3D Human Pose Estimation from a Single Image via Distance Matrix Regression

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Abstract

This paper addresses the problem of 3D human pose estimation from a single image. We follow a standard two-step pipeline by first detecting the 2D position of the N body joints, and then using these observations to infer 3D pose. For the first step, we use a recent CNN-based detector. For the second step, most existing approaches perform 2N-to-3N regression of the Cartesian joint coordinates. We show that more precise pose estimates can be obtained by representing both the 2D and 3D human poses using $N \times N$ distance matrices, and formulating the problem as a 2D-to-3D distance matrix regression. For learning such a regressor we leverage on simple Neural Network architectures, which by construction, enforce positivity and symmetry of the predicted matrices. The approach has also the advantage to naturally handle missing observations and allowing to hypothesize the position of non-observed joints. Quantitative results on Humaneva and Human3.6M datasets demonstrate consistent performance gains over state-of-the-art. Qualitative evaluation on the images in-the-wild of the LSP dataset, using the regressor learned on Human3.6M, reveals very promising generalization results.

1. Introduction

Estimating 3D human pose from a single RGB image is known to be a severely ill-posed problem, because many different body configurations can have virtually the same projection. A typical solution consists in using discriminative strategies to directly learn mappings from image evidence (e.g. HOG, SIFT) to 3D poses [1, 9, 32, 36, 44]. This has been recently extended to end-to-end mappings using CNNs [23, 46]. In order to be effective, though, these approaches require large amounts of training images annotated with the ground truth 3D pose. While obtaining this kind of data is straightforward for 2D poses, even for images 'in the wild' (e.g. FLIC [35] or LSP [18] datasets), it requires using sophisticated Motion Capture (MoCap) systems for the 3D case. Additionally, the datasets acquired this way (e.g. Humaneva [37], Human3.6M [17]) are mostly indoors and their images are not representative of the type

of image appearances outside the laboratory.

It seems therefore natural to split the problem in two stages: Initially use robust image-driven 2D joint detectors, and then infer the 3D pose from these image observations using priors learned from MoCap data. This pipeline has already been used in a number of works [10, 31, 39, 40, 50, 52] and is the strategy we consider in this paper. In particular, we first estimate 2D joints using a recent CNN detector [51]. For the second stage, most previous methods perform the 2D-to-3D inference in Cartesian space, between 2N- and 3N- vector representations of the N body joints. In contrast, we propose representing 2D and 3D poses using $N \times N$ matrices of Euclidean distances between every pair of joints, and formulate the 3D pose estimation problem as one of 2D-to-3D distance matrix regression¹. Fig. 1, illustrates our pipeline.

Despite being extremely simple to compute, Euclidean Distance Matrices (EDMs) have several interesting advantages over vector representations that are particularly suited for our problem. Concretely, EDMs: 1) naturally encode structural information of the pose. Inference on vector representations needs to explicitly formulate such constraints; 2) are invariant to in-plane image rotations and translations, and normalization operations bring invariance to scaling; 3) capture pairwise correlations and dependencies between all body joints.

In order to learn a regression function that maps 2D-to-3D EDMs we consider Fully Connected (FConn) and Fully Convolutional (FConv) Network architectures. Since the dimension of our data is small ($N \times N$ square matrices, with N = 14 joints in our model), input-to-output mapping can be achieved through shallow architectures, with only 2 hidden layers for the FConn and 4 convolutional layers for the FConv. And most importantly, since the distance matrices used to train the networks are built from solely point configurations, we can easily synthesize artifacts and train the network under 2D detector noise and body part occlusion.

We achieve state-of-the-art results on standard benchmarks including Humaneva-I and Human3.6M datasets, and we show our approach to be robust to large 2D detector er-

¹Once the 3D distance matrix is predicted, the position of the 3D body joints can be estimated using Multidimensional Scaling (MDS).

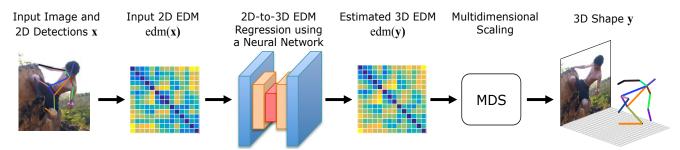


Figure 1. **Overview.** We formulate the 3D human pose estimation problem as a regression between two Euclidean Distance Matrices (EDMs), encoding pairwise distances of 2D and 3D body joints, respectively. The regression is carried out by a Neural Network, and the 3D joint estimates are obtained from the predicted 3D EDM via Multidimensional Scaling.

rors, while (for the case of the FConv) also allowing to hypothesize reasonably well occluded body limbs. Additionally, experiments in the Leeds Sports Pose dataset, using a network learned on Human3.6M, demonstrate good generalization capability on images 'in the wild'.

2. Related Work

Approaches to estimate 3D human pose from single images can be roughly split into three main categories: methods that rely on generative models to constrain the space of possible poses, discriminative approaches that directly predict 3D pose from image evidence, and methods lying in-between the two previous categories.

The most straightforward generative model consists in representing human pose as linear combinations of modes learned from training data [5]. More sophisticated models allowing to represent larger deformations include spectral embedding [43], Gaussian Mixtures on Euclidean or Riemannian manifolds [15, 41] and Gaussian processes [22, 48, 54]. However, exploring the solution space defined by these generative models requires iterative strategies and good enough initializations, making these methods more appropriate for tracking purposes.

Early discriminative approaches [1, 9, 32, 36, 44] focused on directly predicting 3D pose from image descriptors such as SIFT of HOG filters, and more recently, from rich features encoding body part information [16] and from the entire image in Deep architectures [23, 46]. Since the mapping between feature and pose space is complex to learn, the success of this family of techniques depends on the existence of large amounts of training images annotated with ground truth 3D poses. Humaneva [37] and Human3.6M [17] are two popular MoCap datasets used for this purpose. However, these datasets are acquired in laboratory conditions, preventing the methods that uniquely use their data to generalize well to unconstrained and realistic images. [33] addressed this limitation by augmenting the training data for a CNN with automatically synthesized images made of realistic textures.

In between the two previous categories, there are a series of methods that first use discriminative formulations to estimate the 2D joint position, and then infer 3D pose using *e.g.* regression forests, Expectation Maximization or evolutionary algorithms [10, 26, 31, 39, 40, 50, 52]. The two steps can be iteratively refined [39, 50, 52] or formulated independently [10, 26, 31, 40]. By doing this, it is then possible to exploit the full power of current CNN-based 2D detectors like DeepCut [28] or the Convolutional Pose Machines (CPMs) [51], which have been trained with large scale datasets of images 'in-the-wild'.

Regarding the 3D body pose parameterization, most approaches use a skeleton with a number N of joints ranging between 14 and 20, and represented by 3N vectors in a Cartesian space. Very recently, [10] used a generative volumetric model of the full body. In order to enforce joint dependency during the 2D-to-3D inference, [17] and [46] considered latent joint representations, obtained through Kernel Dependency Estimation and autoencoders. In this paper, we propose using $N \times N$ Euclidean Distance Matrices for capturing such joint dependencies.

EDMs have already been used in similar domains, *e.g.* in modal analysis to estimate shape basis [2], to represent protein structures [20], for sensor network localization [7] and for the resolution of kinematic constraints [29]. It is worth to point that for 3D shape recognition tasks, Geodesic Distance Matrices (GDMs) are preferred to EDMs, as they are invariant to isometric deformations [42]. Yet, for the same reason, GDMs are not suitable for our problem, because multiple shape deformations yield the same GDM. In contrast, the shape that produces a specific EDM is unique (up to translation, rotation and reflection), and it can be estimated via Multidimensional Scaling [7, 11].

Finally, representing 2D and 3D joint positions by distance matrices, makes it possible to perform inference with simple Neural Networks. In contrast to recent CNN based methods for 3D human pose estimation [23, 46] we do not need to explicitly modify our networks to model the underlying joint dependencies. This is directly encoded by the distance matrices.

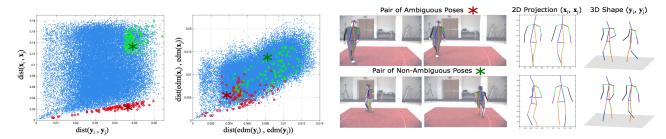


Figure 2. **EDMs vs Cartesian representations. Left:** Distribution of relative 3D and 2D distances between random pairs of poses, represented as Cartesian vectors (first plot) and EDM matrices (second plot). Cartesian representations show a more decorrelated pattern (Pearson correlation coefficient of 0.09 against 0.60 for the EDM), and in particular suffer from larger ambiguities, *i.e.* poses with similar 2D projections and dissimilar 3D shape. Red circles indicate the most ambiguous such poses, and green circles the most desirable configurations (large 2D and 3D differences). Note that red circles are more uniformly distributed along the vertical axis when using EDM representations, favoring larger differences and better discriminability. **Right:** Pairs of dissimilar 3D poses with similar (top) and dissimilar (bottom) projections. They correspond to the dark red and dark green 'asterisks' in the left-most plots.

3. Method

Fig. 1 illustrates the main building blocks of our approach to estimate 3D human pose from a single RGB image. Given that image, we first detect body joints using a state-of-the-art detector. Then, 2D joints are normalized and represented by a EDM, which is fed into a Neural Network to regress a EDM for the 3D body coordinates. Finally, the position of the 3D joints is estimated via a 'reflexion-aware' Multidimensional Scaling approach [7]. We next describe in detail each of these steps.

3.1. Problem Formulation

We represent the 3D pose as a skeleton with N=14 joints and parameterized by a 3N vector $\mathbf{y} = [\mathbf{p}_1^\top, \dots, \mathbf{p}_N^\top]^\top$, where \mathbf{p}_i is the 3D location of the *i*-th joint. Similarly, 2D poses are represented by 2N vectors $\mathbf{x} = [\mathbf{u}_1^\top, \dots, \mathbf{u}_N^\top]^\top$, where \mathbf{u}_i are pixel coordinates. Given a full-body person image, our goal is to estimate the 3D pose vector \mathbf{y} . For this purpose, we follow a regression based discriminative approach. The most general formulation of this problem would involve using a set of training images to learn a function that maps input images, or its features, to 3D poses. However, as discussed above, such a procedure would require a vast amount of data to obtain good generalization.

Alternatively, we will first compute the 2D joint position using the Convolutional Pose Machine detector [51]. We denote by \tilde{x} the output of the CPM, which is a noisy version of the ground truth 2D pose x.

We can then formally write our problem as that of learning a mapping function $f : \mathbb{R}^{2N} \to \mathbb{R}^{3N}$ from potentially corrupted 2D joint observations $\tilde{\mathbf{x}}$ to 3D poses \mathbf{y} , given an annotated and clean training dataset $\{\mathbf{x}_i, \mathbf{y}_i\}_{i=1}^{D}$.

3.2. Representing Human Pose with EDMs

In oder to gain depth-scale invariance we first normalize the vertical coordinates of the projected 2D poses x_i to be within the range [-1, 1]. 3D joint positions y_i are expressed in meters with no further pre-processing. We then represent both 2D and 3D poses by means of Euclidean Distance Matrices. For the 3D pose y we define $\operatorname{edm}(y)$ to be the $N \times N$ matrix where its (m, n) entry is computed as:

$$\operatorname{edm}(\mathbf{y})_{m,n} = \|\mathbf{p}_m - \mathbf{p}_n\|_2 . \tag{1}$$

Similarly, edm(x) is the $N \times N$ matrix built from the pairwise distances between normalized 2D joint coordinates. In case that some of the joints are *occluded*, we set to zero their corresponding rows and columns in edm(x).

Despite being simple to define, EDMs have several advantages over Cartesian representations: EDMs are coordinate-free, invariant to rotation, translation and reflection. Previous regression-based approaches [33, 39, 52] need to compensate for this invariance by pre-aligning the training 3D poses y_i w.r.t. a global coordinate frame, usually defined by specific body joints. Additionally, EDMs do not only encode the underlying structure of plain 3D vector representations, but they also capture richer information about pairwise correlations between all body joints. A direct consequence of both these advantages, is that EDM-based representations allow reducing the inherent ambiguities of the 2D-to-3D human pose estimation problem.

To empirically support this claim we randomly picked pairs of samples from the Humaneva-I dataset and plotted the distribution of relative distances between their 3D and 2D poses, using either Cartesian or EDM representations (see Fig. 2). For the Cartesian case (left-most plot), an entry to the graph corresponds to $[dist(\mathbf{y}_i, \mathbf{y}_j), dist(\mathbf{x}_i, \mathbf{x}_j)]$, where $dist(\cdot)$ is a normalized distance and i, j are two random indices. Similarly, for the EDMs (second plot), an entry to the graph corresponds to $[dist(edm(\mathbf{y}_i), edm(\mathbf{y}_j)), dist(edm(\mathbf{x}_i), edm(\mathbf{x}_j))]$. Observe that 3D and 2D pairwise differences are much more correlated in this case. The interpretation of this pattern is

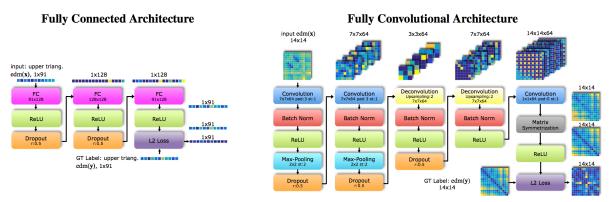


Figure 3. Neural Network Architectures used to perform 2D-to-3D regression of symmetric Euclidean Distance Matrices.

that distance matrices yield larger 3D pose differences for most dissimilar 2D poses. The red circles in the graphs, correspond to the most ambiguous shapes, *i.e.*, pairs of dissimilar poses $\{y_i, y_j\}$ with very similar image projections $\{u_i, u_j\}$. Note that when using EDMs, these critical samples depict larger differences along the vertical axis, *i.e.*, on the 2D representation. This kind of behavior makes it easier the subsequent task of learning the 2D-to-3D mapping.

3.3. 2D-to-3D Distance Matrix Regression

The problem formulated in Sec. 3.1 can now be rewritten in terms of finding the mapping $f : \mathbb{R}^{N \times N} \to \mathbb{R}^{N \times N}$, from potentially corrupted distance matrices $\operatorname{edm}(\tilde{\mathbf{x}})$ to matrices $\operatorname{edm}(\mathbf{y})$ encoding the 3D pose, given a training set $\{\operatorname{edm}(\mathbf{x}_i), \operatorname{edm}(\mathbf{y}_i)\}_{i=1}^{D}$. The expressiveness and low dimensionality of the input and output data (14 × 14 matrices) will make it possible to learn this mapping with relatively tiny Neural Network architectures, which we next describe.

Fully Connected Network. Since distance matrices are symmetric, we first consider a simple FConn architecture with 40K free parameters that regresses the N(N-1)/2 = 91 elements above the diagonal of edm(y). As shown in Fig. 3-left, the network consists of three Fully Connected (FC) layers with 128-128-91 neurons. Each FC layer is followed by a rectified linear unit (ReLU). To reduce overfitting, we use dropout after the first two layers, with a dropout ratio of 0.5 (50% of probability to set a neuron's output value to zero).

The 91-dimensional vector at the output is used to build the 14×14 output EDM, which by construction, is guaranteed to be symmetric. Additionally, the last ReLU layer enforces positiveness of all elements of the matrix, another necessary (but not sufficient) condition for an EDM.

Fully Convolutional Network. Motivated by the recent success of Fully Convolutional Networks in tasks like semantic segmentation [24], flow estimation [13] and change dectection [4], we also consider the architecture shown in Fig. 3-right to regress entire 14×14 distance matrices.

FConv Networks were originally conceived to map images or bi-dimensional arrays with some sort of spatial continuity. The EDMs however, do not convey this continuity and, in addition, they are defined up to a random permutation of the skeleton joints. In any event, for the case of human motion, the distance matrices turn to be highly structured, particularly when handling occluded joints, which results in patterns of zero columns and rows within the input EDM. In the experimental section we will show that FConv networks are also very effective for this kind of situations.

Following previous works [4, 24], we explored an architecture with a contractive and an expansive part. The contractive part consists of two convolutional blocks, with 7×7 kernels and 64 features, each. Convolutional layers are followed by a Batch Normalization (BN) layer with learned parameters, relieving from the task of having to compute such statistics from data during test. BN output is forwarded to a non-linear ReLU; a 2×2 max-pooling layer with stride 2 that performs the actual contraction; and finally, to a dropout layer with 0.5 ratio.

The expansive part also has two main blocks which start with a deconvolution layer, that internally performs a $\times 2$ upsampling and, again, a convolution with 7×7 kernels and 64 features. The deconvolution is followed by a ReLU and a dropout layer with ratio 0.5. For the second block, dropout is replaced by a convolutional layer that contracts the 64, 14 \times 14 features into a single 14 \times 14 channel.

Note that there are no guarantees that the output of the expansive part will be a symmetric and positive matrix, as expected for a EDM. Therefore, before computing the actual loss we designed a layer called 'Matrix Symmetrization' (MS) which enforces symmetry. If we denote by \mathbf{Z} the output of the expansive part, MS will simply compute $(\mathbf{Z} + \mathbf{Z}^{\top})/2$, which is symmetric. A final ReLU layer, guarantees that all values will be also positive.

This Fully Convolutional Network has 606K parameters.

Training. In the experimental section we will report results on multiple training setups. In all of them, the two networks were trained from scratch, and randomly initial-

	Wall	king (Acti	ion 1, Car	nera 1)	Joggi	ng (Acti	ion 2, Ca	mera 1)	Box	ing (Actio	on 5, Cam	era 1)
Method	S1	S2	S3	Average	S1	S2	S3	Average	S1	S2	S 3	Average
Taylor CVPR'10 [45]	48.80	47.40	49.80	48,70	75,35	-	-	-	-	-	-	-
Bo IJCV'10 [8]	45.40	28.30	62.30	45.33	-	-	-	-	42.50	64.00	69.30	58.60
Sigal IJCV'12 [38]	66.00	69.00	-	-	-	-	-	-	-	-	-	-
Ramakrishna ECCV'12 [31](*)	161.80	182.00	188.60	177.47	-	-	-	-	151.00	170.00	158.00	159.67
Simo-Serra CVPR'12 [40]	99.60	108.30	127.40	111.77	-	-	-	-	-	-	-	-
Simo-Serra CVPR'13 [39]	65.10	48.60	73.50	62.40	74.20	46.60	32.20	51.00	-	-	-	-
Radwan ICCV'13 [30]	75.10	99.80	93.80	89.57	79.20	89.80	99.40	89.47	-	-	-	-
Wang CVPR'14 [50]	71.90	75.70	85.30	77.63	62.60	77.70	54.40	64.90	-	-	-	-
Belagiannis CVPR'14 [6]	68.30	-	-	-	-	-	-	-	62.70	-	-	-
Kostrikov BMVC'14 [21]	44.00	30.90	41.70	38,87	57.20	35.00	33.30	41.83	-	-	-	-
Elhayek CVPR'15 [12]	66.50	-	-	_	-	-	-	-	60.00	-	-	-
Akhter CVPR'15 [3](*)	186.10	197.80	209.40	197.77	-	-	-	-	165.50	196.50	208.40	190.13
Tekin CVPR'16 [47]	37.50	25.10	49.20	37.27	-	-	-	-	50.50	61.70	57.50	56.57
Yasin CVPR'16 [52]	35.80	32.40	41.60	36.60	46.60	41.40	35.40	41.13	-	-	-	-
Zhou PAMI'16 [55](*)	100.00	98.90	123.10	107.33	-	-	-	-	112.50	118.60	110.00	113.70
Bogo ECCV'16 [10]	73.30	59.00	99.40	77.23	-	-	-	-	82.10	79.20	87.20	82.83
			Our App	roach, Full	y Conne	cted Net	twork					
Train 2D: GT, Test: CPM	35.70	36.80	41.34	37.95	41.25	27.96	34.34	34.52	47.26	50.52	67.64	55.14
Train 2D: CPM, Test: CPM	20.16	14.00	28.76	20.97	38.12	17.95	21.42	25.83	44.05	48.52	57.00	49.86
Train 2D: GT+CPM, Test: CPM	19.72	13.52	26.46	19.90	34.64	17.85	20.05	24.18	45.67	47.52	57.63	50.27
		C	Our Appro	oach, Fully	Convolu	tional N	etwork					
Train 2D: GT, Test: CPM	28.35	27.75	38.93	31.68	47.75	27.82	30.21	35.26	42.40	49.15	59.17	50.24
Train 2D: CPM, Test: CPM	19.82	12.64	26.19	19.55	43.83	21.79	22.10	29.24	45.55	47.64	46.52	46.57
Train 2D: GT+CPM, Test: CPM	19.68	13.02	24.89	19.20	39.69	20.04	21.04	26.92	46.63	47.56	46.45	46.88

Table 1. **Results on the Humaneva-I dataset.** Average error (in mm) between the ground truth and the predicted joint positions. '-' indicates that the results for that specific 'action' and 'subject' are not reported. The results of all approaches are obtained from the original papers, except for (*), which were obtained from [10].

ized using the strategy proposed in [14]. We use a standard L2 loss function in the two cases. Optimization is carried out using Adam [19], with a batch size of 7 EDMs for Humaneva-I and 200 EDMs for Human3.6M. FConn generally requires about 500 epochs to converge and FConv about 1500 epochs. We use default Adam parameters, except for the step size α , which is initialized to 0.001 and reduced to 0.0001 after 250 (FConn) and 750 (FConv) epochs. The model definition and training is run under MatconvNet [49].

3.4. From Distance Matrices to 3D Pose

Retrieving the 3D joint positions $\mathbf{y} = [\mathbf{p}_1^\top, \dots, \mathbf{p}_N^\top]^\top$ from a potentially noisy distance matrix edm(\mathbf{y}) estimated by the neural network, can be formulated as the following error minimization problem:

$$\underset{\mathbf{p}_1,\ldots,\mathbf{p}_N}{\arg\min} \sum_{m,n} |\|\mathbf{p}_m - \mathbf{p}_n\|_2^2 - \operatorname{edm}(\mathbf{y})_{m,n}^2|.$$
(2)

We solve this minimization using [7], a MDS algorithm which poses a semidefinite programming relaxation of the non-convex Eq. 2, refined by a gradient descent method.

Yet, note that the shape y we retrieve from edm(y) is up to a reflection transformation, *i.e.*, y and its reflected version y^* yield the same distance matrix. In order to disambiguate this situation, we keep either y or y^* based on their degree of anthropomorphism, measured as the number of joints with angles within the limits defined by the physically-motivated prior provided by [3].

4. Experiments

We extensively evaluate the proposed approach on two publicly available datasets, namely Humaneva-I [37] and Human3.6M [17]. Besides quantitative comparisons w.r.t. state-of-the-art we also assess the robustness of our approach to noisy 2D observations and joint occlusion. We further provide qualitative results on the LSP dataset [18]

Unless specifically said, we assume the 2D joint positions in our approach are obtained with the CPM detector [51], fed with a bounding box of the full-body person image. As common practice in literature [39, 52], the reconstruction error we report refers to the average 3D Euclidean joint error (in mm), computed after rigidly aligning the estimated pose with the ground truth (if available).

4.1. Evaluation on Humaneva-I

For the experiments with Humaneva-I we train our EDM regressors on the training sequences for the Subjects 1, 2 and 3, and evaluate on the 'validation' sequences. This is the same evaluation protocol used by the baselines we compare against [3, 6, 8, 10, 12, 21, 30, 31, 38, 39, 40, 45, 47, 50, 52, 55, 56]. We report the performance on the 'Walking', 'Jogging' and 'Boxing' sequences. Regarding our own approach we consider several configurations depending on the type of regressor: Fully Connected or Fully Convolutional Network; and depending on the type of 2D source used for training: Ground Truth (GT), CPM or GT+CPM.



Figure 4. **Hypothesysing Occluded Body Parts.** Ground truth and hypothesized body parts obtained using the Fully Convolutional distance matrix regressor (Subject 3, action 'Jogging' from Humaneva-I). The network is trained with pairs of occluded joints and is able to predict one occluded limb (2 neighboring joints) at a time. Note how the generated tracks highly resemble the ground truth ones.

			Walk	ing (Act	ion 1, C	amera 1)	Joggi	ing (Acti	ion 2, Ca	mera 1)	Box	ing (Actio	n 5, Cam	era 1)
NN Arch.	Occl. Type	Error	S1	S2	S 3	Average	S1	S2	S 3	Average	S1	S2	S 3	Average
FConn	2 Rand. Joints	Avg. Error	53.30	59.49	51.99	54.93	49.93	27.91	37.07	38.30	49.63	60.74	64.53	58.30
		Error Occl. Joints	53.95	60.24	53.65	55.95	54.06	30.61	43.25	42.64	56.32	68.74	72.04	65.70
FConn	Right Arm	Avg. Error	55.55	59.16	49.31	54.67	54.45	31.30	36.73	40.83	49.48	69.59	68.26	62.44
		Error Occl. Joints	59.38	55.02	45.32	53.24	72.48	37.25	41.33	50.35	100.57	127.29	134.75	120.87
FConn	Left Leg	Avg. Error	53.51	55.87	60.04	56.47	49.83	30.90	41.16	40.63	46.68	64.85	62.04	57.86
		Error Occl. Joints	83.15	86.73	88.25	86.04	85.58	61.38	82.04	76.33	38.43	72.66	55.12	55.40
FConv	2 Rand. Joints	Avg. Error	31.56	28.00	38.49	32.68	46.63	26.61	34.34	35.86	50.00	54.19	56.12	53.44
		Error Occl. Joints	32.96	30.22	45.79	36.32	48.04	29.57	40.32	39.31	58.60	60.59	66.34	61.84
FConv	Right Arm	Avg. Error	37.96	27.70	35.27	33.64	51.00	28.11	31.81	36.97	58.09	59.74	62.78	60.20
		Error Occl. Joints	48.06	27.57	29.72	35.12	69.59	32.78	34.79	45.72	111.61	101.49	132.76	115.29
FConv	Left Leg	Avg. Error	34.42	38.64	41.69	38.25	39.72	29.22	33.62	34.19	50.68	53.85	50.14	51.56
		Error Occl. Joints	61.03	64.79	71.48	65.77	59.3	59.24	67.11	61.88	44.59	61.23	46.48	50.77

Table 2. **Results on the Humaneva-I under Occlusions.** Average overall joint error and average error of the occluded and hypothesized joints (in mm) using the proposed Fully Connected and Fully Convolutional regressors. We train the two architectures with 2D GT+CPM and with random pairs of occluded joints. Test is carried out using the CPM detections with specific occlusion configurations.

The 2D source used for evaluation is always CPM.

Table 1 summarizes the results, and shows that all configurations of our approach significantly outperform stateof-the-art. The improvement is particularly relevant when modeling the potential deviations of the CPM by directly using its 2D detections to train the regressors. Interestingly, note that the results obtained by FConn and FConv are very similar, being the former a much simpler architecture. However, as we will next show, FConv achieves remarkably better performance when dealing with occlusions.

Robustness to Occlusions. The 3D pose we estimate obviously depends on the quality of the 2D CPM detections. Despite the CPM observations we have used do already contain certain errors, we have explicitly evaluated the robustness of our approach under artificial noise and occlusion artifacts. We next assess the impact of occlusions. We leave the study of the 2D noise for the following section.

We consider two-joint occlusions, synthetically produced by removing two nodes of the projected skeleton. In order to make our networks robust to such occlusions and also able to hypothesize the 3D position of the non-observed joints, we re-train them using pairs $\{edm(\mathbf{x}_i^{occ}), edm(\mathbf{y}_i)\}_{i=1}^{D}$, where $edm(\mathbf{x}_i^{occ})$ is the same as $edm(\mathbf{x}_i)$, but with two random rows and columns set to zero. At test, we consider the cases with random joint occlusions or with structured occlusions, in which we completely remove the observation of one body limb (full leg or full arm).

Table 2 reports the reconstruction error for FConn and FConv. Overall results show a clear and consistent advantage of the FConv network, yielding error values which are even comparable to state-of-the-art approaches when observing all joints (see Table 1). Furthermore, note that the error of the hypothesized joints is also within very reasonable bounds, exploiting only for the right arm position in the 'boxing' activity (error > 100 mm). This is in the line of previous works which have shown that the combination of convolutional and deconvolutional layers is very effective for image reconstruction and segmentation tasks [27, 53]. A specific example of joint hallucination is shown in Fig. 4.

4.2. Evaluation on Human3.6M

The Human3.6M dataset consists of 3.6 Million 3D poses of 11 subjects performing 15 different actions under 4 viewpoints. We found in the literature 3 different evaluation protocols. For Protocol #1, 5 subjects (S1, S5, S6, S7 and S8) are used for training and 2 (S9 and S11) for testing. Training and testing is done independently per each action and using all camera views. Testing is carried out in all images. This protocol is used in [17, 23, 34, 46, 47, 56]. Protocol #2 only differs from Protocol #1 in that only the frontal view is considered for test. It has been recently used in [10], which also evaluates [3, 31, 55]. Finally, in Protocol #3, training data comprises all actions and viewpoints. Six

Method	Direct.	Discuss	Eat	Greet	Phone	Pose	Purch.	Sit	SitD	Smoke	Photo	Wait	Walk	WalkD	WalkT	Avg
						Pro	tocol #1									
Ionescu PAMI'14 [17]	132.71	183.55	133.37	164.39	162.12	205.94	150.61	171.31	151.57	243.03	162.14	170.69	177.13	96.60	127.88	162,20
Li ICCV'15 [23]	-	136.88	96.94	124.74	-	168.08	-	-	-	-	-	-	132.17	69.97	-	-
Tekin BMVC'16 [46]	-	129.06	91.43	121.68	-	-	-	-	-	-	162.17	-	65.75	130.53	-	-
Tekin CVPR'16 [47]	102.41	147.72	88.83	125.28	118.02	112.38	129.17	138.89	224.90	118.42	182.73	138.75	55.07	126.29	65.76	124.97
Zhou CVPR'16 [56]	87.36	109.31	87.05	103.16	116.18	143.32	106.88	99.78	124.52	199.23	107.42	118.09	114.23	79.39	97.70	112.91
Sanzari ECCV'16 [34]	48.82	56.31	95.98	84.78	96.47	66.30	107.41	116.89	129.63	97.84	105.58	65.94	92.58	130.46	102.21	93.15
Ours, FConv, Test 2D: CPM	67.48	79.01	76.48	83.12	97.43	74.58	71.96	102.40	116.68	87.70	100.37	94.57	75.21	82.72	74.92	85.64
						Pro	tocol #2									
Ramakrishna ECCV'12 [31](*)	137.40	149.30	141.60	154.30	157.70	141.80	158.10	168.60	175.60	160.40	158.90	161.70	174.80	150.00	150.20	156.03
Akhter CVPR'15 [3](*)	1199.20	177.60	161.80	197.80	176.20	195.40	167.30	160.70	173.70	177.80	186.50	181.90	198.60	176.20	192.70	181.56
Zhou PAMI'16 [55](*)	99.70	95.80	87.90	116.80	108.30	93.50	95.30	109.10	137.50	106.00	107.30	102.20	110.40	106.50	115.20	106.10
Bogo ECCV'16 [10]	62.00	60.20	67.80	76.50	92.10	73.00	75.30	100.30	137.30	83.40	77.00	77.30	86.80	79.70	81.70	82.03
Ours. FConv, Test 2D: CPM	64.11	76.58	70.59	80.81	93.01	74.01	65.45	87.93	109.49	83.81	96.31	93.08	73.51	81.57	72.59	81.52
5.						Pro	tocol #3									
Yasin CVPR'16 [52]	88.40	72.50	108.50	110.20	97.10	81.60	107.20	119.00	170.80	108.20	142.50	86.90	92.10	165.70	102.00	110.18
Rogez NIPS'16 [33]	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	88.10
Ours, FConv, Test 2D: CPM	66.05	61.69	84.51	73.73	65.23	67.17	60.85	67.29	103.48	74.75	92.55	69.59	71.47	78.04	73.23	73.98

Table 3. **Results on the Human3.6M dataset.** Average joint error (in mm) considering the 3 evaluation prototocols described in the text. The results of all approaches are obtained from the original papers, except for (*), which are from [10].

Occ. Type	Error	Direct.	Discuss	Eat	Greet	Phone	Pose	Purch.	Sit	SitD	Smoke	Photo	Wait	Walk	WalkD	WalkT	Avg
2 Rnd.Joints	Avg. Error	88.53	97.83	139.99	99.57	106.13	102.78	92.97	113.35	126.62	111.73	122.74	109.85	95.1	96.76	97.97	106.79
	Err.Occl. Joints	94.77	104.37	155.66	110.48	119.62	103.83	91.04	141.31	135.35	137.76	146.68	131.41	116.16	96.11	99.73	118.95
Left Arm	Avg. Error	197.86	101.88	123.91	109.72	93.00	106.15	100.55	113.19	129.50	111.15	135.72	118.07	99.21	100.73	100.94	109.44
	Err.Occl. Joints	177.44	177.68	152.06	220.28	145.93	180.42	143.24	192.42	154.62	184.24	253.88	213.6	176.11	160.44	188.38	181.38
Right Leg	Avg. Error	79.94	82.23	132.64	92.05	100.77	97.32	76.37	126.95	125.51	106.66	109.82	95.92	94.88	89.82	91.60	100.17
	Err.Occl. Joints	81.23	92.57	177.80	103.69	148.45	120.74	92.63	200.56	183.03	146.10	145.29	107.36	133.11	105.9	120.12	130.57

Table 4. **Results on Human3.6M under Occlusions.** Average overall joint error and average error of the hypothesized occluded joints (in mm). The network is trained and evaluated according to the 'Protocol #3' described in the text.

2D Input	Direct.	Discuss	Eat	Greet	Phone	Pose	Purch.	Sit	SitD	Smoke	Photo	Wait	Walk	WalkD	WalkT	Avg
GT	53.51	50.52	65.76	62.47	56.9	60.63	50.83	55.95	79.62	63.68	80.83	61.80	59.42	68.53	62.11	62.17
GT + N(0, 5)	57.05	56.05	70.33	65.46	60.39	64.49	59.06	58.62	82.80	67.85	83.97	70.13	66.76	75.04	68.62	67.11
GT+N(0, 10)	76.46	70.74	77.18	77.25	73.42	81.94	64.65	71.05	97.08	76.91	93.45	77.12	85.14	80.96	83.47	79.12
GT+N(0, 15)	90.72	91.99	96.54	94.99	87.43	101.81	89.39	84.46	107.26	93.31	106.01	95.96	100.38	96.59	104.41	96.08
$GT+\mathcal{N}(0,20)$	109.84	110.21	117.13	115.16	107.08	116.92	107.14	101.82	131.43	114.76	115.07	112.54	125.50	118.93	129.73	115.55

Table 5. Results on the Human3.6M dataset under 2D Noise. Average 3D joint error for increasing levels of 2D noise. The network is trained with 2D Ground Truth (GT) data and evaluated with GT+ $\mathcal{N}(\mathbf{0},\sigma)$. where σ is the standard deviation (in pixels) of the noise.

subjects (S1, S5, S6, S7, S8 and S9) are used for training and every 64^{th} frame of the frontal view of S11 is used for testing. This is the protocol considered in [33, 52].

We will evaluate our approach on the three protocols. In contrast to HumanEva experiments, CPM detections will not be used for training (very time consuming), and we will train with the ground truth 2D positions. CPM detections are used during test, though. For Protocol #3 we choose the training set by randomly picking 400K samples among all poses and camera views, a similar number as in [52]. For the rest of experiments we will only consider the FConv regressor, which showed overall better performance than FConn in the Humaneva dataset. The results are summarized in Table 3. For Protocols #1 and #3 our approach improves state-of-the-art by a considerable margin, and for Protocol #2 is very similar to [10], a recent approach that relies on a high-quality volumetric prior of the body shape.

Robustness to Occlusions. We perform the same occlusion analysis as we did for Humaneva-I and re-train the network under randomly occluded joints and test for random and structured occlusions. The results (under Protocol #3) are reported in Table 4. Again, note that the average body error remains within reasonable bounds. There are, how-

ever, some specific actions (*e.g.* 'Sit', 'Photo') for which the occluded leg or arm are not very well hypothesized. We believe this is because in these actions, the limbs are in configurations with only a few samples on the training set. Indeed, state of the art methods also report poor performance on these actions, even when observing all joints.

Robustness to 2D Noise. We further analyze the robustness of our approach (trained on clean data) to 2D noise. For this purpose, instead of using CPM detections for test, we used the 2D ground truth test poses with increasing amounts of Gaussian noise. The results of this analysis are given in Table 5. Note that the 3D error gradually increases with the 2D noise, but does not seem to break the system. Noise levels of up to 20 pixels std are still reasonably supported. As a reference, the mean 2D error of the CPM detections considered in Tables 4 and 3 is of 10.91 pixels. Note also that there is still room for improvement, as more precise 2D detections can considerably boost the 3D pose accuracy.

4.3. Evaluation on Leeds Sports Pose Dataset

We finally explore the generalization capabilities of our approach on the LSP dataset. For each input image, we locate the 2D joints using the CPM detector, perform the

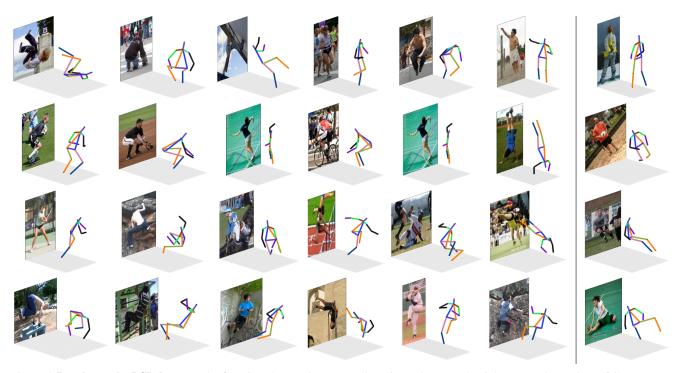


Figure 5. Results on the LSP dataset. The first six columns show correctly estimated poses. The right-most column shows failure cases.

	5 4.7
Reproj. 2D CPM 12.68 8.71 10.32 9.50 8.05 5.79 7.61 5.	4 8.8
Reproj. 2D GT 9.75 7.33 7.47 6.05 6.14 4.52 6.24 4.	9 6.6

Table 6. Reprojection Error (in pixels) on the LSP dataset.

2D-to-3D EDM regression using the Fully Convolutional network learned on Human3.6M (Protocol #3) and compute the 3D pose through MDS. Additionally, once the 3D pose is estimated, we retrieve the rigid rotation and translation that aligns it with the input image using a PnP algorithm [25]. Since the internal parameters of the camera are unknown, we sweep the focal length configuration space and keep the solution that minimizes the reprojection error.

The lack of 3D annotation makes it not possible to perform a quantitative evaluation of the 3D shapes accuracy. Instead, in Table 6, we report three types of 2D reprojection errors per body part, averaged over the 2000 images of the dataset: 1) Error of the CPM detections; 2) Error of the reprojected shapes when estimated using CPM 2D detections; and 3) Error of the reprojected shapes when estimated using 2D GT annotations. While these results do not guarantee good accuracy of the estimated shapes, they are indicative that the method is working properly. A visual inspection of the 3D estimated poses, reveals very promising results, even for poses which do not appear on the Human3.6M dataset used for training (see Fig. 5). There still remain failure cases (shown on the right-most column), due to *e.g.* detector misdetections, extremal body poses or camera viewpoints that largely differ from those of Human3.6M.

5. Conclusion

In this paper we have formulated the 3D human pose estimation problem as a regression between matrices encoding 2D and 3D joint distances. We have shown that such matrices help to reduce the inherent ambiguity of the problem by naturally incorporating structural information of the human body and capturing joints correlations. The distance matrix regression is carried out by simple Neural Network architectures, that bring robustness to noise and occlusions of the 2D detected joints. In the latter case, a Fully Convolutional network has allowed to hypothesize unobserved body parts. Quantitative evaluation on standard benchmarks shows remarkable improvement compared to state of the art. Additionally, qualitative results on images 'in the wild' show the approach to generalize well to untrained data. Since distance matrices just depend on joint positions, new training data from novel viewpoints and shape configurations can be readily synthesized. In the future, we plan to explore online training strategies exploiting this.

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