Spectroscopic aperture biases in inside-out evolving early-type galaxies from CALIFA*


Received 5 September 2015 / Accepted 2 November 2015

ABSTRACT

Integral field spectroscopy (IFS) studies based on CALIFA survey data have recently revealed ongoing low-level star formation (SF) in the periphery of a small fraction (~10%) of local early-type galaxies (ETGs), witnessing a still ongoing inside-out galaxy growth process. A distinctive property of the nebular component in these ETGs, classified i+, is a structure with two radial zones, the inner of which displays LINER emission with a Hα equivalent width $EW$(Hα) $\leq$ 1 Å, the outer (3 Å $< EW$(Hα) $< 20$ Å) Hβ-region characteristics. Using CALIFA IFS data, we empirically demonstrate that the confinement of nebular emission to the galaxy periphery leads to a strong aperture (or, correspondingly, redshift) bias in spectroscopic single-fiber studies of type i ETGs: at low redshift ($z$ $\leq$ 0.45), SDSS spectroscopy is restricted to the inner (SF-devoid LINER) zone, which causes the galaxies to be erroneously classified as “retired”, that is, systems entirely lacking SF, and whose faint nebular emission is solely powered by the post-AGB stellar component. The SDSS aperture progressively encompasses the outer SF zone only at higher $z$, at which the galaxies are unambiguously classified as “composite SF/LINER”. We also empirically demonstrate that the principal effect of a decreasing spectroscopic aperture on the classification of i+ ETGs through standard [NII]/Hα vs. [OIII]/Hβ emission-line (BPT) ratios consists of a monotonic shift upward and to the right precisely along the upper right wing of the “seagull” distribution on the BPT plane, that is, along the pathway connecting composite SF/HII galaxies with AGN/LINERs. Motivated by these observational insights, we also investigate theoretically observational biases in aperture-limited studies of inside-out growing galaxies as a function of $z$. To this end, we devise a simple 1D model that involves an outward-propagating exponentially decreasing SF process since $z$ $\sim$ 10 and reproduces the radial extent and two-zone $EW$(Hα) distribution of local i+ ETGs. By simulating the 3$''$ spectroscopic SDSS aperture in this model, we find that SDSS studies at $z$ $\leq$ 1 are progressively restricted to the inner (SF-devoid LINER) zone and miss an increasingly larger portion of the Hα-emitting periphery. This leads to the incorrect spectroscopic classification of these inside-out growing galaxies as retired ETG/LINERs and also to a severe underestimation of their total star formation rate (SFR) in a manner inversely related to $z$. More specifically, the SFR inferred from the Hα luminosity registered within the SDSS fiber is reduced by 50% at $z$ $\sim$ 0.86, reaching only 0.1% of its integral value at $z$ = 0.1. We argue that the aperture-driven biases described above pertain to any morphological analog of i+ ETGs (e.g., SF-quiescent bulges within star-forming disks), regardless of whether it is viewed from the perspective of inside-out growth or inside-out SF quenching, and might be of considerable relevance to galaxy taxonomy and studies of the cosmic SFR density as a function of $z$.

Key words. galaxies: elliptical and lenticular, cD – galaxies: nuclei – galaxies: ISM – galaxies: star formation

1. Introduction

Studies of large extragalactic samples with single-fiber spectroscopy from the SDSS (York et al. 2000) and GAMA (Driver et al. 2009) have largely been relying on the assumption that aperture-effects are negligible or can be accounted for in a statistical sense. For example, Kewley et al. (2005) reported that the condition of the 3$''$ SDSS fiber enclosing $\sim$20% of the total emission of a galaxy suffices for minimizing systematic and random aperture-related errors, and recommended selecting samples at redshifts $z$ $>$ 0.04. More generally, numerous single-fiber studies (e.g., Kauffmann et al. 2003; Brinchmann et al. 2004; Tremonti et al. 2004) are based on the assumption that the spectroscopic aperture encompasses a representative probe of the spectrum of a galaxy, thus astrophysical quantities derivable

* Based on observations collected at the Centro Astronómico Hispano Alemán (CAHA) at Calar Alto, operated jointly by the Max-Planck-Institut für Astronomie (MPIA) and the Instituto de Astrofísica de Andalucía (CSIC).

from it (e.g., the Hα luminosity) are either characteristic for a galaxy as a whole or can be converted into integral ones through simple parametrizations.

This rationale essentially permeates the entire work that has dealt with large extragalactic probes and their evolution with $z$ in the era of SDSS and GAMA, and has gone a long way in our current understanding of a wide range of topical issues, for example, related to the dependence of the star formation rate (SFR) and specific SFR on stellar mass ($M_\star$), the cosmic evolution of the SFR density, and the spectral galaxy classification on the basis of diagnostic emission-line ratios (e.g., [NII]6584/Hα vs. [OIII]5007/Hβ, Baldwin et al. 1981, hereafter BPT). For instance, determinations of integral SFRs have by necessity had to rely on an extrapolation of emission-line measurements within the spectroscopic aperture assuming that the Hα scales with the underlying stellar continuum throughout the galaxy extent or is linked to broad-band colors. For example, Hopkins et al. (2003) estimated integral SFRs from the Hα luminosity within the spectroscopic aperture and assumed
a constant equivalent width \((EW(H\alpha))\) throughout the galaxy extent. Similarly, Brinchmann et al. (2004) employed a probabilistic estimate for the total SFR of SDSS galaxies that relates broad-band colors with the \(H\alpha\) luminosity. An inherent weakness of these approaches obviously is that, depending on the \(z\) and the linear extent of a galaxy, the fiber spectrum can be biased toward particular luminosity entities (e.g., the brightest star-forming knot of a starburst galaxy or the non-star-forming bulge of a late-type star-forming disk), making an extrapolation to integral quantities uncertain.

The advent of integral field spectroscopy (IFS) over a large field of view (FoV), for example, from the Calar Alto Legacy Integral Field Area survey (CALIFA, Sánchez et al. 2012), has recently permitted empirical studies of aperture-effects on various physical properties of the nebular emission in late-type galaxies (for instance, \(H\alpha\) luminosity and equivalent width \(EW\), e.g., Gerssen et al. 2012; Iglesias-Páramo et al. 2013; Brough et al. 2013; Belfiore et al. 2015).

This subject has not been investigated in similar detail for early-type galaxies (ETGs), however, partly because of the faintness of their nebular emission and the associated uncertainties in studying them, and presumably also due to the widespread view that these systems are comparatively simple and spatially homogeneous in the characteristics of their stellar and nebular components. This picture has now been substantially revised through IFS studies, which continue to reveal an impressively high complexity in both (e.g., Sarzi et al. 2006; McDermid et al. 2007; Sarzi et al. 2010; Krajnović et al. 2011; Kehrig et al. 2012; Arnold et al. 2014; Houghton et al. 2013; Pracy et al. 2014; Gomes et al. 2015a, hereafter G15a), with conspicuous radial trends in stellar age (e.g., Pérez et al. 2013; González Delgado et al. 2014, G15a) and the \(EW(H\alpha)\) of local ETGs (G15a, Papaderos et al. 2013, hereafter P13). It appears to be especially important for a better understanding of aperture effects on spectroscopic BPT classifications of ETGs to investigate the gas excitation mechanism in a spatially resolved manner with IFS data.

Several studies over the past years have pointed out the role of low-level SF activity (see, e.g., Trager et al. 2000; Schawinski et al. 2007; Shapiro et al. 2010, and references therein) on the excitation of faint nebular emission in ETGs, as an alternative or supplementary mechanism to photoionization by an active galactic nucleus (AGN; e.g., Ho 2008) or the evolved \((\geq10^8\) yr) post-AGB (pAGB) (pAGB) population (e.g., Trinchieri & di Serego Alighieri 1991; Binette et al. 1994; Stasińska et al. 2008), or fast shocks (e.g., Dopita & Sutherland 1995). Observational evidence for SF in ETGs has been accumulating from multi-wavelength studies (e.g., Kaviraj et al. 2007; Gil de Paz et al. 2007; Schawinski et al. 2009; Huang & Gu 2009; Salim et al. 2012; Petty et al. 2013; Ko et al. 2014; Pan et al. 2014). For example, Kaviraj et al. (2008) found that 10–15\% of the stellar mass \((M_\star)\) in these systems has been built in a declining SF process since \(z \sim 1\), a conclusion that appears to be in line with the small fraction (~5.7\%) of blue ETGs in the local Universe with estimated SF rates (SFRs) of between 0.5 and 50 \(M_\odot/yr\) (Schawinski et al. 2008). It is also noteworthy in this context that spatially resolved studies of individual ETGs indicate an outward-increasing luminosity contribution from young-to-intermediate-age stellar populations (e.g., Fang et al. 2012; Gomes et al. 2015a).

In particular, Gomes et al. (2015a, see also G15b) identified a small fraction (~10\%) of CALIFA ETGs (classified as type i+) that show a steep \(EW(H\alpha)\) increase in their periphery. As demonstrated in a subsequent study (Gomes et al. 2016, hereafter G16), this outer \(EW(H\alpha)\) excess is due to SF, reflecting a still ongoing inside-out galaxy buildup process.

Central to our considerations in this study is the fact that the dominant fraction (60–80\%) of the total \(H\alpha\) emission in all but one i+ ETGs studied in G16 arises beyond one effective radius \(R_{eff} (\geq10^\prime)\), it thus evades detection within the 3" SDSS aperture. Our aim here is to explore aperture-effects on spectroscopic SDSS studies of type i+ ETGs and other inside-out forming galaxies as a function of cosmic time. To this end, we take a twofold approach that combines an empirical assessment of aperture biases using as templates CALIFA IFS data for the galaxies studied in G16 (Sect. 2) with simulations on the basis of a simplified inside-out galaxy growth model (Sect. 3). Our conclusions are summarized in Sect. 4.

### 2. Anatomy of type i+ ETGs and aperture biases on their spectroscopic classification

The defining characteristics of i+ ETGs were discussed in G15a-c on the basis of three CALIFA galaxies (Fig. 1). A distinctive property of the nebular component of these systems is a structure with two radial zones, the inner of which contains faint \((EW(H\alpha) \sim 1\) Å) LINER emission, the outer \((3 < EW(H\alpha) \leq 20\) Å) essentially shows HII-region characteristics.

This two-zone morphology can be best illustrated in the case of NGC 1349: Its central part \((R^* \leq 8\", equivalent to 3.4 kpc\)) shows a low, nearly constant \(EW(H\alpha)\) of 1 Å, which is consistent with gas photoionization by the evolved \((\geq10^9\) yr) post-AGB stellar component (cf., e.g., G15a), whereas the high \((\sim 10\) Å) \(EW(H\alpha)\) and BPT ratios in its periphery \((R^* \geq 8\)") imply gas photoionization by massive OB stars. Using the isophotal annuli technique (Papaderos et al. 2002, P13), we extracted the spectrum within the inner and outer zone, which are shown with the integrated spectrum overlaid in Fig. 1a. The middle panel shows the pure nebular component in the region around the \(H\alpha\) Balmer line as obtained after subtracting the best-fitting stellar model (see G15a for details). This diagram shows the significant decrease in \([NII]/H\alpha\) flux ratio from the inner to the outer zone. This effect can be better evaluated in panel c, where we illustrate the change in position of the type i+ ETGs on the BPT plane when the galaxy spectrum is sampled within successively larger annuli: Including the very faint SF rim for NGC 1167 has a marginal effect on its classification as an AGN/LINER, whereas in NGC 1349 the much brighter peripheral SF zone results in a shift downward and to the left below the LINER demarcation curve, moving the ETG into the locus of “composite SF/LINER” galaxies. Had this galaxy been observed within a FoV of \(\Omega \leq 20^\prime\), then only its central, almost emission-line free zone would have been considered in the analysis, prompting its spectroscopic classification as a retired ETG/LINER in the definition by Stasińska et al. (2008). Obviously, the same conclusion would have been drawn from SDSS or GAMA spectra (York et al. 2000; Baldry et al. 2010). The aperture of these surveys would encompass the whole ETG only beyond \(z \geq 0.45\), where its true nature is revealed. In the specific context of i+ ETGs (i.e., systems where SF is mainly confined to the galaxy periphery), the decreasing (increasing) proportion of star-forming (retired) galaxies with decreasing redshift (e.g., Stasińska et al. 2015) could therefore be partly driven by aperture effects.

In summary, a decrease in the spectroscopic aperture can result in the case of i+ ETGs in a shift upward and to the right precisely along the right wing of the “seagull” distribution on the BPT plane, that is, along the pathway connecting SF/HII galaxies with AGN/LINERs. This empirical fact calls for a critical
reconsideration of the way this right wing should be interpreted in addressing the relative role of thermal and non-thermal activity in i+ ETGs and their morphological analogs (e.g., late-type galaxies with an old, SF-devoid bulge within a more extended star-forming disk).

3. Inside-out galaxy formation and associated aperture effects

Motivated by the observational evidence laid out in G16 and in the previous section, we extend our study by considering an inside-out formation process (e.g., Pérez et al. 2013; González Delgado et al. 2014) for ETGs. This is simulated by an inside-out formation process (e.g., Pérez et al. 2013; D'Alembert 1747) with a linear sum of two arbitrary functions \( f(t - r) \) and \( g(t + r) \) that represent an incoming and outgoing wave, respectively. Since the SFR wave propagates outward as a result of the inside-out growth of the galaxy, we can write the general solution as \( \text{SFR}(r, t) = f(t - r) + g(t + r) \).

For each radial zone, the SFR\( (r, t) \) is chosen to be exponentially declining as \( \propto e^{-t/\tau} \) with an e-folding timescale of \( \tau = 1 \) Gyr, constant wave velocity \( v \), and subject to the constraint \( t \geq r/v \). This scenario is compatible with a quick cessation of SF in the inner zone (as expected, e.g., during the bulge formation) and continued residual SF in the galaxy periphery in an inside-out galaxy buildup process. For simplicity, the galaxy is constructed such as to display a constant age gradient \( \nabla t = -0.5 \text{ Gyr/kpc} \), which imposes a maximum radius as a function of lookback time of \( R_{\text{max}}(t) = (t_0 - t)/|\nabla t| \), where \( t_0 \) is the galaxy formation lookback time. For the adopted model, the galaxy grows radially at a constant speed \( v \approx 2 \text{ km s}^{-1} \), and when it attains \( R_{\text{max}} = 20 \text{ kpc} \) (at \( z \approx 0.3 \)), the linear growth ceases, yielding a typical present-day ETG radius (e.g., Gomes et al. 2015a). The Friedmann-Robertson-Walker cosmology with \( H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1} \), \( \Omega_m = 0.3 \) and \( \Omega_k = 0.7 \) was adopted, yielding 13.52 Gyr for the age of the Universe. The time \( t_0 \) of galaxy formation is taken to be \( -0.5 \) Gyr (redshift 10) after the Big Bang.

The spectral energy distribution (SED) is computed following the detailed prescriptions by G15a. The synthetic composite stellar SEDs were evaluated using the full set of ages for the simple stellar populations (SSPs) from Bruzual & Charlot (2003, hereafter BC03); they comprise ~200 spectra spanning an age between 0 and 13.52 Gyr and assume a constant solar metallicity. We note that even though emission-line luminosities and their ratios for subsolar metallicities can significantly change due to the harder, increased UV ionizing output of massive low-metallicity stars, the principal trends and conclusions inferred from the adopted inside-out galaxy growth model remain unaltered. The BC03 SSP library uses the Padova 1994 evolutionary tracks (Alongi et al. 1993; Bressan et al. 1993; Fagotto et al. 1994a,b,c; Girardi et al. 1996), the Chabrier (2003) initial mass function, and the STELIB stellar library (Le Borgne et al. 2003).
Hydrogen (Balmer, Paschen, etc.) line fluxes were computed from the total UV ionizing flux assuming case B recombination \( (T_e = 10\,000\, K \text{ and } n_e = 100\, \text{cm}^{-3}) \) with the corresponding effective recombination coefficient \( \alpha_{\text{eff}} \) and by assuming ionization-bound nebulae. The fluxes of collisionally excited lines are based on semi-empirical calibrations for a) classical HII regions (e.g., Anders & Fritze 2003), photoionized by OB stars, and b) ETG nuclei that are photoionized by post-AGB stars (old stellar populations \( \geq 1 \text{ Myr} \)) and show LINER BPT ratios (e.g., Binette et al. 1994). Therefore, the total UV ionizing flux from an exponentially declining SFR model with \( t = 1 \text{ Gyr} \) contains the combined output from a young SF plus an old post-AGB component in certain evolutionary phases that produces a luminosity-weighted average of the modeled emission lines.

The computed radial profiles for the \( \text{EW}(\text{H}\alpha) \) and light-weighted stellar age for various evolutionary stages (from 0 to 13.52 Gyr) are shown in Fig. 3. It is apparent that the \( \text{EW}(\text{H}\alpha) \), in general, decreases as a function of time, while the stellar age always increases.

The 3rd SDSS aperture was subsequently simulated on the model galaxy to evaluate aperture effects and their dependence on \( z \). In the adopted cosmological model, the linear radius projected within the SDSS fiber as a function of \( z \) was simulated on the model (Fig. 4). For \( z \leq 1 \) the SDSS aperture encompasses a progressively smaller fraction of the galaxy. Quite importantly, the fraction of \( \text{H}\alpha \) luminosity registered within the SDSS fiber (upper panel) has a much steeper decline than the fractional area covered by SDSS because the SF activity is confined to the galaxy periphery. Quantitatively, the \( \text{H}\alpha \) flux registered within the SDSS fiber decreases by 50% at \( z \sim 0.86 \), reaching only 0.1% of its integral value at \( z = 0.1 \).

Consequently, a strong aperture bias is to be expected in SFR determinations and the spectroscopic classification of inside-out assembling \( i^+ \) ETGs and their morphological analogs. To exemplify this bias, a snapshot at \( z \sim 0.1 \) is shown in Fig. 2. At this stage, in which the model galaxy has reached its maximum radius, the SDSS fiber samples a projected radius of \( 2.75 \text{kpc} \).

The fact that in \( i^+ \) ETGs (and any inside-out forming galaxy in general) nebular emission is confined to the galaxy periphery and almost absent in the central part reinforces the warning voiced by Salim et al. (2012) who pointed out that the absence of \( \text{H}\alpha \) in SDSS spectra serves as a reminder that the information from fiber spectra cannot always be extrapolated to entire galaxies.
In summary, for an inside-out assembling galaxy with the model assumption adopted here, the simultaneous linear and angular growth of the inner (SF devoid/LINER) zone will cause limited-aperture surveys to strongly underestimate the total SFR in a manner inversely related to $z$. This bias, arising at $z \lesssim 1$ and becoming progressively severer for lower $z$, could artificially increase the estimated fraction of non-star-forming (retired) galaxies over the past $\sim7$ Gyr, which would affect the galaxy classification and mimic a steeper decline of the cosmic SFR density.

4. Summary and conclusions

This study has been motivated by the recent detection of faint spiral-like features in the low-surface brightness periphery of a small subset $(\sim10\%)$ of nearby early-type galaxies (ETGs) that was reported by Gomes et al. (2015a,b) from the CALIFA integral field spectroscopic (IFS) galaxy survey. As a subsequent analysis by Gomes et al. (2016) has revealed, these features witness a still ongoing inside-out galaxy growth process and are spatially associated with an extended emission-line zone containing up to $\sim80\%$ of the total Hα emission of these galaxies. A distinctive property of the nebular component in these ETGs, classified as i+, is a structure with two radial zones, the inner of which is on the order of the galaxy effective radius $R_{\text{eff}}$ $(\sim10^7)$ and contains faint $(\text{EW}(\text{H}\alpha) \approx 1 \text{ Å})$ LINER emission, the outer $(3 \text{ Å} < \text{EW}(\text{H}\alpha) \lesssim 20 \text{ Å})$ displays Hii-region characteristics.

The question that naturally arises from the observed segregation of the nebular emission in i+ ETGs in two spatially and physically distinct concentric zones is how aperture effects might impact spectroscopic studies of these systems. To address these questions, we here adopted a combined empirical and theoretical approach, aiming at a qualitative assessment of aperture-driven biases in SDSS studies of type i+ ETGs and other inside-out forming galaxies across cosmic time.

In the first stage, we empirically demonstrated with CALIFA IFS data that for a typical i+ ETG the confinement of nebular emission to the galaxy periphery leads to a strong observational bias in spectroscopic studies with SDSS. At low redshift $(z \lesssim 0.45)$, the 3“ SDSS fiber only captures the inner (non-star-forming LINER) zone of such a galaxy, which causes it to be erroneously classified as retired, that is, as a system entirely lacking ongoing star formation (SF) and one whose faint nebular emission is solely powered by the post-AGB stellar component. The SDSS aperture progressively encompasses the outer (star-forming) zone only at higher $z$, where it can be unambiguously classified as a “composite SF/LINER”. We also empirically demonstrated that the principal effect of a decreasing spectroscopic aperture on the classification of i+ ETGs through standard [NII]/Hα vs. [OIII]/Hβ emission-line (BPT) ratios consists of a monotonic shift upward and to the right precisely along the right wing of the “seagull” distribution on the BPT plane, that is, along the pathway connecting composite SF/Hii galaxies with AGN/LINERs.

These empirical insights were further underscored through a simple 1D inside-out galaxy formation model involving an outward-propagating exponentially decreasing SF process since $z = 10$, which reproduces both the radial extent and the two-zone $\text{EW(H}\alpha)$ morphology of present-day i+ ETGs. By simulating the SDSS aperture in this model, we found that for $z \leq 1$, SDSS spectroscopy is progressively restricted to the inner (SF-devoid LINER) zone of an inside-out forming galaxy, thereby missing an increasingly larger portion of its Hα-emitting periphery. More specifically, according to our model, the Hα flux registered within the SDSS fiber decreases by 50% at $z = 0.86$, reaching only 0.1% of its integral value at $z = 0.1$.

For local ($z \approx 0.1$) i+ ETGs our model also reproduces the observed variation of BPT line-ratios with aperture sizes along the right wing of SDSS determinations, lending further support to the conjecture that spectroscopic classification on the basis of SDSS data is prone to substantial aperture effects. It is particularly important in this context that the same trend along the right wing is reproducible when the SDSS aperture is simulated on an inside-out forming galaxy since $z = 10$ $(\sim13$ Gyr) instead of using successively larger apertures for a local model-ETG.

The combined empirical and theoretical evidence from this study therefore suggests that the right wing distribution of BPT determinations for i+ ETGs and their morphological analogs (e.g., late-type galaxies with an old SF-devoid bulge centered on a more extended star-forming disk) with single-fiber spectroscopy (e.g., SDSS, GAMA) is consistent with (yet no proof for) a pure aperture effect and is naturally reproducible in an inside-out galaxy growth scenario. This calls for a closer examination of the way this right wing should be interpreted in addressing the relative role of thermal and non-thermal activity in these systems.

Finally, in the framework of the adopted inside-out galaxy formation model, the simultaneous linear and angular growth of the inner (SF devoid/LINER) zone will cause limited-aperture surveys (e.g., SDSS, GAMA) to strongly underestimate the total star formation rate (SFR) in a manner inversely related to $z$. This bias, arising at $z \lesssim 1$ and becoming progressively severer for lower $z$, could artificially increase the estimated fraction of non-star-forming (retired) galaxies over the past $\sim7$ Gyr, which would affect galaxy classification and mimic a steeper decline of the cosmic SFR density.
These considerations underscore the critical importance of IFS studies of ETGs (and galaxies in general) over their entire optical extent.

Acknowledgements. This paper is based on data from the Calar Alto Legacy Integral Field Area Survey, CALIFA (http://califa.caha.es), funded by the Spanish Ministry of Science under grant ICTS-2009-10, and the Centro Astronómico Hispano-Alemán. JMG acknowledges support by Fundación para Ciencia e a Tecnologia (FCT) through the Fellowship SFRH/BPD/69058/2009 and POPH/FSE (EC) by FEDER funding through the program Programa Operacional de Factores de Competitividade (COMPETE). P.P. is supported by FCT through the Investigator FCT Contract No. IF/01220/2013 and POPH/FSE (EC) by FEDER funding through the program COMPETE. J.M.G., P.P., I.B. and S.N.d.R acknowledge support by FCT under project FCOMP-01-0124-FEDER-092170 (Researcher FCT PhD/FSE-3212/2012), funded by FCT-MEC (PIDDAC) and FEDER (COMPETE). They also acknowledge support by the exchange programme “Study of Emission-Line Galaxies with Integral Field Spectroscopy” (SELGIFS, FP7-PEOPLE-2013-IRSES-612701), funded by the EU through the IRSES scheme. SFS acknowledges support from CONACyT-180125 and PAPIIT-IA100815 grants. Support for LG is provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute provided by the Ministry of Economy, Development, and Tourism’s Millennium Science Initiative through grant IC120009, awarded to The Millennium Institute.