modes of radial orders differing by 1 and degrees differing by 2 (e.g. Cunha et al. 2007), although since earlier studies of this star have suggested growth and decay of mode amplitude, that could also be consistent here.

Although we do not detect the pulsation at 2.0 mHz (probably a result of the red filter), we agree with Medupe et al. (2015) that the importance of TIC 139191168 lies in the large frequency difference between the 1.2 mHz and 2.0 mHz pulsations, since there must be a large number of non-excited modes between those. Unfortunately, we will not be able to solve this problem with the TESS data. No further observations of this star are planned.


Figure 11. Top: amplitude spectrum of TIC 167695608 to nearly the Nyquist frequency. The roAp pulsations are clear at about 1.55 mHz . Middle: detailed view of the pulsation modes in this star. Bottom: amplitude spectrum of the residuals after removing all of the frequencies shown in Table 11. There are potentially further modes present in this star, however the current data are inconclusive.

### 5.3 TIC 167695608

TIC 167695608 (TYC 8912-1407-1) was found to be an roAp star by Holdsworth et al. (2014a) through a survey of A stars in the SuperWASP archive. In the broad-band WASP data, the pulsation was detected at a frequency of 1.53 mHz with an amplitude of 0.79 mmag. The star was spectroscopically classified in the same work as $\mathrm{F} 0 \mathrm{p} \mathrm{SrEu}(\mathrm{Cr})$. As this was not previously known to be a chemically peculiar star, no Strömgren nor $\mathrm{H} \beta$ indices exist in the literature. The star is relatively faint among the known roAp stars ( $V$ $=11.513$ ), and is a recent addition to the class, which explains the lack of previous study in the literature. The temperature derived in this work, $T_{\text {eff }}=7460 \pm 160 \mathrm{~K}$ (Table 1), is consistent with that derived from Balmer line fitting of low-resolution spectra (Holdsworth et al. 2014a). Of the known roAp stars, TIC 167695608 will have the most complete data set from TESS - it will be observed in 12 of the 13 sectors, being missed only in sector 5 . Therefore, the analysis presented here will be greatly improved by the end of TESS's cycle 1.

There is no clear signal of rotation in TIC 167695608, which is consistent with the longer time-base observations from SuperWASP. The middle panel of Fig. 11 shows a detailed view of the pulsation modes after a highpass filter has been applied. The dominant mode, at 1.53 mHz , is already known, but additional, lower amplitude modes have been revealed by these TESS data. Furthermore, there

Table 11. Details of the pulsation modes found in TIC 167695608. The zero-point for phases is BJD 2458381.51320.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.022$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | ---: | ---: |
| $\nu_{1}$ | $1.531950 \pm 0.000008$ | 0.294 | $1.62 \pm 0.14$ | 13.4 |
| $\nu_{2}$ | $1.554816 \pm 0.000015$ | 0.164 | $-2.023 \pm 0.26$ | 7.5 |
| $\nu_{3}$ | $1.564918 \pm 0.000022$ | 0.107 | $3.10 \pm 0.40$ | 4.9 |

may be additional modes present in this star. For the modes we are confident of, we fit them by non-linear least-squares and show the results in Table 11.

The frequencies found at $\nu_{1}$ and $\nu_{2}$ in this star are separated by $22.9 \mu \mathrm{~Hz}$, which could represent half of the large-frequency separation. The difference between $\nu_{2}$ and $\nu_{3}$ could be the small separation. However, as there are many more data to come for this star, we will not claim that here.

### 5.4 TIC 211404370

TIC 211404370 (HD 203932) was classified as Ap SrEu by Houk (1982). Martinez (1993) measured Strömgren and $\mathrm{H} \beta$ indices for this star: $V=8.820 ; b-y=0.175 ; m_{1}=0.196 ; c_{1}=0.742$; $\beta=2.694$, from which the parameters $\delta m_{1}=0.004$ and $\delta c_{1}=$ -0.020 . The $\mathrm{H} \beta$ index indicates an equivalent spectral type near mid-F, so this is one of the coolest roAp stars. The TIC temperature and gravity, $T_{\text {eff }}=7500 \mathrm{~K}, \log g=4.1$, suggest an equivalent spectral type around F0. Gelbmann et al. (1997) performed an abundance analysis on TIC 211404370 and showed it to be an Ap star with abundances similar to $\alpha$ Cir. They derived $T_{\text {eff }}=$ $7540 \pm 100 \mathrm{~K}$ and $\log g=4.30 \pm 0.15$, putting the star close to the zero-age main sequence. Their metallicity, $[\mathrm{M} / \mathrm{H}]=0.0 \pm 0.1$, is consistent with the Strömgren parameters. Here we derive an effective temperature of $7370 \pm 160 \mathrm{~K}$, even lower than the previous value, albeit consistent given the errors. Hubrig et al. (2004) derived a longitudinal magnetic field strength of $\left\langle B_{z}\right\rangle=-267 \mathrm{G}$ from FORS 1 data for TIC 211404370 and later Ryabchikova et al. (2008) have set a limit of 1 kG to the star's magnetic field modulus.

TIC 211404370 was discovered to be an roAp star by Kurtz (1984). It was studied further photometrically by Kurtz (1988), who found it to be multiperiodic, with pulsation mode frequencies in the range of $2.8-2.9 \mathrm{mHz}(P=5.9 \mathrm{~min})$, making this, at the time, the shortest known period for an roAp star. However, later multisite observations by Martinez, Kurtz \& Heller (1990) found only the dominant pulsation frequency, leading them to suggest that the other frequencies found by Kurtz (1988) were possibly transient.

TIC 211404370 was observed during sector 1 of TESS's primary mission. The observations reveal the star to be an $\alpha^{2} \mathrm{CVn}$ variable, with a rotation period of $6.442 \pm 0.012 \mathrm{~d}$. This is the first measurement of the rotation period of this star. The top panel of Fig. 12 shows the low-frequency amplitude spectrum of the TESS light curve. Clearly visible is the rotation signal, with some harmonics present. Also mixed into the stellar signal are some instrumental artefacts that are evidenced by the broad power at low frequency and deviations from a smooth curve in the phase-folded light curve at phase 0.55 .

We detected two pulsation modes, with a third frequency being a rotationally split sidelobe. The frequencies are given in Table 12. An inspection of the $\nu_{2}$ peak in Fig. 12 gives an indication of a second sidelobe to this mode at $\nu_{2}+\nu_{\text {rot }}$. To investigate this further, and


Figure 12. Top: low-frequency amplitude spectrum of TIC 211404370. The dominant peak suggests a rotation period of about 6.4 d . There are also harmonics and instrumental artefacts present. Second: phase-folded light curve on the determined rotation period. The single wave nature suggests that only one magnetic pole is seen. Third: amplitude spectrum showing the pulsation modes in the star. Bottom: amplitude spectrum of the residuals after removing the three frequencies listed in Table 12.

Table 12. A linear least-squares fit to the presumed triplet at $v_{2}$ in TIC 211404370. The frequencies are split by exactly the rotation frequency, and the zero-point in time is chosen so the sidelobe phases are equal. The zero-point is BJD 2458341.53111.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.006$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | :---: | ---: |
| $\nu_{1}$ | $2.698436 \pm 0.000046$ | 0.030 | $-0.89 \pm 0.20$ | 5.0 |
| $\nu_{2}-v_{\text {rot }}$ | 2.802956 | 0.029 | $-0.75 \pm 0.21$ | 4.8 |
| $\nu_{2}$ | $2.804756 \pm 0.000016$ | 0.082 | $-2.84 \pm 0.07$ | 13.7 |
| $\nu_{2}+v_{\text {rot }}$ | 2.806556 | 0.016 | $-0.75 \pm 0.38$ | 2.7 |

to apply the oblique pulsator model to TIC 211404370, we fitted a triplet with sidelobes split by exactly the rotation frequency to the data by linear least squares. The results are shown in Table 12.

The $\nu_{2}+\nu_{\text {rot }}$ sidelobe has a significance of $2.7 \sigma$. With the sidelobe present, we can apply the dipole form of the oblique pulsator model, as shown in equation (1). We find that $\tan i \tan \beta=$ $0.54 \pm 0.11$. Although we cannot disentangle $i$ and $\beta$, we illustrate their relationship in Fig. 6. We find that $i+\beta \leq 90^{\circ}$, which is consistent with the observed single-wave light curve shown Fig. 12, i.e. only one pulsation pole and one magnetic pole are seen.

Previous ground-based observations of TIC 211404370 have often reported that it pulsates in multiple frequencies, but with the presence of different modes at different epochs. In the works by both Kurtz (1988) and Martinez et al. (1990), the authors report separations between modes of about $35 \mu \mathrm{~Hz}$, or multiples thereof. Here, the difference between $\nu_{1}$ and $\nu_{2}$ is $106.3 \mu \mathrm{~Hz}$, or about $3 \times 35 \mu \mathrm{~Hz}$. Therefore, the TESS observations of TIC 211404370 are consistent with previous studies of this star, showing transient frequencies with separations of $35 \mu \mathrm{~Hz}$, which could represent the large-frequency separation, or half of it. From the parameters in Table 1, we estimate $\Delta v=73 \pm 32 \mu \mathrm{~Hz}$, the large uncertainty resulting from the uncertainty in the Gaia DR2 parallax for this star, $\pi=5.2 \pm 0.9$ mas. Despite that, the value obtained from the scaling indicates that $35 \mu \mathrm{~Hz}$ most likely represents half of the large-frequency separation in this star.

### 5.5 TIC 237336864

TIC 237336864 (HD 218495) was classified as Ap EuSr by Houk \& Cowley (1975). Martinez (1993) measured Strömgren and H $\beta$ indices for this star: $V=9.356 ; b-y=0.114 ; m_{1}=0.252 ; c_{1}=$ $0.812 ; \beta=2.870$, from which the parameters $\delta m_{1}=-0.049$ and $\delta c_{1}=-0.098$ can be derived; both of these indices are indicative of a strong Ap star. The $\mathrm{H} \beta$ index indicates an equivalent spectral type near mid-A. The effective temperature derived here, $7950 \pm 160 \mathrm{~K}$, is consistent with that. A longitudinal magnetic field strength of $\left\langle B_{z}\right\rangle=-912 \mathrm{G}$ has been detected in this star by Hubrig et al. (2004) based on FORS1 data.

Rapid pulsations were discovered in TIC 237336864 by Martinez \& Kurtz (1990), who found an oscillation at 2.24 mHz . No further photometric observations of this star have been published since that time.

TESS observed TIC 237336864 only during sector 1 . The top panel of Fig. 13 shows the amplitude spectrum of these data. There is a significant peak that corresponds to a period of 2.1 d . However, this is a case where the harmonic of the rotation has a much more significant signal than the true rotation frequency. To prove we have determined the correct period (as shown in Table 1), we present a phase-folded light curve in the bottom panel of Fig. 13, which shows the double-wave nature of the rotational modulation. We extracted the rotation frequency and processed an 8-harmonic series using both linear and non-linear least-squares to derive the rotation frequency, $v_{\text {rot }}=0.00275536 \pm 0.00000007 \mathrm{mHz}$, which gives a rotation period of $P_{\text {rot }}=4.2006 \pm 0.0001 \mathrm{~d}$.

As outlined earlier, we pre-whitened the rotational variations and some low-frequency artefacts to create a highpass filtered data set to study the pulsation frequencies. This did not affect those pulsation frequencies, and provides a better estimate of errors in least-squares fitting by removing the variance at low frequency. The top panel of Fig. 14 shows an amplitude spectrum of the pulsation modes in TIC 237336864; this is a much richer spectrum than previously reported from ground-based observations. The plot


Figure 13. Top: low-frequency amplitude spectrum of TIC 237336864. The dominant peak suggests a rotation period of about 2.1 d , however we find this to be the first harmonic of the rotation frequency. Bottom: phase-folded light curve, folded on a period of $4.2006 \pm 0.0001 \mathrm{~d}$. The unequal maxima and minima show this to be correct period. The light curve has been binned 50:1.


Figure 14. Top: amplitude spectrum of TIC 237336864 showing the pulsations detected in this star. Bottom: amplitude spectrum of the residuals after removing all of the frequencies shown in Table 13. There are no remaining peaks with significant amplitude.
shows a singlet, a doublet, a quintuplet, and a triplet of frequencies. The multiplets are all split by either $v_{\text {rot }}$ or $2 v_{\text {rot }}$. We optimized the frequencies by non-linear least-squares fitting, and then forced the multiplets to be equally split by $\nu_{\text {rot }}$ or $2 \nu_{\text {rot }}$. Table 13 shows the derived frequencies. We found that this fitted the data as well as the non-linear least-squares determined frequencies. The bottom panel of Fig. 14 shows the amplitude spectrum of the residuals with

Table 13. A linear least-squares fit of the frequencies extracted for TIC 237336864. The zero-point for the phases has been chosen to be BJD 2458338.92557 to set the phases of the doublet to be equal.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.008$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | :---: | ---: |
| $\nu_{1}$ | $2.098269 \pm 0.000032$ | 0.056 | $1.23 \pm 0.14$ | 7.1 |
| $\nu_{2}-v_{\text {rot }}$ | 2.217975 | 0.099 | $0.76 \pm 0.08$ | 12.5 |
| $\nu_{2}+v_{\text {rot }}$ | 2.223486 | 0.114 | $0.76 \pm 0.07$ | 14.4 |
| $\nu_{3}-2 v_{\text {rot }}$ | 2.240365 | 0.045 | $1.67 \pm 0.18$ | 5.7 |
| $\nu_{3}-1 v_{\text {rot }}$ | 2.243121 | 0.090 | $1.89 \pm 0.09$ | 11.4 |
| $\nu_{3}$ | $2.245876 \pm 0.000039$ | 0.046 | $1.22 \pm 0.17$ | 5.9 |
| $\nu_{3}+1 v_{\text {rot }}$ | 2.248631 | 0.104 | $2.01 \pm 0.08$ | 13.1 |
| $\nu_{3}+2 v_{\text {rot }}$ | 2.251387 | 0.058 | $-0.86 \pm 0.14$ | 7.3 |
| $\nu_{4}-2 v_{\text {rot }}$ | 2.255722 | 0.047 | $-2.21 \pm 0.17$ | 5.9 |
| $\nu_{4}$ | $2.261233 \pm 0.000011$ | 0.159 | $-1.98 \pm 0.05$ | 20.1 |
| $\nu_{4}+2 v_{\text {rot }}$ | 2.266744 | 0.048 | $-1.65 \pm 0.17$ | 6.1 |

only noise with highest peaks less than $40 \mu \mathrm{mag}$. The purpose of force fitting the multiplets is to test the phase relationships of the multiplet members, which is informative about the mode geometry within the oblique pulsator model.

Table 13 shows those results, where we have chosen the zeropoint in time to give equal phases for the doublet. We note that the phases of the two highest amplitude components of the quintuplet and the outer components of the triplet are equal within $1 \sigma$. This is what is expected for oblique pulsation, but the different amplitudes for the multiplets suggest either different degrees, $\ell$, or different pulsation axes or both (see e.g. Bigot \& Kurtz 2011; Kurtz et al. 2011). A more detailed examination of this is deferred to a future paper.

Looking at the quintuplet, $v_{3}$, we were able to constrain the geometry of the star with the oblique pulsator model under equation (3). We obtained $\tan i \tan \beta=2.11 \pm 0.26$. We graphically show the relationship in Fig. 6, and see that $i+\beta$ is always $>90^{\circ}$ implying we see both pulsation poles, consistent with the double-wave nature of the light curve seen in Fig. 13.

We now look at the mode frequency separation, assuming that each multiplet arises from oblique pulsation, so that the central frequency is the actual pulsation frequency. That gives $v_{1}=$ $2.098269 \mathrm{mHz} ; v_{2}=2.220730 \mathrm{mHz}$, where we have taken the average of the two components to obtain the central frequency of an assumed triplet; $v_{3}=2.245876 \mathrm{mHz}$; and $\nu_{4}=2.261233 \mathrm{mHz}$. We then look at the frequency separations for the mode frequencies of these multiplets: $v_{2}-v_{1}=122 \mu \mathrm{~Hz} ; v_{3}-v_{2}=25 \mu \mathrm{~Hz} ; v_{4}-v_{3}$ $=15 \mu \mathrm{~Hz}$. These are plausibly in the range of the large separation, or half or a multiple of that. However, scaling from the Sun with the parameters provided in Table 1, we estimate $\Delta v=91 \pm 16 \mu \mathrm{~Hz}$. Further insight clearly requires detailed modelling of this star.

### 5.6 TIC 348717688

TIC 348717688 (HD 19918) was classified as Ap SrCrEu by Houk \& Cowley (1975). Martinez (1993) measured Strömgren and $\mathrm{H} \beta$ indices for this star: $V=9.336 ; b-y=0.169 ; m_{1}=0.216 ; c_{1}=$ $0.822 ; \beta=2.855$, from which the parameters $\delta m_{1}=-0.010$ and $\delta c_{1}$ $=-0.058$ can be derived; both of these indices are indicative of a mild Ap star. The $\mathrm{H} \beta$ index indicates an equivalent spectral type near mid-A. Here we derive a temperature of $T_{\text {eff }}=7480 \pm 160 \mathrm{~K}$, lower than $T_{\text {eff }}=8110 \pm 150 \mathrm{~K}$ derived by Ryabchikova et al. (2007). A mean longitudinal magnetic field strength of $-625 \pm 87 \mathrm{G}$ has
been derived from FORS1 data for this star (Hubrig et al. 2006). A mean field modulus of 1.6 kG was obtained from the analysis of high-resolution spectra by Ryabchikova et al. (2007).

Rapid pulsations were discovered in TIC 348717688 by Martinez \& Kurtz (1991) and studied in more detail by Martinez et al. (1995), who found two pulsation modes separated by either the large separation or half of that, depending on mode identification, in observations obtained in the years 1990, 1991, 1992, and 1994. Martinez et al. (1995) also found a strong harmonic to the principal pulsation frequency.

TIC 348717688 was observed during TESS's sector 1 and will be revisited during sectors 12 and 13. The large gap between the current data set and subsequent observations will introduce a window pattern that may interfere with the pulsation analysis, but with two consecutive sectors, the future data will allow for a more precise analysis than we present here.

The top panel of Fig. 15 shows an amplitude spectrum of the sector 1 data, where the principal pulsation frequency, $v_{7}$ $=1.510057 \pm 0.000002 \mathrm{mHz}$, its harmonic at $2 v_{7}$ and other significant peaks can be seen. Those are clearer in the second panel, which has a higher frequency resolution. The third panel shows the amplitude spectrum after pre-whitening by $v_{7}$, where other pulsation mode frequencies are seen better. The bottom panel shows an amplitude spectrum of the residuals after removing all of the frequencies shown in Table 14.

In total, we extracted nine frequencies from the amplitude spectrum seen in the third panel of Fig. 15. The results are given in Table 14. The principal mode frequency $v_{7}=$ $1.510057 \pm 0.000002 \mathrm{mHz}$ is very close to that found by Martinez et al. (1995), $1.510208 \pm 0.000004 \mathrm{mHz}$. The small difference between these two measurements of $\nu_{7}$ is significant, hence probably indicating some change of frequency between these data sets; this is not uncommon for roAp stars. The second frequency found by Martinez et al. (1995) was at $1.48061 \pm 0.00001 \mathrm{mHz}$ and is between two of the peaks listed in Table 14, hence may be unresolved. This suggests that care is called for in any attempt to model these frequencies.

With a large number of frequencies, we search for repeating frequency separations to find the large and/or small frequency separations. We find that $\nu_{8}-v_{7}=v_{7}-v_{5}=29.8 \mu \mathrm{~Hz}$ and $\nu_{5}-v_{4} \simeq$ $\nu_{4}-\nu_{3} \simeq 40.8 \mu \mathrm{~Hz}$. Both of these values are plausible for the largefrequency separation, or half of it. From the parameters in Table 1, we estimate $\Delta v=59 \pm 10 \mu \mathrm{~Hz}$, thus pointing towards the observed $29.8 \mu \mathrm{~Hz}$ spacing being half of the true large-frequency separation.

Furthermore, the difference between $\nu_{1}$ and $\nu_{2}$, of $5.1 \mu \mathrm{~Hz}$, could be the rotation frequency, or two times the rotation frequency, under the assumption of a triplet with a missing sidelobe, or a triplet with no central component. The derived rotation period would be either 2.27 d or 4.54 d , both of which are feasible. With future sectors 12 and 13 observations, we hope to be able to confirm all of the separations discussed here.

Kurtz, Elkin \& Mathys (2006) obtained 2 h of high time resolution, high spectral resolution observations of TIC 348717688 with the UVES spectrograph on the ESO VLT. They also found two frequencies, 1.510 mHz and 1.383 mHz , in radial velocity variations of lines of PrIII and $\mathrm{H}_{\alpha}$. Of course, with only 2 h time span, their second frequency is not resolved in those spectroscopic data. Ryabchikova et al. (2007) performed a more detailed analysis of the UVES data for this star and nine other roAp stars and discussed the pulsation radial velocity amplitude as a function of atmospheric height. A detailed analysis of the pulsational line profile variability as a function of atmospheric height, using the same UVES data, was


Figure 15. Top: amplitude spectrum of TIC 348717688 to almost the Nyquist frequency. Evident is the principal pulsation mode and its harmonic. Second: zoom of the pulsation modes in this star. Third: the amplitude spectrum after removing the principal mode to show the presence of further, low-amplitude, modes. Note the change in the ordinate scale. Bottom: amplitude spectrum of the residuals after removing all of the frequencies shown in Table 14. There are no remaining peaks with significant amplitude.
presented by Kochukhov et al. (2007). The new results here from the TESS data show the dominance of $\nu_{7}$ to the variations in this star, hence indicate that the spectroscopic results are secure, as they are not likely to be affected by the additional, significantly lower amplitude, pulsation modes.

Kurtz et al. (2006) comment on a relatively small amplitude ratio of $A_{2 \nu_{7}} / A_{\nu_{7}}=0.10$ for $\nu_{7}$ and its harmonic in the spectroscopic data compared to the $B$ photometric data, for which they found a ratio of $A_{2 \nu_{7}} / A_{\nu_{7}}=0.36 .{ }^{5}$ As can be seen in Table 14, $A_{2 \nu_{7}} / A_{\nu_{7}}=0.07$ for

[^4]Table 14. Details of the pulsation mode found in TIC 348717688 . The zero-point for phases is BJD 2458339.23761.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.007$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :--- | :---: | :---: | ---: | ---: |
|  |  |  |  |  |
| $\nu_{1}$ | $1.371648 \pm 0.000029$ | 0.055 | $-0.471 \pm 0.129$ | 7.9 |
| $\nu_{2}$ | $1.376747 \pm 0.000021$ | 0.077 | $2.345 \pm 0.093$ | 11.0 |
| $\nu_{3}$ | $1.398550 \pm 0.000040$ | 0.040 | $2.11 \pm 0.179$ | 5.7 |
| $\nu_{4}$ | $1.439870 \pm 0.000034$ | 0.047 | $1.419 \pm 0.152$ | 6.7 |
| $\nu_{5}$ | $1.480236 \pm 0.000034$ | 0.050 | $2.975 \pm 0.147$ | 7.1 |
| $\nu_{6}$ | $1.480999 \pm 0.000025$ | 0.066 | $0.512 \pm 0.111$ | 9.4 |
| $\nu_{7}$ | $1.510057 \pm 0.000002$ | 1.031 | $-0.090 \pm 0.007$ | 147.3 |
| $\nu_{8}$ | $1.539902 \pm 0.000029$ | 0.055 | $1.219 \pm 0.128$ | 7.9 |
| $2 \nu_{7}$ | $3.020152 \pm 0.000021$ | 0.076 | $2.652 \pm 0.094$ | 10.9 |

the TESS filter data, which is similar to the spectroscopic results. This is not a surprise, since the amplitudes of the pulsation modes and their harmonics in roAp stars are very sensitive to atmospheric height and photometric bandpass, as well as to particular spectral lines or depths in their line profiles, sample different atmospheric heights. There is information here, but it may be difficult to exploit it in modelling the pulsations.

### 5.7 TIC 394124612

TIC 394124612 (HD 218994) was classified with spectral type A3 Sr by Houk \& Cowley (1975). Martinez (1993) measured Strömgren and $\mathrm{H} \beta$ indices for this star: $V=8.565 ; b-y=0.154$; $m_{1}=0.196 ; c_{1}=0.826 ; \beta=2.807$, from which the parameters $\delta m_{1}=0.008$ and $\delta c_{1}=0.032$ were derived, indicative of a normal main sequence A-type star.

The star is part of a visual binary system with a separation of 1.2 arcsec (Renson et al. 1991). At least one of the components of the binary system is a $\delta$ Sct star, according to Kurtz et al. (2008). In the same work, a longitudinal magnetic field strength of $440 \pm 23 \mathrm{G}$ was determined.

TIC 394124612 was observed during the Cape Survey, but not found to pulsate (Martinez \& Kurtz 1994). Nevertheless, high timeresolution spectroscopic observations later revealed pulsational variability in the Nd III and Pr III lines of this star (González et al. 2008), with a frequency of 1.17 mHz (a period of 14.2 min ).

TIC 394124612 was observed by TESS during sector 1 only. The data show a low-frequency signal which we take to be the rotation period of the Ap star (top panel of Fig. 16). Such a strong lowfrequency peak is not expected to be present in a non-peculiar A star. Under this assumption, we determine the rotation period for TIC 394124612 as $5.855 \pm 0.008 \mathrm{~d}$, which is significantly different from the value found in the literature, as discussed in Section 3.1.

As stated above, TIC 394124612 is a visual double star. Given the small separation of the two components, and the large pixel size of TESS, the data contain pulsation signals from both stars. The $\delta$ Sct frequencies are found in the range $0.040-0.515 \mathrm{mHz}$ (3.46-44.54 d ${ }^{-1}$ ), and are not analysed here. Rather, we remove all of these frequencies before we study the variability in the Ap star.

The middle panel of Fig. 16 shows the roAp pulsation signal in TIC 394124612 . Obviously, the peak is not represented by a clean sinc function, which implies frequency/amplitude modulation, or further unresolved modes. We fitted the signal by non-linear leastsquares and show the results in Table 15. The bottom panel of Fig. 16 shows the amplitude spectrum of the residuals after removing the pulsation. The remaining power supports our previous point. We


Figure 16. Top: amplitude spectrum at low-frequency showing the rotation signal of TIC 394124612. Middle: zoom of the pulsation mode found in this star. Bottom: the amplitude spectrum of the residuals after removing the frequency shown in Table 15. There is clearly some remaining signal, but this is not resolved in the 27.88 -d data set.

Table 15. Details of the pulsation mode found in TIC 394124612. The zero-point for phase is BJD 2458339.23972.

| ID | Frequency <br> $(\mathrm{mHz})$ | Amplitude <br> $(\mathrm{mmag})$ <br> $\pm 0.008$ | Phase <br> $(\mathrm{rad})$ | $\mathrm{S} / \mathrm{N}$ |
| :---: | :---: | :---: | :---: | :---: |
| $v_{1}$ | $1.14444 \pm 0.00004$ | 0.123 | $-1.61 \pm 0.16$ | 15.4 |

caution that the frequency we fitted may be perturbed by unresolved modes in the vicinity - a longer time-base is needed to fully resolve this pulsation.

The work by González et al. (2008) suffered from alias effects and the authors exercised caution in their frequency determination. The TESS data however confirm that their frequency determination was correct, i.e. $1.14444 \pm 0.00004 \mathrm{mHz}$.

## 6 MODE AMPLITUDE COMPARISONS

It is well known that the amplitudes of the pulsation modes in the roAp stars change dramatically depending on which photometric bandpass is used to observe them (Medupe \& Kurtz 1998). This is primarily because the photometric variations are dominated by the temperature fluctuations during the pulsation cycle. Since the A stars have peak flux towards the blue, the pulsation amplitude with this
temperature variation drops to the red of the Rayleigh-Jeans tail, simplisitically thinking of the SED as a black-body. In addition, the different filters probe different heights in the atmosphere of the star, where the pulsation amplitude, which has contributions from both acoustic and Alfven components, varies significantly (see e.g. Quitral-Manosalva, Cunha \& Kochukhov 2018). The optimum filters for roAp observations, to maximise the measured pulsation amplitude, are bluewards of about $4400 \AA$, with Johnson $B$ often providing the best signal-to-noise as it samples near to the flux maximum. TESS's broad red filter $(6000-10000 \AA$ ) is weighted towards the Rayleigh-Jeans tail, and is therefore not optimal for the study of roAp stars.

To provide a quantitative measure of the reduction in the pulsation amplitudes due to the TESS filter, we made a comparison of some of the known roAp stars where $B$ data are available. We chose stars that show stable modes, have clearly dominant or well-resolved modes, and which are not known to be rotationally modulated to remove the risk of comparing amplitudes at different rotation phases. Table 16 shows the results of this exercise.

Typically we are seeing a reduction in the amplitudes as seen by TESS of about a factor of 6 . The comparison shows that the factor is different from star to star, thus making the transform from TESS to $B$ amplitudes uncertain for the newly discovered roAp stars. Having these $B$ and TESS amplitudes side by side demonstrates that although amplitudes are reduced, the $\mathrm{S} / \mathrm{N}$ is just as good, or better, in the case of TESS. This is a result of near-continuous, space-based photometry, which are two great advantages for the study of roAp stars.

The reduction factor for TIC 348717688 is implausibly small, however (see Medupe \& Kurtz 1998). We conclude that the amplitude was significantly higher at the time of the TESS observations than it was during the 3 yr of observations by Martinez et al. (1995). Whether this is a change in pulsation amplitude, or a change in aspect for an oblique pulsator with a very long rotation period, is not known. The lack of any rotational photometric variability found so far would be consistent with a very long rotation period (years), and such long periods are known among the Ap stars.

The amplitude reduction in TIC 139191168 is about a factor of 20 compared to the $B$ observations. This is a striking difference. However, we do not include this star in our comparison table as it is multiperiodic.

## 7 THE WELL-CHARACTERIZED NOAP STARS

### 7.1 TIC 277688819

TIC 277688819 (HD 208217) was classified as A0p (pSrEuCr) by Houk \& Cowley (1975). Manfroid \& Renson (1983) and Mathys \& Manfroid (1985) studied the photometric variability of this star in the Strömgren system, finding a rotational period of 8.35 d . Mathys et al. (1997) discovered resolved magnetically split lines in the spectra of TIC 277688819 and deduced that the field strength of this star changes by about $\pm 1 \mathrm{kG}$ about the mean value of $\langle B\rangle=$ 7.8 kG . Using these magnetic measurements and new photometric observations, Manfroid \& Mathys (1997) derived an improved value of the rotational period, $8.44475 \pm 0.00011 \mathrm{~d}$. New mean field modulus, longitudinal field, crossover, and quadratic magnetic field measurements were published for TIC 277688819 by Mathys (2017). He also noted that this star exhibits a long-term radial velocity variation indicative of motion in a binary system but could not determine the orbital period nor identify a contribution of the secondary in the spectra. The star is known to be an

Table 16. Comparison of the mode amplitudes for TESS and ground-based $B$ observations of known roAp stars.

| Star <br> TIC) | Mode | TESS Amplitude (mmag) | $B$ Amplitude (mmag) | $A_{B} / A_{\text {TESS }}$ | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 69855370 | $\nu_{1}$ | $0.172 \pm 0.007$ | $0.96 \pm 0.07$ | $5.58 \pm 0.47$ | Martinez et al. (1998) |
|  | $\nu_{2}$ | $0.120 \pm 0.007$ | $0.50 \pm 0.07$ | $4.17 \pm 0.63$ | Martinez et al. (1998) |
| 167695608 | $\nu_{1}$ | $0.294 \pm 0.022$ | $2.31 \pm 0.15$ | $7.86 \pm 0.78$ | Unpublished data |
| 211404370 | $\nu_{2}$ | $0.083 \pm 0.006$ | $0.64 \pm 0.03$ | $7.71 \pm 0.66$ | Martinez et al. (1990) |
| 348717688 | $\nu_{1}$ | $1.031 \pm 0.007$ | $1.24 \pm 0.04$ | $1.20 \pm 0.04$ | Martinez et al. (1995) |

astrometric binary (Makarov \& Kaplan 2005), but it is unknown if the astrometric companion is the same as the spectroscopic one.

Landstreet \& Mathys (2000) fitted all magnetic field measurements available to them with an axisymmetric low-order multipolar field geometry model. According to the authors, the surface magnetic field geometry of TIC 277688819 is dominated by a 13.1 kG dipole field with $\beta=86^{\circ}$ and $i=15^{\circ}$. On the other hand, Bagnulo et al. (2002) derived a different, quadrupoledominated magnetic field configuration by applying an alternative non-axisymmetric multipolar field parametrization to the same set of magnetic observations.

Hubrig, North \& Mathys (2000) investigated the evolutionary state of a sample of Ap stars, including TIC 277688819. They reported a photometric effective temperature of $7900 \pm 300 \mathrm{~K}$ and obtained $M=2.00 \pm 0.11 \mathrm{M}_{\odot}, \log L / \mathrm{L}_{\odot}=1.38 \pm 0.13$. A similar study of a larger sample of Ap stars by Kochukhov \& Bagnulo (2006) also included TIC 277688819, for which these authors found $T_{\text {eff }}=8000 \pm 200 \mathrm{~K}, M=1.93 \pm 0.10 \mathrm{M}_{\odot}, \log L / \mathrm{L}_{\odot}$ $=1.29 \pm 0.12$. Spectroscopic analysis by Freyhammer et al. (2008) indicated $T_{\text {eff }}=7500-8000 \mathrm{~K}$ from the $\mathrm{H}_{\alpha}$ line. Here we derive $T_{\text {eff }}=8320 \pm 170 \mathrm{~K}$, which is consistent with previous determinations.

Martinez \& Kurtz (1994) reported null results in the search of high-overtone pulsations based on photometric observations of TIC 277688819 on seven different nights. Freyhammer et al. (2008) did not detect rapid oscillations above $\sim 10 \mathrm{~m} \mathrm{~s}^{-1}$ with 2.5 h of timeresolved high-resolution spectroscopic observations with UVES at VLT. An independent search of radial velocity pulsations with the HARPS spectrograph (Kochukhov et al. 2008) also yielded null results. Thus, TIC 277688819 is a well-established noAp star in our sample.

The TESS sector 1 data for TIC 277688819 show low-frequency signals of rotation. The amplitude spectrum showing the rotation signal and the phase-folded light curve are shown in the top two panels of Fig. 17. The bottom panel of Fig. 17 shows the amplitude spectrum of the data set after applying a highpass filter. There are no signs of high-frequency variability in this star, to a limit of $13 \mu \mathrm{mag}$. This limit was estimated from the top of the noise peaks (i.e. the Fourier grass) and four times the error on the highest amplitude noise peak. These TESS data, therefore, support the case that TIC 277688819 is a noAp star.

### 7.2 TIC 281668790

TIC 281668790 (HD 3980) is a bright southern Ap star, classified as F0 ( pSrEuCr ) by Bidelman \& Böhm (1955) and as $\mathrm{A} 3 \mathrm{~V}(\mathrm{pSrCr})$ by Abt \& Morrell (1995). Renson (1979) discussed photometric variability of this star, suggesting a period of 2.13 d . A revised analysis by Maitzen et al. (1980) established a rotational period of $3.9516 \pm 0.0003 \mathrm{~d}$ with an outstanding 0.13 mag double-wave variation in the Strömgren $v$ passband. These authors also reported


Figure 17. Top: amplitude spectrum at low frequency showing the rotation signal of TIC 277688819. Middle: phase-folded light curve showing a double-wave nature. The light curve is folded on a period of $8.3200 \pm 0.0084 \mathrm{~d}$ and is binned $50: 1$. Bottom: an amplitude spectrum to almost the Nyquist frequency of the TESS data showing a distinct lack of pulsational variability down to a limit of $13 \mu \mathrm{mag}$. The rotation signal, its harmonics, and low-frequency noise have been removed.
coarse photographic measurements of the longitudinal magnetic field with an amplitude of about 2 kG , but no clear changes with the rotational phase. Catalano, Kroll \& Leone (1991) and Catalano, Leone \& Kroll (1998) confirmed the 3.9 d rotational period of TIC 281668790 with near-IR $J H K$ photometric observations.

Definitive longitudinal field measurements were made for TIC 281668790 by Hubrig et al. (2006) and Kochukhov \& Bagnulo (2006) with the use of observations collected with the FORS1 lowresolution spectropolarimeter at the ESO VLT. The latter authors also derived $T_{\text {eff }}=8260 \pm 200 \mathrm{~K}, \log L / \mathrm{L}_{\odot}=1.24 \pm 0.04$, $M=1.91 \pm 0.03 \mathrm{M}_{\odot}$ using photometric temperature calibrations, theoretical stellar evolutionary models, and Hipparcos parallax.

Elkin et al. (2008) determined $T_{\text {eff }}=8000 \pm 200 \mathrm{~K}, \log g=$ $4.0 \pm 0.2$, by fitting theoretical spectra to the hydrogen Balmer lines. They also reported several additional longitudinal field measurements, which, together with the literature data, allowed them to establish a clear sinusoidal variation of $\left\langle B_{z}\right\rangle$ between about -2 and +2 kG .

Chemical abundances derived by Elkin et al. (2008) for TIC 281668790 revealed a large heavy element overabundance and a discrepancy between abundances of singly and doubly ionized rare-earth elements, typical of roAp stars (Ryabchikova et al. 2004). Nesvacil et al. (2012) carried out a detailed phase-resolved spectroscopic study of TIC 281668790, deriving surface abundance distributions of 13 elements with the Doppler imaging technique. They also analysed all available magnetic field measurements, finding a dipolar field strength of $B_{\mathrm{p}}=6.9 \pm 1.0 \mathrm{kG}$ and an obliquity of $\beta=88 \pm 12^{\circ}$. The atmospheric parameters, $T_{\text {eff }}=8300 \pm 250 \mathrm{~K}$, $\log g=4.0 \pm 0.2$, obtained by Nesvacil et al. (2012) are compatible with previous determinations.
Null results of photometric searches of rapid oscillations in TIC 281668790 were reported by Weiss (1979) and Martinez \& Kurtz (1994). Furthermore, Elkin et al. (2008) could not find radial velocity oscillations above a few tens of $\mathrm{m} \mathrm{s}^{-1}$ in the period range typical of roAp stars using two $1-2 \mathrm{~h}$-long time series observations with the UVES spectrograph at the ESO VLT. These ground-based observations established TIC 281668790 as a noAp star.
The TESS observations in sector 2 support the ground-based observations of TIC 281668790. The amplitude spectrum at low frequency of the TESS data shows the rotation frequency and its first harmonic (Fig. 18). This indicated a double-wave nature to the light curve, which is evidenced by the phase-folded light curve shown in Fig. 18. The rotation period is the same as that given in the literature, within the errors.

The bottom panel of Fig. 18 shows the full amplitude spectrum of TIC 281668790 , demonstrating the lack of a detection of pulsations in the TESS data. The detection limit to pulsational variability, at $6 \mu \mathrm{mag}$, is estimated from the top of the noise peaks, which is approximately 4 times the error of the highest amplitude noise peak. These results strongly support the case that TIC 281668790 is a noAp star.

## 8 CONCLUSIONS

In this work we present the results from the analysis of the first data collected by the TESS satellite on Ap stars, acquired during the obsevation of sectors 1 and 2 , with a 2 -min cadence. The sample studied is composed of 83 stars, of which 80 were previously classified as chemically peculiar, 7 of which were known to be roAp stars prior to the TESS launch. The main outcomes from this analysis can be summarized as follows:
(i) Five new roAp stars were discovered, including one hosting the highest frequency pulsations of any known roAp star (TIC 350146296; highest pulsation frequency of 3.562 mHz , corresponding to a period of 4.68 min ). The new roAp stars TIC 152808505, TIC 350146296 , and TIC 431380369 show multiple principal pulsation frequencies and rotational multiplets. In addition, TIC 12968953 was found to be multiperiodic and TIC 41259805 was found to have a single pulsation frequency split by rotation. Also, one of the new roAp stars, TIC 41259805, has the shortest rotation period measured for this class of objects, $P_{\text {rot }}=$ 1.71 d , although other Ap stars not known to be roAp have shorter rotation periods. Considering that three of these stars were found


Figure 18. Top: amplitude spectrum at low frequency showing the rotation signal of TIC 281668790. Middle: phase-folded light curve showing a double wave. The light curve is folded on a period of $3.9517 \pm 0.0001 \mathrm{~d}$ and is binned 50:1. Bottom: an amplitude spectrum to almost the Nyquist frequency of the TESS data showing a distinct lack to pulsational variability to a limit of $6 \mu \mathrm{mag}$. The rotation signal, its harmonics, and low-frequency noise have been removed.
among the sample of 73 Ap stars not previously known to pulsate, we estimate a 4 per cent incidence of the roAp phenomenon among Ap stars. An important result of this study is the knowledge that roAp stars are rare, rather than just difficult to detect. Previous ground-based studies were all more limited by $\mathrm{S} / \mathrm{N}$ than the uniform, high-precision TESS data.
(ii) Seven previously known roAp stars, members of the sample, were also analysed. In five of them, TIC 167695608 , TIC 237336864, TIC 348717688, TIC 139191168, and TIC 211404370, either additional or different pulsation frequencies were discovered. Moreover, in another two, TIC 69855370 and TIC 394124612, it was possible to distinguish the correct pulsation frequency from possible aliases present in the ground-based data.
(iii) The new roAp star TIC 350146296 and the previously known roAp star TIC 237336864 show particularly interesting and challenging pulsation spectra, with the presence of several multiplets. These stars are promising candidates for further asteroseismic studies.
(iv) Two of the best characterized noAp stars known to date, TIC 281668790 and TIC 277688819, with properties very similar to those of typical roAp stars were also analysed. The analyses
set pulsation amplitude limits in these stars of 6 and $13 \mu \mathrm{mag}$, respectively, in the TESS filter.
(v) We found a typical reduction factor of 6 in the pulsation amplitudes observed through the TESS filter, compared with the $B$ filter usually used in ground-based surveys. This corresponds to an amplitude suppression of 83 per cent. To determine this value, we considered only stars showing stable modes, with a clearly dominant mode or well-resolved modes, and with no sign of rotational modulation. Still, a definitive value requires simultaneous observations from TESS and ground-based observatories.
(vi) We have identified 27 new rotational variables in our sample. Moreover, we found that the rotation period has been misidentified in five of the previously known rotational variables, TIC 307642246, TIC 309148260, TIC 336731635, TIC 348898673, and TIC 394124612; we provided corrected values for them. For another two stars, we found rotation periods that are slightly, but significantly, different to the values published in the literature (Table 2).

The results from this study provide important insights to the state-of-the-art theoretical models of chemically peculiar, magnetic A stars. In particular, concerning pulsational variability, we find puzzling frequency separations, possible additional cases of stars with frequencies higher than those predicted to be excited by the opacity mechanism, and additional pulsating stars located outside the theoretical instability strip. These new observations are challenges to theory. Moreover, we continue to witness a lack of roAp stars located close to the theoretical blue edge and continue to fail to find pulsations in stars that are, from the photometric and spectroscopic point-of-view, twins of roAp stars. All of these findings reinforce the urgency to revisit the theory of pulsations in chemically peculiar, strongly magnetic, stars.

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[^0]:    ${ }^{2}$ http://archive.stsci.edu/tess/all_products.html

[^1]:    ${ }^{1}$ https://mast.stsci.edu/portal/Mashup/Clients/Mast/Portal.html

[^2]:    ${ }^{3}$ http://www.cbabelgium.com/peranso/index.htm

[^3]:    ${ }^{4}$ Note that we have changed the labelling of the modes presented by Martinez et al. (1998) to be in increasing frequency order, rather than in decreasing amplitude order, to fit the convention we use in this work.

[^4]:    ${ }^{5}$ Again, note that we have changed the labeling of the modes presented by Kurtz et al. (2006) to fit the convention we use in this work.

